NORTHROP RESEARCH AND TECHNOLOGY CENTER PALOS VERDES --ETC F/G 20/5 INVESTIGATION OF EFFICIENT CO LASER FREQUENCY TRIPLING. (U) SEP 79 H KOMINE, E A STAPPAERTS, A S PERFER F29601-78-C-0068 NRTC79-13R AFWL-TR-79-71 NL AD-A080 810 UNCLASSIFIED 1 = 2 AGSL N

79-71

INVESTIGATION OF EFFICIENT CO LASER FREQUENCY TRIPLING

H. Komine

E. A. Stappaerts

A. S. Gerwer

Northrop Corporation Northrop Research and Technology Center One Research Park Palos Verdes Peninsula, CA 90274

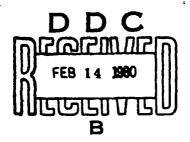
September 1979



Final Report

Approved for public release; distribution unlimited.

THE TO SEE TO SEE A MAINTINABLE. SIGNIFICANT BUNDAN OF PAGES WHICH DO NOT REPRODUCE LEGIBLY.



AIR FORCE WEAPONS LABORATORY Air Force Systems Command Kirtland Air Force Base, NM 87117

This final report was prepared by the Northrop Research and Technology Center, Palos Verdes Peninsula, California, under Contract F29601-78-C-0068, Job Order 317J0522 with the Air Force Weapons Laboratory. Maj Jerry J. Perrizo (ALE) was the Laboratory Project Officer-in-Charge.

When US Government drawings, specifications, or other data are used for any purpose other than a definitely related Government procurement operation, the Government thereby incurs no responsibility nor any obligation whatsoever, and the fact that the Government may have formulated, furnished, or in any way supplied the said drawings, specifications, or other data, is not to be regarded by implication or otherwise, as in any manner licensing the holder or any other person or corporation, or conveying any rights or permission to manufacture, use, or sell any patented invention that may in any way be related thereto.

This report has been authored by a contractor of the United States Government. The United States Government retains a nonexclusive, royalty-free license to publish or reproduce the material contained herein, or allow others to do so, for the United States Government purposes.

This report has been reviewed by the Information Office and is releasable to the National Technical Information Service (NTIS). At NTIS, it will be available to the general public, including foreign nations.

This technical report has been reviewed and is approved for publication.

JERRY J. PERRIZO

Major, USAF Project Officer

William P. Burckel

Major, USAF

Chief, Pulsed Laser Branch

FOR THE DIRECTOR

ARMAND D. MAIO Colonel, USAF

Chief, Advanced Laser Technology Div

DISCLAIMER NOTICE

THIS DOCUMENT IS BEST QUALITY PRACTICABLE. THE COPY FURNISHED TO DDC CONTAINED A SIGNIFICANT NUMBER OF PAGES WHICH DO NOT REPRODUCE LEGIBLY.

UNCLASSIFIED

(BAFWL, SBIE)

(/9) REPORT DOCUMENTATION PAGE	READ INSTRUCTIONS BEFORE COMPLETING FORM
AFWL-TR-79-71, AD-E200 137	N NO. 3. RECIPIENT'S CATALOG NUMBER
4. TITLE me Submits	DANS OF REPORT & PERIOD COVER
INVESTIGATION OF EFFICIENT CO LASER FREQUENCY/	Final Report
	NRTC 79-13R
H. Komine E. A Stappaerts A. S. Gerwer	F296Ø1-78-C-ØØ68
Northrop Research and Technology Center One Research Park Palos Verdes Peninsula, CA 90274	10. PROGRAM ELEMENT, PROJECT, TAS AREA & WORK UNIT NUMBERS 63605F/317J0522
11. CONTROLLING OFFICE NAME AND ADDRESS	(1) Service 3070
Air Force Weapons Laboratory (ALP) Kirtland Air Force Base, NM 87117	13. NUMBER OF PAGES 136
MONITORING AGENCY NAME & ADDRESS(II different from Controlling Of	ice) 15. SECURITY CLASS. (of this report)
(12) +14 +1	UNCLASSIFIED
1474	15e. DECLASSIFICATION, DOWNGRADING
Approved for public release; distribution unl 17. DISTRIBUTION STATEMENT (of the abstract entered in Block 20, if different	
Approved for public release; distribution unl	
Approved for public release; distribution unline of the abstract entered in Block 20, it different to the abstract entered in Block 20, it different enter	
Approved for public release; distribution unline of the electron entered in Block 20, it different to the electron entered in Block 20, it differe	nt (rom Report)
Approved for public release; distribution unl	mt (rom Report)
Approved for public release; distribution unline provided in Block 20, it dittered to the abetract entered in Block 20, it dittered to the supplementary notes 19. Key words (Continue on reverse side if necessary and identify by block notes to the provided in the provid	mber) resonant enhancement schemes, resonant enhancement schemes, t CO laser frequency tripling ode calculations of nonlinear iency limitations have been ing to three different resonan show that direct frequency er, a two-step conversion proc y provide large enhancement

URITY CLASSIFICATION OF THIS PAGE (When Deta Entered)

499 696

13

TABLE OF CONTENTS

1.0	SUMMAR	RY	1
2.0	INTROD	DUCTION	3
3.0	THIRD SUSCEP	HARMONIC AND SUM FREQUENCY GENERATION: NONLINEAR PTIBILITY ANALYSIS AND CALCULATION	5
	3.1	Third-Order Susceptibility $\chi^{(3)}$	7
	3.2	Resonance Ennancement Schemes	9
	3.3	Nonlinear Susceptibility $\chi^{(3)}$ Code	12
		3.3.1 Type I Scheme	12
		3.3.2 Type II Scheme	21
		3.3.3 Type III Scheme	24
	3.4	$x^{(3)}$ Calculation Results	30
		3.4.1 Type I Scheme	30
		3.4.2 Type II Scheme	39
		3.4.3 Type III Scheme	41
4.0	EFFICI	IEMCY LIMITATION AND PHASE-MATCHING ANALYSIS	44
	4.1	Linear Processes	45
		4.1.1 Absorption Coefficient and Refractive Index at Pump Frequencies	45
		4.1.2 Absorption Coefficient and Refractive Index at Generated Frequencies	49
		4.1.3 Population Transfer and Dynamic Phase Mismatch	52
		4.1.4 Thermal Defocusing	53
	4.2	Nonlinear Processes	54
		4.2.1 Two-Photon Absorption	54
		4.2.2 Quadratic Kerr Effect	55
		4.2.3 Stimulated Raman Scattering	58
		4.2.4 Three-Photon Absorption	62
		4.2.5 Gas Breakdown	63
		4.2.6 Pump Depletion	64
	4.3	Optimum Scheme	-65
5.0	MULTIL	INE THE AND SFE ANALYSIS	_ 6 8
	5.1	Efficient THG and SFG Optimization	68
	5.2	Two-Step Frequency Conversion	69
		· · · · · · · · · · · · · · · · · · ·	•

TABLE OF CONTENTS (Continued)

6.0	EXPER	EXPERIMENTAL PROGRAM				
	6.1	Approach	74			
	6.2	Experimental Facility	74			
	6.3	Parametric Study	78			
7.0	CONCL	LUSION	79			
8.0	REFER	80				
APPEN	DIX A		83			
APPEN	DIX B		116			

ACCESSION	l for	
NTIS	White Section	n 🖊
DDC	Buff Section	
UNANNOU	NCED	
JUSTI ICA	10N	
	TON/AVAILABILITY COL	
Dist. A	VAIL and/or SPI	C. I. C.

LIST OF FIGURES

FIGURE		
1.	Three Types of Resonance Enhancement	10
2.	x ⁽³⁾ Flow Chart	20
3.	Nonlinear Susceptibility of CO^{18} for Third Harmonic Generation	37
4(a).	DC1 Refractive Index vs'Frequency	46
(b).	DC# Absorption Coefficient vs Frequency	46
5(a).	DBr Refractive Index vs Frequency	47
(b).	DBr Absorption Coefficient vs Frequency	47
6(a).	NO Refractive Index vs Frequency	48
(b).	NO Absorption Coefficient vs Frequency	48
7(a).	DF Refractive Index vs Frequency	50
(b).	DF Absorption Coefficient vs Frequency	50
8(a).	HC1 Refractive Index vs Frequency	51
(b).	HCl Absorption Coefficient vs Frequency	51
9.	Normalized $ \mathbf{x}^{SFG} $ vs HD Q(1) Two-Photon Resonance Frequency Detuning	70
10.	Normalized $ \mathbf{x}^{SFG} $ vs Density	71
11.	Normalized χ^{KERR} and χ^{TPA} vs HD Q(1) Two-Photon Resonance Frequency Detuning	72
12.	Schematic of Two-Step CO Laser Sum Frequency Generation	73
13.	Sum Frequency Generation Experiment Block Diagram	75
14.	Fixed IR Source Block Diagram	75
15.	Tunable IR Source Block Diagram	76
16	Schematic of Evnonimental Annamatus	7.9

LIST OF TABLES

TABLE		
1.	Nonlinear Susceptibility $x^{(3)}$	8
2.	x ⁽³⁾ Formula	9
3.	Type I Scheme Optimum Pump Frequencies	11
4.	Type II Scheme Molecules: Two-Photon Resonance Frequency	11
5.	Product of Rotational Matrix Elements for Λ = 0 Molecules	14
6.	$W(J_a, J_b, J_c, J_d)$ for $\Lambda = 1$ Molecules	17
7.	$\xi_\alpha(a,b)$ in Terms of Mixing Coefficients and Reduced Rotational Matrix Elements	19
8.	Terms in the Ω -Path Summation	19
9.	Type II Nonlinear Susceptibility	25
10.	Type I Scheme Molecular Parameter References	30
11.	Type I $x^{(3)}$ Calculation Results: $c0^{18}$	31
12.	Type I $x^{(3)}$ Calculation Results: NO ¹⁶	32
13.	Type I $\chi^{(3)}$ Calculation Results: DC135	33
14.	Type I $\chi^{(3)}$ Calculation Results: DC ℓ^{37}	34
15.	Type I $\chi^{(3)}$ Calculation Results: DBr ⁷⁹	35
16.	Type I $\chi^{(3)}$ Calculation Results: DBr 81	36
17.	Type I THG Survey Calculation	38
18.	Type II Scheme Molecular Parameter References	39
19.	Type II THG Survey Calculation	40
20.	Type III Scheme Molecular Parameter References	41
21.	Type III $\chi^{(3)}$ Calculation Results: HC1 35	42
22.	Type III $x^{(3)}$ Calculation Results: DF	43
23.	Vibrational Raman Gain Coefficients	60
24.	Efficiency Limitation Analysis: Summary	66
25.	Coherent IR Source Parameters	77

1.0 SUMMARY

A detailed analysis on the feasibility of efficient CO laser frequency tripling in molecular gases has been carried out. The results of the study indicate that direct frequency tripling of multiline CO laser output leads to small conversion efficiencies based on the nonlinear susceptibilities and the efficiency limiting processes of the molecules surveyed. However, the analysis of the three resonance enhancement schemes shows that two-photon resonant SFG and THG in hydrogen molecules are potentially efficient frequency conversion processes if the pump frequencies can satisfy the resonance condition.

In the type I resonance enhancement scheme, pump absorption leading to dynamic phase mismatches is likely to be the primary efficiency limiting process. Since this scheme requires near-resonant conditions at one-, two-, and three-photon resonances, the pump absorption is always present and inherently restricts the application of the type I scheme to short pump pulses.

The type II scheme, which is based on two-photon resonance enhancement, avoids the dynamic phase mismatch caused by pump absorption. However, other competing nonlinear processes become significant at the high pump intensities required for efficient conversion. Although two-photon absorption, quadratic Kerr effect, and stimulated Raman scattering ultimately limit the efficiency, near unity THG and SFG conversion efficiencies are predicted under optimum conditions. The parameters that govern these conditions are the two-photon resonance frequency detuning and Kerr-induced phase shifts.

The type III scheme analysis and the related $\chi^{(3)}$ calculations which were performed utilizing three-photon resonances in a number of infrared-active molecules show that relatively small conversion efficiencies can be expected for this resonance enhancement scheme. The principal efficiency limitation in the type III scheme is optical gas breakdown at high pump intensities. The high pump intensities are necessary to compensate for relatively small nonlinear susceptibilities.

Efficient multiline frequency up-conversion of CO laser frequencies requires resonantly enhanced THG and/or SFG processes for a number of frequency combinations. The nonlinear medium must also allow simultaneous phase-matching for

different combinations of the pump frequencies. These requirements suggest that the type II scheme is more suitable for multiline pumping than the two other schemes. When the two-photon resonance condition is satisfied, the SFG nonlinear susceptibilities for various combinations of three pump frequencies are very similar. The type II candidate molecules such as $\rm H_2$ and HD have very small dispersion at the pump and the generated frequencies. This property is desirable for the simultaneous phase-matching of the various pump frequency combinations.

Efficient CO laser output spans a frequency range between 1920 and 2030 cm $^{-1}$. Analysis of two-photon resonances in H $_2$ and HD indicates that the sum of two pump frequencies lies in between the strong Q-branch resonances of H $_2$ and HD. This leads to relatively small nonlinear susceptibilities for direct THG and SFG. Further investigation of competing effects shows that stimulated Raman scattering may be significant under certain conditions. In particular, stimulated rotational Raman scattering can become an efficient nonlinear process in H $_2$. The Raman shifted frequencies may participate further in other nonlinear interactions such as induced two-photon absorption and sum frequency generation. The Raman-shifted frequencies in H $_2$ and the original pump frequencies closely match the Q-branch two-photon resonances in HD. This suggests that a two-step frequency conversion involving an initial Raman shifting in H $_2$ followed by sum frequency generation in HD is a potentially efficient process for multiline pumping. The two-step conversion process leads to output wavelengths in the 1.77 and 1.90 μ m region.

These results indicate that two-photon resonantly enhanced sum frequency generation in HD is the most promising approach to up-convert multiline CO laser frequencies. In order to verify this feasibility, an experimental investigation of SFG in HD is recommended for future study. The investigation should consist of setting up an experimental facility to generate tunable IR frequencies in the 5-6 μm region and performing parametric SFG experiments using the generated frequencies.

2.0 INTRODUCTION

Efficient frequency up-conversion of high power infrared gas lasers is of considerable interest due to the advent of very efficient IR lasers. For example, the frequency conversion of CO laser output to shorter wavelengths would provide high power coherent radiation suitable for atmospheric transmission with smaller beam control and pointing optics. Recent experimental and theoretical studies indicate that IR laser frequency tripling in molecular media is indeed possible. High conversion efficiencies at reasonable pump intensities are predicted using resonance enhancement of the third order non-linear susceptibility due to vibrational states. 1-6

The resonance enhancement of frequency up-conversion processes is a widely used technique which is particularly useful for infrared laser frequency up-conversion in molecular media. The nonlinear medium may consist of infrared-active or Raman-active molecular species. In the IR-active molecules, the fundamental and overtone transitions provide one-, two-, and three-photon resonances in addition to contributions from the electronic states. The Raman-active molecules have energy level structures suitable for two-photon resonances. These resonances may yield a very significant enhancement of the nonlinear susceptibility leading to potentially high conversion efficiencies.

Several recent investigations have been devoted to frequency tripling of the ${\rm CO}_2$ laser radiation. Although earlier results of these investigations were not promising, some very recent progress in the demonstration of ${\rm CO}_2$ laser frequency tripling indicates that the experimental conversion efficiencies are approaching the theoretically predicted values. 2,3,4 Analysis of the particular resonance enhancement schemes used in the ${\rm CO}_2$ experiments shows that a similar technique is applicable to ${\rm CO}$ laser frequency tripling for generating high power coherent radiation at 1.7 μm . Since the ${\rm CO}$ laser output consists of several frequencies, sum frequency generation may occur simultaneously with frequency tripling.

Because of the complexity created by the multitude of CO spectral lines, as many schemes as possible should be considered. For this reason, three different resonance enhancement schemes have been analyzed in terms of third harmonic

and sum frequency generation in several different molecular media. The basic concept of two of these schemes has been discussed in the literature. $^{1-6}$ Another scheme conceived at the Northrop Research and Technology Center (NRTC) involves a different type of resonance enhancement which may solve some of the problems inherent in the other schemes.

The details of the three schemes and the analysis and calculations of third-order susceptibilities for each of the schemes are described in Section 3. Section 4 discusses the efficiency limiting processes and phase-matching analysis, which are essential in understanding the optimum device performance characteristics and conversion efficiencies. Section 5 analyzes the effect of a multiline pump source on the third harmonic and sum frequency generation efficiencies and suggests a potentially efficient two-step frequency conversion scheme based on an intermediate frequency shifting technique. Recommendations for an experimental program aimed at verification of theoretical calculations are presented in Section 6.

3.0 THIRD HARMONIC AND SUM FREQUENCY GENERATION: NONLINEAR SUSCEPTIBILITY ANALYSIS AND CALCULATION

Optical third harmonic generation (THG) or frequency tripling is described by a microscopic nonlinear susceptibility tensor $\chi^{(3)}$ which relates the cubic power of the incident electric field amplitude to the generated polarization in the medium. More generally, the quantity $\chi^{(3)}$ relates a product of three electric field amplitudes to the generated polarization oscillating at the sum of the three field frequencies. This is referred to as sum frequency generation (SFG).

The theory of optical frequency mixing has been well established and experimentally verified. The basic quantity that enters into the equations which describe the THG and SFG processes is the macroscopic nonlinear polarization of the medium. For the case of three monochromatic (plane-wave) applied fields, the generated polarization at the sum frequency can be expressed as:⁷

$$P_{s}^{(3)}(z,t) = \frac{1}{2} P_{s}(z) e^{-i\omega_{s}t} + c. c.$$

$$P_{s}(z) = \frac{N}{4} Z x_{s}^{(3)} (\omega_{p}, \omega_{q}, \omega_{r}) E_{p}(z) E_{q}(z) E_{r}(z)$$
(1)

 $x \exp [i(k_p + k_q + k_r)z]$

where

The factor Z is the number of distinguishable permutations of the applied field amplitudes: Z = 6 for three distinct (including sign) frequencies, Z = 3 for a pair of equal frequencies, and Z = 1 for $\omega_p = \omega_q = \omega_r$. The other quantities N and $\chi^{(3)}_s(\omega_p, \omega_q, \omega_r)$ are the total number density and microscopic (molecular) third-order susceptibility.

The macroscopic nonlinear polarization provides the source term for the wave equation governing the growth of the generated field. In the slowly-varying amplitude approximation, the wave equation reduces to:

$$\frac{\partial E_{S}(z)}{\partial z} = \frac{i \eta_{S}}{2 \eta_{S}} P_{S}(z) e^{-i k_{S} z}$$
 (2)

where

$$n_s$$
 = the refractive index at w_s

$$k_s = \frac{n_s w_s}{c}$$

$$T_i = (\mu_0/\epsilon_0)^{\frac{1}{2}}$$
, the impedance of free space

Substitution of the expression for $P_{S}(z)$ from expression (1) into (2) yields

$$\frac{\partial E_s(z)}{\partial z} = \frac{i \pi_i \omega_s^N}{8 n_s} Z_{x_s}^{(3)} E_p(z) E_q(z) E_r(z) e^{-i\Delta kz}$$
 (3)

where the wave vector mismatch, Δk , is defined by

$$\Delta k = k_s - (k_p + k_q + k_r) \tag{4}$$

If the depletion of the applied fields is neglected, equation (3) can be integrated directly over the interaction length, L:

$$E_s(L) = \frac{i \, \pi \, \omega_s \, NL}{8 \, n_s} \, Z \, \chi_s^{(3)} \, E_p \, E_q \, E_r \, e^{-i\Delta k L/2} \, \text{sinc (L/2)} \quad (5)$$

The electric field intensities are given by

$$I_{\ell} = \frac{n_{\ell} |E_{\ell}|^2}{2\hat{i}_{\ell}} \qquad (\ell = p,q,r)$$
 (6a)

$$I_{s} = \frac{n_{s} |E_{s}|^{2}}{2T_{l}} \tag{6b}$$

Equations (5) and (6) are applicable to third harmonic generation as well as to sum frequency generation. For example, the third harmonic field at $\omega_s = 3\omega_1$ is given by

$$E_{3\omega_1}(L) = \frac{3T_i \omega_1 LN}{8 n_s} \chi^{THG} E_1^3 e^{-i\Delta kL/2} \text{ sinc } (\Delta kL/2)$$
 (7)

Accordingly, the field intensity of the third harmonic is given by

$$I_{THG} = \frac{1}{16} \frac{\eta^4}{n_s n_1^3} (3\omega_1)^2 L^2 N^2 |\chi^{THG}|^2 I_1^3 sinc^2 (\Delta kL/2) (8)$$

where

 I_{THG} = the field intensity at $3\omega_1$

 I_1 = the field intensity at ω_1

 $\chi^{THG} \equiv \chi_{3\omega_1}^{(3)} (\omega_1, \omega_1, \omega_1)$

= the nonlinear susceptibility for THG.

All of the parameters in Equation (8) are expressed in MKS units. In sum frequency generation ω_s may be either a sum of three different frequencies $(\omega_s = \omega_1 + \omega_2 + \omega_3)$ or a sum of one frequency and twice another frequency (e.g., $\omega_s = 2\omega_1 + \omega_2$). The generated field intensities for these two cases are given by

$$I_{SFG} = \frac{9}{4} \frac{\eta^4}{n_s n_1 n_2 n_3} \omega_s^2 N^2 L^2 \left[\chi_s^{(3)}(\omega_1, \omega_2, \omega_3) \right]^2 I_1 I_2 I_3 \operatorname{sinc}^2 (\Delta k L/2)$$
 (9)

where $\omega_s = \omega_1 + \omega_2 + \omega_3$, and

$$I_{SFG'} = \frac{1}{16} \frac{T_1^4}{n_s n_1^2 n_2} (\omega_s')^2 N^2 L^2 |\chi_s^{(3)}(\omega_1, \omega_1, \omega_2)|^2 I_1^2 I_2^2$$

$$\times \operatorname{sinc}^2 (\Delta k L/2)$$
(10)

where $w_s' = 2w_1 + w_2$.

Equations (8), (9), and (10) indicate that the generated intensities for THG and SFG depend on the molecular parameters through $\chi^{(3)}$ and Δk . Thus, efficient THG and SFG from CO laser output requires molecular species in which large values of $\chi^{(3)}$ can be obtained at the CO laser frequencies. Furthermore, the phase mismatch, ΔkL , must be minimized in order to obtain a value of $\sin^2(\Delta kL/2)$ which is as close to unity as possible. More detailed analyses of these important considerations are presented in the following sections.

3.1 Third Order Susceptibility $\chi^{(3)}$

The derivation of the nonlinear susceptibility tensor is based on density matrix perturbation calculations for atoms and molecules interacting with external electric fields. The formula for $\chi^{(3)}$ is given by the set of equations in Table 1. The application of the $\chi^{(3)}$ formula for molecules involves summation over intermediate states, as shown by the expressions in Table 2. In principle,

all of the rotational, vibrational, and electronic states of the molecule are required for the calculation. However, various approximations can be used to simplify the summations under certain conditions. For example, if the applied field frequencies or their combinations are nearly resonant with the molecular transition frequencies of the nonlinear medium, a large enhancement of the frequency factor results from the intermediate states associated with the resonances. This resonance enhancement not only gives large susceptibilities but also reduces the number of intermediate states which are necessary for accurate computation.

TABLE 1. NONLINEAR SUSCEPTIBILITY $x^{(3)}$

TABLE 1. NONLINEAR SUSCEPTIBILITY
$$\chi^{(3)}$$

Process: $\omega_p + \omega_q + \omega_r \rightarrow \omega_s$
 $\chi_s^{(3)}(\omega_p, \omega_q, \omega_r) = \mathbf{S}\left(\frac{-1}{6 \, \mathrm{h}^3}\right) \sum_{\mathrm{abcd}} \rho_{\mathrm{aa}}^{(0)} \mu_{\mathrm{ab}} \mu_{\mathrm{bc}} \mu_{\mathrm{cd}} \mu_{\mathrm{da}} \Gamma_{\mathrm{abcd}}(\omega_1, \omega_2, \omega_3)$
 $\mathbf{S} \equiv \mathrm{sum} \ \mathrm{over} \ \mathrm{all} \ \mathrm{permutations} \ \mathrm{of} \ (\omega_p, \omega_q, \omega_r) \ \mathrm{for} \ (\omega_1, \omega_2, \omega_3)$
 $\rho_{\mathrm{aa}}^{(0)} \equiv \mathrm{population} \ \mathrm{distribution} \ \mathrm{of} \ \mathrm{molecules}$
 $\mu_{i,j} \equiv \mathrm{electric} \ \mathrm{dipole} \ \mathrm{matrix} \ \mathrm{element}$
 $F_{\mathrm{abcd}}(\omega_1, \omega_2, \omega_3) \equiv \mathrm{frequency} \ \mathrm{factor}$
 $= \frac{1}{(\omega_{\mathrm{ab}} + \mathrm{i} \Gamma_{\mathrm{ab}} + \omega_1 + \omega_2 + \omega_3)(\omega_{\mathrm{ac}} + \mathrm{i} \Gamma_{\mathrm{ac}} + \omega_2 + \omega_3)(\omega_{\mathrm{ad}} + \mathrm{i} \Gamma_{\mathrm{ad}} + \omega_3)}$
 $+ \frac{1}{(\omega_{\mathrm{ab}} - \mathrm{i} \Gamma_{\mathrm{ab}} - \omega_1)(\omega_{\mathrm{ac}} + \mathrm{i} \Gamma_{\mathrm{ac}} + \omega_2 + \omega_3)(\omega_{\mathrm{ad}} + \mathrm{i} \Gamma_{\mathrm{ad}} + \omega_3)}$
 $+ \frac{1}{(\omega_{\mathrm{ab}} - \mathrm{i} \Gamma_{\mathrm{ab}} - \omega_1)(\omega_{\mathrm{ac}} - \mathrm{i} \Gamma_{\mathrm{ac}} - \omega_1 - \omega_2)(\omega_{\mathrm{ad}} + \mathrm{i} \Gamma_{\mathrm{ad}} + \omega_3)}$
 $+ \frac{1}{(\omega_{\mathrm{ab}} - \mathrm{i} \Gamma_{\mathrm{ab}} - \omega_1)(\omega_{\mathrm{ac}} - \mathrm{i} \Gamma_{\mathrm{ac}} - \omega_1 - \omega_2)(\omega_{\mathrm{ad}} + \mathrm{i} \Gamma_{\mathrm{ad}} + \omega_3)}$

$$x^{(3)} = \mathbf{S}\left(\frac{-1}{6 \, \mathrm{h}^3}\right) \sum_{[Y]} \sum_{[V]} \varphi_V \sum_{[J]} f_J \sum_{[K]} \varphi_r \, (K) \, F_{abcd}$$

$$\varphi_V = \mu_{ab}^V \, \mu_{bc}^V \mu_{cd}^V \mu_{da}^V \quad \text{with} \quad V_a = 0$$

$$f_J = Q^{-1} \, (2J+1) \, \mathrm{e}^{-E(J)/kT} \, (Q = \text{partition function})$$

$$\psi_R = \frac{1}{2 \, J+1} \sum_{[K]} \mu_{ab}^R \mu_{bc}^R \mu_{cd}^R \mu_{da}^R$$

$$[K] = \text{set of} \, (J_a, J_b, J_c, J_d) \, \text{allowed by the selection rules}$$

$$\text{with} \, J_a = J$$

$$F_{abcd} = \text{frequency factor determined by} \, (\omega_1, \omega_2, \omega_3) \, \text{and}$$

$$\text{molecular transition frequencies}$$

3.2 Resonance Enhancement Schemes

The resonance enhancement schemes considered for CO laser frequency tripling are based on one, two, and/or three photon resonances in infrared-active and Raman-active diatomic molecules. Figure 1 illustrates the three different schemes. The difference between the transition resonance frequency and the pump frequency or the combination of the pump frequencies is the frequency detuning which determines the resonance enhancement of the frequency factor.

The type I scheme utilizes near-resonant frequency detunings at the fundamental and the first two overtone transitions corresponding to the vibrational levels v=1, 2, and 3. The candidate molecules are IR active species with fundamental frequencies near 2000 cm⁻¹. Table 3 lists the molecules and the optimum THG pump frequency ranges for two and three photon resonance enhancement.

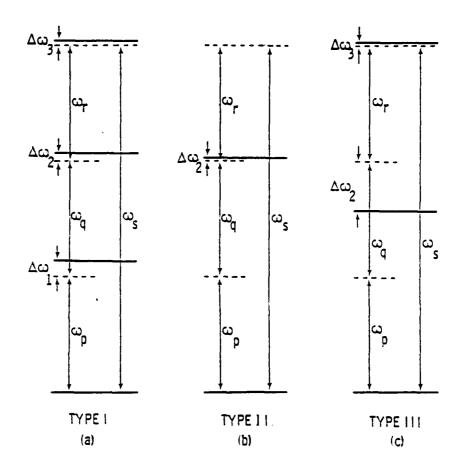


FIGURE 1. THREE TYPES OF RESONANCE ENHANCEMENT

TABLE 3. TYPE I SCHEME OPTIMUM PUMP FREQUENCIES

Molecule	THG Optimum Pump Free	
	<u> 2 Photon Resonant</u>	3-Photon Resonant
CO18	2050 - 2065	2055 - 2060
DCL 35,37	1990 - 2025	2005 - 2020
DBr ^{79,81}	1860 - 1890	1805 - 1810
NO	1840 - 1890	1830 - 1860

The type II scheme is based on two-photon resonance in Raman-active molecules, The candidate molecules and the optimum two-photon resonant pump frequencies are listed in Table 4.

TABLE 4. TYPE II SCHEME MOLECULES
Two-Photon Resonance Frequency

Molecule	Two-Photon T Branch (J)	ransition ω (cm ⁻¹)	Optimum Pump Frequency (cm ⁻¹)
H ₂	Q(0)	4161.1	2080.55
-	Q(1)	4155.2	2077.60
	Q(2)	4143.3	2071.65
	Q(3)	4125.3	2062.65
	Q(4)	4101.2	2050.60
	0(2)	3806.8	1903.40
	0(3)	3568.4	1784.20
HD	Q(0)	3632.1	1816.05
	Q(1)	3628.2	1814.10
	Q(2)	3620.5	1810.25
	Q(3)	3608.9	1804.45
	Q(4)	3593.3	1796.65
	\$(0)	3887.5	1943.75
	S(1)	4051.8	2025.90
HF	Q(0)	3961.54	1980.77
	Q(1)	3960.00	1980.00
	Q(2)	3956.90	1978.45
	Q(3)	3952.26	1976.13
	Q(4)	3946.06	1973.03
	Q(5)	3938.30	1969.15

The type III scheme derives three-photon resonance enhancement from small frequency detunings at the v=2 excited vibrational state of the molecule. The candidate molecules are DF and HC ℓ , both of which have first overtone transitions in the 5500 to 5800 cm⁻¹ range.

3.3 Nonlinear Susceptibility x (3) Code

A general third order nonlinear susceptibility code for infrared-active molecules has been developed using vibration-rotation transitions in the ground electronic state of the molecule. The code is based on the $\chi^{(3)}$ formula given in Table 2, and is capable of calculating nonlinear susceptibilities for THG, SFG, quadratic Kerr effect, two-photon absorption, and stimulated Raman effect for the type I and type III scheme molecules. The necessary input parameters are the equilibrium molecular energy level constants, gas temperature, the number of vibrational and rotational intermediate states, the dipole matrix elements, and the three pump frequency values. For the type III calculation, the code computes only the near-resonant contributions from the R-branch overtone transitions. The $\chi^{(3)}$ code consists of the pump and the generated frequencies as well as the real part, the complex part, and the modulus of the nonlinear susceptibility tensor.

The $\chi^{(3)}$ calculation for the type II resonance enhancement scheme involves virtual vibronic transitions in Raman-active molecules. According to the literature, the perturbation calculation requires extensive computation involving vibronic matrix elements which are not generally available. However, $\chi^{(3)}$ values may be obtained from differential Raman scattering cross section data and appropriate frequency factor scaling. This procedure is believed to be a reliable method.

The details of the $\chi^{(3)}$ program structure and the procedures used in the computation are described in the following sections.

3.3.1 Type I Scheme

The calculation of nonlinear susceptibilities for molecular media in principle requires a knowledge of all of the energy levels and of all of the transition matrix elements for the molecules of the nonlinear medium. When resonance

enhancement occurs, however, a knowledge of only a small group of intermediate states may be sufficient to determine good approximate values of $\chi^{(3)}$. The accuracy of this approximation depends on the frequency detunings. Thus a reliable resonance enhancement calculation requires a precise knowledge of the molecular energy level scheme. The molecular constants taken from spectroscopic data are generally adequate for computing frequency detunings to within approximately 1 cm⁻¹.

The equations for computing the molecular energy levels are summarized below. 8,9 Each level is characterized by vibrational and rotational quantum numbers. The total energy, T(v,J) is expressed as a sum of the vibrational term, G(v), and the rotational term, $F_v(J)$.

$$T(v, J) = G(v) + F_v(J)$$
 (11)

$$G(v) = \omega_{e}(v+\frac{1}{2}) - \omega_{e}x_{e}(v+\frac{1}{2})^{2} + \omega_{e}y_{e}(v+\frac{1}{2})^{3} + \omega_{e}z_{e}(v+\frac{1}{2})^{4} + \dots$$
 (12)

$$F_{v}(J) = B_{v}J(J+1) - D_{v}[J(J+1)]^{2} + H_{v}[J(J+1)]^{3} + ... (\Lambda=0)$$
 (13)

$$F_{v}(J) = -D_{v} + (-1)^{\frac{1}{2}} \cancel{1}_{v} / (2 + B_{v_{1}} (J + \frac{1}{2})^{2} - D_{v_{1}} (J + \frac{1}{2})^{4} + H_{v_{1}} (J + \frac{1}{2})^{6} + \dots$$
 (14)

where

$$B_{v} = B_{e} - \alpha_{e} (v + \frac{1}{2}) + \gamma_{e} (v + \frac{1}{2})^{2} + \dots$$
 (15)

$$D_{v} = D_{e} - \beta_{e}(v^{+\frac{1}{2}}) + \dots$$
 (16)

$$H_{\mathbf{v}} = H_{\mathbf{e}} + \dots \tag{17}$$

$$A_{v} = \lambda_{v} B_{v} \tag{18}$$

$$A_{v} = A_{v} - 2B_{v} - 2B_{v}^{2}/A_{v} + \dots$$
 (19)

$$B_{vi} = B_v + D_v + (-1)^i B_v [\lambda_v + 2\lambda_v^2 + ...]$$
 (20)

$$D_{vi} = D_{v} + (-1)^{i} B_{v} [\lambda_{v}^{3} + 6\lambda_{v}^{4} + ...]$$
 (21)

$$H_{vi} = H_{v} + (-1)^{i} B_{v} [2\lambda_{v}^{5} + 20\lambda_{v}^{6} + ...]$$
 (22)

The transition frequency between any two levels can be calculated using Equations (15) through (22). The calculated frequencies can then be used to compute the frequency denominator term in Table 1.

Direct calculation of the nonlinear susceptibility requires a variety of summations according to Table 2. Since the molecular states are labeled by vibrational (v) and rotational (J) quantum numbers, an explicit form of the expression in Table 2 requires the calculation of

$$\phi_{R} (J_{a}, J_{b}, J_{c}, J_{d}) = \frac{1}{2J+1} \sum_{\substack{m_{a} \ m_{b} \ m_{c} \ m_{d}}} \sum_{\substack{m_{c} \ m_{d} \ m_{c} \ m_{d} \ cos\theta \mid J_{d}m_{d} \rangle \langle J_{d}m_{d} \mid cos\theta \mid J_{a}m_{a} \rangle}} [\langle J_{a}m_{a} \mid cos\theta \mid J_{b}m_{b} \rangle \langle J_{b}m_{b} \mid cos\theta \mid J_{c}m_{c} \rangle$$

$$\langle J_{c}m_{c} \mid cos\theta \mid J_{d}m_{d} \rangle \langle J_{d}m_{d} \mid cos\theta \mid J_{a}m_{a} \rangle]$$
(23)

In Equation (23) the indices b, c, and d denote the vibrational or vibronic quantum numbers of the intermediate states. The variables (J_b, J_c, J_d) are the rotational quantum numbers of the intermediate states. The frequency denominator term $F_{abcd}(J_a, J_b, J_c, J_d)$, indicates the dependence of $\chi^{(3)}$ on vibrational and rotational energy levels. Equation (23) gives the product of the rotational matrix elements. The selection rules for linearly polarized fields are $\Delta J = \pm 1$ and $\Delta m = 0$ for a molecular state with $\Delta = 0$, and $\Delta J = 0$, ± 1 and $\Delta m = 0$ for a molecular state with $\Delta = 1$. Using these selection rules, $\phi_R(J_a, J_b, J_c, J_d)$ can be calculated for allowed values of J_b, J_c, J_d . The results for the $\Delta = 0$ case are summarized in Table 5.

TABLE 5. PRODUCT OF ROTATIONAL MATRIX ELEMENTS FOR Λ = 0 MOLECULES

Path	J _b	Jc	^J d	ϕ_{R} (J _a ,J _b ,J _c ,J _d) J _a =J
1	J-1	J-2	J-1	$\frac{2J (J-1)}{15 (2J-1) (2J+1)}$
2	J-1	J	J-1	$\frac{J (4J^2 + 1)}{15 (2J-1) (2J+1)^2}$
3	J+1	J	J-1	2J(J+1) 15 (2J+1) ²
4	J-1	J	J+1	2J (J+1) 15 (2J+1)2
5	J+1	J	J+1	$\frac{(J+1)(4J^2+8J+5)}{15(2J+3)(2J+1)^2}$
6	J+1	J+2	J+1	2(J+1)(J+2) 15 (2J+3)(2J+1)

The experimental data on vibrational matrix elements are available for a number of infrared-active diatomic molecules. In most cases $\Delta v = \pm 1$ transitions are well approximated by the harmonic oscillator matrix elements which are given by

$$\langle v \mid \mu \mid v-1 \rangle = \sqrt{v} \langle 1 \mid \mu \mid 0 \rangle \tag{24}$$

The matrix elements for overtone transitions ($\Delta v = 2$ and 3) may be expressed as

$$\mu_{V,0} = S_{V,0} \mu_{1,0}$$
 (25)

where $S_{v,0}$ is the strength relative to the fundamental (0 \rightarrow 1) transition. Typically, $S_{2,0}\approx 10^{-1}$ and $S_{3,0}\approx 5\times 10^{-3}$.

The population distribution in the rotational states is represented by a factor f_J . For a gaseous medium in thermal equilibrium the distribution is considered Boltzmann. The quantity $Q_{\mbox{Rot}}$ is the rotational partition function which is defined as

$$Q_{Rot} = \sum_{J=0}^{\infty} (2J+1) \exp(-hc F_0(J)/kT)$$
 (26)

For hc $\rm B_{\rm o} <\!\!< kT$, $\rm Q_{\rm Rot}$ may be approximated by

$$Q_{Rot} \cong \frac{kT}{hc B_0}$$
 (27)

The summations involving vibrational quantum numbers and frequency permutations which are needed for the Λ = 1 case are exactly the same as the summations that are required for the Λ = 0 case. However, since the rotational states have two sets of levels $(\Omega = \frac{1}{2}, \frac{3}{2})$, two distinct summations over J must be performed.

$$\chi^{(3)} \propto \sum_{v} \sum_{bcd} \mu^{4} \left[\sum_{J=\frac{1}{2}} \left(\omega = \frac{1}{2} \right) + \sum_{J=\frac{1}{2}} \left(\Omega = \frac{1}{2} \right) \right]$$
 (28)

In each summation over J, there are nineteen different paths to be summed as a result of allowed values of (J_b, J_c, J_d) .

$$\sum_{J=\frac{1}{2}} (\vec{a} = \frac{1}{2}) = \sum_{J=\frac{1}{2}} f_J (\vec{a} = \frac{1}{2}) \sum_{J_b J_c J_d} \rho(J_a, J_b, J_c, J_d) F_{abcd}$$
 (29)

In each path of rotational quantum numbers, the Ω values of the intermediate states can be either $\frac{1}{2}$ or $\frac{1}{2}$, making eight different contributions to each set of (J_a, J_b, J_c, J_d)

$$\sum_{\text{abcd}} \phi(J_a, J_b, J_c, J_d) \quad F_{\text{abcd}} = \sum_{\text{path } (J)} (-1)^s \quad \frac{W(J_a J_b J_c J_d)}{2 J_a + 1} \sum_{\text{path } (\Omega)} \psi(a, b, c, d) \quad F_{\text{abcd}}$$
(30)

where $s = J_a + J_b + J_c + J_d$. $W(J_a, J_b, J_c, J_d)$ is defined by:

$$W(J_{a},J_{b},J_{c},J_{d}) = \sum_{m_{a}} \sum_{m_{b}} \sum_{m_{c}} \sum_{m_{d}} \begin{pmatrix} J_{a} & 1 & J_{b} \\ -m_{a} & 0 & m_{b} \end{pmatrix} \begin{pmatrix} J_{b} & 1 & J_{c} \\ -m_{b} & 0 & m_{c} \end{pmatrix} \begin{pmatrix} J_{c} & 1 & J_{d} \\ -m_{c} & 0 & m_{d} \end{pmatrix} \begin{pmatrix} J_{d} & 1 & J_{a} \\ -m_{d} & 0 & m_{a} \end{pmatrix}$$
(31)

Using the properties of the summations involving products of 3j symbols expression (31) reduces to

$$W(J_{a},J_{b},J_{c}J_{d}) = \frac{(-1)^{(-J_{b}+2J_{c}+J_{d})}}{9} \left[(-1)^{J_{b}+J_{d}} \begin{cases} 1 & J_{a} & J_{b} \\ 1 & J_{c} & J_{d} \end{cases} + \sum_{k=0}^{2} \begin{cases} J_{c} & 1 & J_{b} \\ 1 & J_{a} & k \end{cases} \begin{cases} J_{c} & 1 & J_{d} \\ 1 & J_{a} & k \end{cases} h(k) \right]$$
(32)

where
$$h(k) = \frac{(-1)^k (2k+1)}{10} [3k^2 (k+1)^2 - 21 k (k+1) + 20]$$
 (33)

By specifying a particular set of rotational quantum numbers, expression (32) can be evaluated using 6'j symbol formulas, 10' and the results are summarized in Table 6.

The frequency factor is computed in the same way as was done for the $\Lambda=0$ case. The only difference is the formulae used for calculating molecular levels with quantum numbers $\{v, J, \Omega\}$.

The summation over intermediate Ω states can be written

$$\sum_{\text{path }(\Omega)} \psi(a,b,c,d) F_{\text{abcd}} = \sum_{\Omega_b} \sum_{\Omega_c} \sum_{\Omega_d} \xi(a,b) \xi(b,c) \xi(c,d) \xi(d,a) F_{\text{abcd}}$$
(34)

TABLE 6. W (J_a, J_b, J_c, J_d) FOR $\Lambda = 1$ MOLECULES

Path	J _P	J _c	³ d	w(J _a ,J _b ,J _c ,J _d), (J _a =J)
1	J-1	J-2	J-1	2 1 15 (2J-1)
2	J −1	J	J-1	$\frac{1}{15} \frac{(4J^{2}+1)}{J(2J-1)(2J+1)}$
3	J+1	J	J-1	$\frac{2}{15} \frac{1}{(20+1)}$
4	J-1	J	J+1	$\frac{2}{15}$ (23+1)
5	J+1	J	J+1	$\frac{1}{15} \frac{(4J^2+8J+5)}{(J+1)(2J+1)(2J+3)}$
6	J+1	J+2	J+1	$\frac{2}{15} \frac{1}{(2J+3)}$
7	J	J	J-1	$\frac{1}{15} \frac{(3-1)}{3(23+1)}$
3	J	j	J+1	$\frac{1}{15} \frac{(3+2)}{(3+1)(23+1)}$
9	J	J-1	J	$\frac{1}{15} \frac{(3-1)}{3(20-1)}$
10	j	J+1	J	$\frac{1}{15} \frac{(3+2)}{(3+1)(23+1)}$
11	J-1	J	J	$\frac{1}{15} \frac{(J-1)}{J(2J+1)}$
12	J+1	j	J	$\frac{1}{15} \frac{(J+2)}{J(2J-1)}$
13	J-1	J+1	3-1	$\frac{1}{15} \frac{(3+1)}{3(23-1)}$
14	J+1	J+1	J+1	$\frac{1}{15} \frac{3}{(3+1)(23+3)}$
15	J	J-1	J-1	$=\frac{1}{15}\left[\frac{(3+1)(3-1)}{3^2(23+1)(23-1)}\right]^2$
16	J	J-1	J - 1	$-\frac{1}{15} \left[\frac{J(J+2)}{(J+1)^2(2J+1)(2J+3)} \right]^2$
17	J - 1	J-1	ů	$-\frac{1}{15} \left[\frac{(J+1)(J+1)}{J^2(2J+1)(2J+1)} \right]^{\frac{1}{2}}$
19	J+1	J+1	j	$=\frac{1}{15}\left[\frac{3(3+2)}{(3+1)^2(23+1)(23+3)}\right]^{\frac{1}{2}}$
19	ů	J	3	1 (3J ² +3J-1) 15 3(3+1)(23+1)

The terms of the form \$(a,b) represent effective reduced matrix elements between states a and b when both states are expressed in the intermediate coupling scheme. In this coupling scheme, molecular states are expressed as linear combinations of unperturbed eigenfunctions with coefficients defined by the following relations:

$$\left| {\frac{{2\pi _1 }}{2}} \right\rangle _{\text{INT}} = CA(v) \left| {\frac{{2\pi _1 }}{2}} \right\rangle - CB(v) \left| {\frac{{2\pi _2 }}{2}} \right\rangle$$
 (35)

and

$$|^{2}\pi_{\frac{3}{2}}\rangle$$
 = $CA(v) |^{2}\pi_{\frac{3}{2}}\rangle + CB(v) |^{2}\pi_{\frac{1}{2}}\rangle$ (36)

where the mixing coefficients are given by:

and
$$CA(v) = \frac{X_{v} - 2 + \lambda_{v}}{2 X_{v}}$$

$$CB(v) = \frac{X_{v} + 2 - \lambda_{v}}{2 X_{v}}$$

$$X_{v} = \left[\lambda_{v}(\lambda_{v} - 4) + 4(J + \frac{1}{2})^{2}\right]^{\frac{1}{2}}$$

$$\lambda_{v} = A_{v}/B_{v}$$
(37)

The rotational reduced matrix elements are also necessary to compute ξ . For $\Omega \neq 0$ cases, these matrix elements are given by $\frac{11}{2}$

$$R_{\Omega}(J,J') = \begin{cases} \left[\frac{(J+1)^2 - \Omega^2}{J+1} \right]^{\frac{1}{2}} & \text{for } J' = J+1 \\ \left[\frac{(2J+1)\Omega^2}{J(J+1)} \right]^{\frac{1}{2}} & \text{for } J' = J \\ \left[\frac{J^2 - \Omega^2}{J} \right]^{\frac{1}{2}} & \text{for } J' = J-1 \end{cases}$$
(38)

The three different forms of ξ in terms of the expressions given in Equations (35) through (38) are given in Table 7.

TABLE 7. $\xi_{\alpha}(a,b)$ IN TERMS OF MIXING COEFFICIENTS AND REDUCED ROTATIONAL MATRIX ELEMENTS

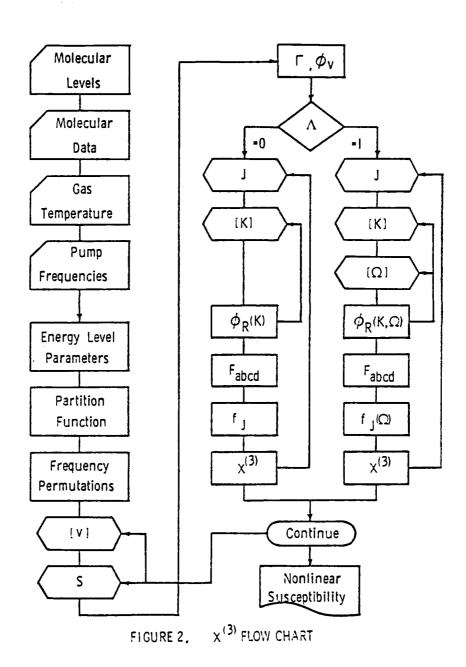
α	Ω _a	Ω _b	s _α (a,b)
1	1 2	- 2	CA(a) CA(b) $R_{\frac{1}{2}}$ (J _a ,J _b)+ CB(a) CB(b) $R_{\frac{5}{2}}$ (J _a ,J _b)
2	3 2	2	CA(a) CA(b) $R_{\frac{3}{2}}$ (J _a ,J _b) + CB(a) CB(b) $R_{\frac{3}{2}}$ (J _a ,J _b)
3	1 1 2 1 2 1 2 1 2 1 2 1 2 1 2 1 2 1 2 1	~ \2 - 2	CA(a) CB(b) $R_{\frac{1}{2}}$ (J _a ,J _b) - CA(b) CB(a) $R_{\frac{3}{2}}$ (J _a ,J _b)

In Table 8, ψ (a,b,c,d) is defined in terms of appropriate products of the effective reduced matrix elements, determined by the possible combinations (paths) of the quantum numbers, Ω_a , Ω_b , Ω_c , and Ω_d .

TABLE 8. TERMS IN THE A-PATH SUMMATION

Path	Ω ar	$\Omega_{\mathbf{a}}$ $\Omega_{\mathbf{b}}$	·²c -²d	y(a,b,c,d) $s_{\alpha}(a,b)s_{\beta}(b,c)s_{\gamma}(c,d)s_{\delta}(d,a)$				
					α	<u> </u>	<u>. </u>	δ
1	. #Q	ই	+ + 2	- 2	1	1	1	1
2	喜	Ž		<u>:</u>	1	1	3	3
3	· = = = = = = = = = = = = = = = = = = =	<u>1</u>	- <u>#</u>	- 2	1	3	3	1
4	10	12	<u> 3</u>	3 2	1	3	2	3
5	≅	3 2	÷ 📆	<u>:</u>	3	3	1	1
6	102	32	2	. Q ∵ Q	3	3	3	3
7	. <u> </u>	· 2	÷	=======================================	3	2	3	1
8	2	2	<u>3</u>	· 2	3	2	2	3
1	2	÷	÷ 2	Ž	2	2	2	2
2	<u> </u>	<u>:</u>	<u>3</u> 2	- 2	2	2	3	3
3	<u> 3</u>	· 2	Ž	. io	2	3	3	2
4	· 2	<u>;</u>		- - -	2	3	1	3
5	· Ž	12	10 3	- <u> </u> 2	3	3	2	2
6	<u>;</u>	2	<u>3</u>	2	3	3	3	3
7	2	÷ = = = = = = = = = = = = = = = = = = =	į	<u>:</u>	3	1	3	2
8	2	Ē	Ž	<u>.</u>	3	1	1	3

The expressions presented in this section constitute a general method for calculating third-order susceptibilities in IR-active molecules. Figure 2 shows a flow chart of the $\chi^{(3)}$ code based on these expressions. A listing of the computer program is given in Appendix A.



20

3.3.2 Type II Scheme

In the type II scheme, analysis of the $\chi^{(3)}$ formula shows that THG and SFG, stimulated Raman scattering (SRS), two-photon absorption (TPA), and quadratic Kerr effect share the same two-photon resonance and vibronic intermediate states. Consequently, the susceptibilities are related and may be evaluated from measured data on one of the processes. A direct relation between χ^{SRS} and differential Raman scattering cross section, $d\sigma/d\Omega$, enables the calculation of the various susceptibilities. The relation has been derived using the definitions of the scattering cross sections. A derivation consistent with the definition of $\chi^{(3)}$ of this report is outlined below.

The starting point is Placzek's definition of the "effective cross section" for scattered light due to a transition $k \rightarrow n$ in both scattering polarization directions: 12

$$Q_{kn} = \frac{2^7 \pi^5}{3 \lambda_s^4} \sum_{\rho} |(C_{\rho\sigma})_{kn}|^2$$
 (39)

[Placzek's Equation (5.5a)]

where

$$(C_{p\sigma})_{kn} = \frac{1}{h} \sum_{r} \frac{(M\sigma)_{kr} (M\rho)_{rn}}{\omega_{rk} - \omega} + \frac{(M\rho)_{kr} (M\sigma)_{rn}}{\omega_{rn} + \omega}$$
(40)

[Placzek's Equation (5.2)]

and $\sigma = 1$, 2, or 3 corresponding to the x, y, or z directions of polarization for the incident radiation, respectively

p = 1, 2, or 3 corresponding to the x, y, or z directions of polarization for the scattered radiation, respectively

 λ_c = the wavelength of the scattered radiation

$$(M_{\gamma})_{kr} = \int \psi_r^* \hat{M}_{\gamma} \psi_k d\tau$$

 \mathring{M}_{V} = the electric dipole operator of polarization specified by γ .

In the equation for $\chi^{(3)}$, the states are labeled as (a,b,c,d), so that $k=|a,J_a,m_a\rangle$ and $n=|c,J_cm_c\rangle$. Consider the case of parallel polarization $(\rho = \sigma)$

$$(Q_{a,J_{a},m_{a}\rightarrow c,J_{c},m_{c}})_{\parallel} = \frac{2^{7}\pi^{5}}{3\lambda_{s}^{4}} |(C_{\sigma\sigma})_{a,J_{a},m_{a};c,J_{c},m_{c}}|^{2}$$
(41)

Summing over the degenerate m states and dividing by the degeneracy of the initial state (according to Equation (5.5b) of Placzek) yields

$$(Q_{a,J_a} \rightarrow c,J_c)_{\parallel} = (\frac{8\pi}{3}) k_s^4 \frac{1}{g_a} \sum_{m_a} \sum_{m_c} |(C_{\sigma\sigma})_{a,J_a,m_a;c,J_c,m_c}|^2$$
 (42)

where $k_{\rm S}$ = the wavevector for the scattered radiation (= $2\pi/\lambda_{\rm S}$).

The differential Raman scattering cross section $(d\sigma/d\Omega)$ at 90° to the direction of the incident radiation and at 90° to the polarization direction of the incident radiation has the maximum value $(d\sigma/d\Omega)_{max}$. This is the value measured experimentally. The relationship between the total cross section, $(\sigma)_{total}$, and the differential cross section, $(d\sigma/d\Omega)_{max}$, for the case of isotropic scattering is:¹³

$$(\sigma)_{\text{total}} = \frac{8\pi}{3} \left(\frac{d\sigma}{d\Omega}\right)_{\text{max}}$$
 (43)

where $(\sigma)_{\text{total}}$ is the $(Q_{a,J_a} \rightarrow c,J_c)$ of Equation (42). Hence, the polarized $(d\sigma/d\Omega)$ is given by:

$$\left(\frac{d\sigma}{d\Omega}\right)_{\parallel}^{S} = k_{S}^{4} \frac{1}{g_{a}} \sum_{m_{a}} \sum_{m_{c}} \left| (C_{\sigma\sigma})_{a,J_{a},m_{a};c,J_{c},m_{c}} \right|^{2}$$
(44)

where the subscript s on $(d\sigma/d\Omega)^S$ indicates the cross section for the scattered (Stokes) radiation.

Analysis of the form of $\chi^{(3)}$ which is appropriate for Raman scattering shows that for a,J_a \rightarrow c,J_c resonance:

$$x^{(3)}(\omega_{p}, -\omega_{p}, \omega_{s}) = \frac{-1}{6h^{3}} \sum_{a,c} \sum_{m_{a}, m_{c}} \rho_{aa}^{(0)} | \sum_{b} \mu_{ab} \mu_{bc} A_{ab} |^{2} \times -\frac{1}{11}$$
(45)

where
$$A_{ab} = \frac{1}{\omega_{ab} + \omega_{p}} + \frac{1}{\omega_{ab} - \omega_{s}}$$
 (46)

and Γ is the half-width at half-maximum corresponding to the a,J $_a$ \rightarrow c,J $_c$ resonance. Note that

$$\omega_{ab} = -\omega_{ba}$$

and wbc = wbc + wac, or wbc = wba - wRaman

so that $-\omega_{ab} = \omega_{bc} + \omega_{Raman}$

and $w_{ab} - w_{s} = -w_{bc} - w_{p}$.

Rewriting Equation (46) using the last relation

$$A_{ab} = -\left[\frac{1}{\omega_{ba} - \omega_{p}} + \frac{1}{\omega_{bc} + \omega_{p}}\right]$$

Therefore,

$$\chi^{(3)}(\omega_{p}, -\omega_{p}, \omega_{s}) = \frac{-i}{6h\Gamma} \sum_{a,c} \sum_{m_{a}} \sum_{m_{c}} \rho_{aa}^{(0)} | (C_{c\sigma})_{a,J_{a},m_{a};c,J_{c},m_{c}} |^{2}$$
(47)

The expression for $\rho_{aa}^{(0)}$ is independent of m_a and is given by

$$\rho_{aa}^{(0)} = \frac{1}{Q} \exp \left[-E_a/kT\right]$$

$$= \frac{1}{g_a} \qquad f_a \qquad (48)$$

where Q is the rotational partition function for molecules of the Raman medium. Thus,

$$\chi^{(3)}(\omega_{p}, -\omega_{p}, \omega_{s}) = \frac{-i}{6\hbar\Gamma} \sum_{a} f_{a} \frac{1}{g_{a}} \sum_{m_{a}} \sum_{m_{c}} |(C_{\sigma\sigma})_{a}, J_{a}, m_{a}; c, J_{c}, m_{c}|^{2}$$

$$= \frac{-i}{6\hbar\Gamma} \sum_{a} f_{a} \frac{1}{k_{s}} \left(\frac{d\sigma}{d\Omega}\right)_{\parallel}^{s}$$
(49)

For vibrational Raman scattering, the final state is essentially empty. Thus the summations over v_a and v_c reduce to a particular initial state $(v_a=0,J_a=J)$

$$\chi^{(3)}(\omega_{p}, -\omega_{p}, \omega_{s}) = \frac{-1}{6\Omega\Gamma} f_{J} \left[\frac{1}{k_{s}^{4}} \left(\frac{d\sigma}{d\Omega} \right)_{\parallel}^{s} \right]$$
 (50)

Since $x^{SRS} = Im \left[x^{(3)}(\omega_p, -\omega_p, \omega_s)_{\Delta\omega=0}\right],$

$$\chi^{SRS} = \frac{-1}{6} \left(\frac{1}{h\Gamma} \right) \left[\frac{1}{k_s^4} + \left(\frac{d\sigma}{d\Omega} \right)_{\parallel}^{S} \right] f_J$$
 (51)

The quantities in expression (51) are defined in CGS units. By multiplying (51) by $(4\pi\epsilon_0)^2$ and expressing all quantities in MKS units, χ^{SRS} is obtained also in MKS units.

In order to relate χ^{SRS} of Equation (51) to other third-order susceptibilities, the $\chi^{(3)}$ formula given in Table 1 has been analyzed. The results are summarized in Table 9. Since the cross section is proportional to the fourth power of the Stokes wave vector, the peak values of $\chi^{(3)}$ (i.e. $\Delta\omega=0$) are nearly independent of frequency for radiation in the IR and visible regions. Thus, Raman scattering data obtained at a certain visible wavelength can be used to compute the peak values of $\chi^{(3)}$ for all of the third-order processes associated with the type II scheme.

3.3.3 Type III Scheme

The type III resonance enhancement scheme utilizes three-photon resonance via vibrational-rotational and vibronic intermediate states. A detailed study of the $\chi^{(3)}$ formula indicates that an exact calculation requires vibronic transition moments and Franck-Condon amplitudes for each of the excited electronic states coupled to the ground electronic state by electric dipole transitions. An extensive literature search provided only a small fraction of the necessary parameters for HC ℓ and DF. Because of this lack of data, various approximations were considered in order to derive formulas that can be evaluated numerically with the existing data.

TABLE 9. TYPE II NONLINEAR SUSCEPTIBILITY

•
$$x^{(3)} = \text{Re}[x^{(3)}] + i \text{Im}[x^{(3)}]$$

• Re
$$[\chi^{(3)}] = Im [\chi^{(3)}]_{\Delta\omega=0} \times \left[\frac{\Delta\omega\Gamma}{\Delta\omega^2+\Gamma^2}\right]$$

•
$$\operatorname{Im}\left[\chi^{(3)}\right] = \operatorname{Im}\left[\chi^{(3)}\right]_{\Delta\omega=0} \times \left[\frac{\Gamma^2}{\Delta\omega^2 + \Gamma^2}\right]$$

$$\bullet \quad \Delta \omega \equiv \omega_{R} \quad - \quad (\omega + \omega')$$

•
$$\operatorname{Im}\left[\chi^{(3)}\right]_{\Delta\omega=0} = \frac{A}{6} \left[\frac{(4\pi\epsilon_0)^2}{h\Gamma}\right] \left[k^{-4}\left(\frac{d\sigma}{d\Omega}\right)_{ij}\right] f_{ij}$$

THG:
$$3\omega \rightarrow \omega_{\varsigma}$$
 3

SFG:
$$2\omega + \omega' \rightarrow \omega_s$$

$$\omega + \omega' + \omega'' \rightarrow \omega_c$$
 1

SRS at
$$\omega$$
, ω'

 Γ : Two-Photon Resonance Linewidth (HWHM)

$$\left(\frac{d\sigma}{d\Omega}\right)_{ij}$$
: Polarized Differential Raman Scattering Cross Section

The calculation of $\chi^{(3)}$ for candidate molecules in the type III resonance enhancement scheme involves three different kinds of pairs of the intermediate states $|c\rangle$ and $|d\rangle$: The two intermediate states may both be pure vibrational-rotational; one intermediate state may be pure vibrational-rotational and the other intermediate state may be vibronic, or both intermediate states may be vibronic. Pairs of intermediate states of the first kind have already been encountered in the calculation of $\chi^{(3)}$ for candidate molecules in the type I resonance enhancement scheme. Accordingly, the treatment of the contributions from pairs of intermediate state of the first kind has been discussed during the analysis of the type I resonance enhancement scheme and will not be repeated here. Parts of the intermediate states of the third kind lead to terms which are small because of the square of the electronic energy occurring in the denominator of these terms. Thus, pairs of intermediate states of the second kind will be considered in detail in the following discussion.

The third-order susceptibility for the type III resonance enhancement may be approximated as

$$\chi_{III}^{(3)} \cong \frac{-1}{h^3} \sum_{a} \rho_{aa}^{(0)} \sum_{bc} \frac{\mu_{ab} \mu_{bc}}{\omega_{ab} + \omega_3 + i \Gamma_{ab}} \frac{1}{\omega_{ac} + \omega_2 + \omega_3} \sum_{d} \frac{\mu_{cd} \mu_{da}}{\omega_{ad} + \omega_3}$$
 (52)

Consider the special case of three-photon resonance at v_a =0, J_a =J and v_b =2, J_b =J+1 (0-2 R(J) transition)

$$\chi_{\text{III,res}}^{(3)} = \frac{-1}{h^3} \rho_{aa}^{(0)} \frac{\mu_{02}}{\omega_{02} + \omega_3 + i\Gamma_{02}} \sum_{c} \int_{d}^{\mu_{2c}} \frac{\mu_{2c} \mu_{cd} \mu_{d0}}{(\omega_{0c} + \omega_2 + \omega_3)(\omega_{0d} + \omega_3)}$$
(53)

The summations over the intermediate states $|c\rangle$ and $|d\rangle$ must now be examined in the case where one of the two intermediate states is a vibronic state. Let "e" stand for a set of vibronic levels and "I" stand for the summations over the intermediate states.

$$I = \sum_{d} \sum_{e} \frac{\mu_{2e} \mu_{ed} \mu_{d0}}{(\omega_{0e} + \omega_{2} + \omega_{3})(\omega_{0d} + \omega_{3})} + \sum_{e} \sum_{e} \frac{\mu_{2e} \mu_{ed} \mu_{e0}}{(\omega_{0e} + \omega_{2} + \omega_{3})(\omega_{0e} + \omega_{3})} = I_{1} + I_{2}$$
 (54)

where $|\omega_{0e}|$ is the electronic transition frequency, assumed to be much greater than any of the input frequencies. Analyzing the two terms in Equation (54) separately,

$$I_{1} = \sum_{e} \left\{ \frac{\mu_{2e} \mu_{e0} \mu_{00} \mu_{00}}{(\omega_{0e} + \omega_{2} + \omega_{3})(\omega_{00} + \omega_{3})} + \frac{\mu_{2e} \mu_{e1} \mu_{1} \mu_{0}}{(\omega_{0e} + \omega_{2} + \omega_{3})(\omega_{01} + \omega_{3})} + \frac{\mu_{2e} \mu_{e2} \mu_{2} \mu_{2} \mu_{0}}{(\omega_{0e} + \omega_{2} + \omega_{3})(\omega_{02} + \omega_{3})} \right\}$$

$$(55)$$

$$I_{2} = \sum_{e} \left\{ \frac{\mu_{20'} \mu_{0'} e^{\mu_{e0}}}{(\omega_{00'} + \omega_{2} + \omega_{3})(\omega_{0e} + \omega_{3})} + \frac{\mu_{21'} \mu_{1'} e^{\mu_{e0}}}{(\omega_{01'} + \omega_{2} + \omega_{3})(\omega_{0e} + \omega_{3})} + \frac{\mu_{22'} \mu_{2'} e^{\mu_{e0}}}{(\omega_{02'} + \omega_{2} + \omega_{3})(\omega_{0e} + \omega_{3})} \right\}$$

$$+ \frac{\mu_{22'} \mu_{2'} e^{\mu_{e0}}}{(\omega_{02'} + \omega_{2} + \omega_{3})(\omega_{0e} + \omega_{3})}$$
(56)

where the primes indicate summation over rotational states.

Note that $|\omega_{0e}| \gg \omega$. This fact leads to the approximations $\omega_{0e}^{+} \omega_{2}^{+} \omega_{3}^{=} \omega_{0e}$ and $\omega_{0e}^{+} \omega_{3}^{=} \omega_{0e}^{-}$ which, when applied to Equations (54)-(56) yields

$$I = \sum_{e} \left[\frac{1}{\omega_{0e}} \left\{ \frac{\frac{1}{\omega_{0e}} + \frac{1}{\omega_{0e}} + \frac{\frac{1}{\omega_{0e}} + \frac{1}{\omega_{0e}} + \frac{\frac{1}{\omega_{0e}} + \frac{1}{\omega_{0e}} + \frac{1}{\omega_{0e}} + \frac{1}{\omega_{0e}} + \frac{1}{\omega_{0e}} + \frac{\frac{1}{\omega_{0e}} + \frac{1}{\omega_{0e}} + \frac{1}{\omega_{0e}} + \frac{1}{\omega_{0e}} + \frac{\frac{1}{\omega_{0e}} + \frac{1}{\omega_{0e}} + \frac{1}{\omega_{0e$$

Next, the summation over vibronic intermediate states is carried out assuming that the quantity ω_{0e} may be energy averaged over the vibrational levels of the electronic state to yield the quantity Ω_e which is independent of the vibrational quantum numbers, v_a . Making this second approximation,

$$I \approx \sum_{e} \frac{-1}{\omega_{e}} \sum_{J_{e}} \sum_{V_{e}} \left\{ \frac{\mu_{2e} \mu_{e0} \mu_{0}' 0}{\omega_{00}' + \omega} + \frac{\mu_{22}' \mu_{2}' e \mu_{e0}}{\omega_{02}' + 2\omega} + \frac{\mu_{2e} \mu_{e1}' \mu_{1}' 0}{\omega_{01}' + \omega} + \frac{\mu_{21}' \mu_{1}' e \mu_{e0}}{\omega_{01}' + 2\omega} + \frac{\mu_{20}' \mu_{0}' e \mu_{e0}}{\omega_{00}' + 2\omega} \right\}$$

$$+ \frac{\mu_{21}' \mu_{1}' e \mu_{e0}}{\omega_{01}' + 2\omega} + \frac{\mu_{2e} \mu_{e2}' \mu_{2}' 0}{\omega_{02}' + \omega} + \frac{\mu_{20}' \mu_{0}' e \mu_{e0}}{\omega_{00}' + 2\omega} \right\}$$

$$(58)$$

where J_e and v_e are the rotational and vibrational quantum numbers of states in the excited electronic level manifold. The above approximation allows a simplification of the summation over vibrational levels of the electronic state. Note that the products of the matrix elements in Equation (58) have the general form $\mu_{2e} \mu_{ev}' \mu_{v'0}$ or $\mu_{2v}' \mu_{v'e} \mu_{e0}$. Thus, separating the rotational and vibrational parts of each matrix element, these two products can be explicitly written as

$$\mu_{2e} \mu_{ev'} \mu_{v'0} = \langle g, 2 | \mu | e, v_e \rangle \langle e, v_e | \mu | g, v' \rangle \langle g, v' | \mu | g, 0 \rangle R_1$$
 (59)

$$\mu_{2v'} \mu_{v'e} \mu_{e0} = \langle g, 2 | \mu | g, v' \rangle \langle g, v' | \mu | e, v_e \rangle \langle e, v_e | \mu | g, 0 \rangle R_2$$
 (60)

where \mathbf{R}_1 and \mathbf{R}_2 represent the appropriate product of rotational integrals. Both terms are of the form

$$\langle g, v'' | \mu | g, v' \rangle \langle g, v' | \mu | e, v_e \rangle \langle e, v_e | \mu | g, v \rangle R$$
 (61)

The summation over $|e,v_e\rangle$ can thus be evaluated using the completeness property of the vibrational states in the manifold of the excited electronic state.

The product of the second and third factors in Equation (61) is performed first. The electronic part of the matrix element must be integrated. It is assumed that the individual matrix elements can be written 14 as

$$\langle g, v' | \mu | e, v_e \rangle = \langle v' | \mu_{ge} | v_e \rangle$$

$$\langle e, v_e | \mu | g, v \rangle = \langle v_e | \mu_{ge} | v \rangle$$
(62)

where $\mu_{ge} = \mu_{eg}^{+}$ is the dipole moment operator for the nuclear coordinates. The nuclear dipole moment operator can be expressed as a Taylor series expansion about the equilibrium internuclear separation, r_e : 14

$$\mu_{ge}(r) = \mu_{ge}(re) + \frac{\partial \mu_{ge}}{\partial r} \Big|_{r_e} (r-r_e) + \frac{1}{2} \frac{\partial^2 \mu_{ge}}{\partial r^2} \Big|_{r_e} (r-r_e)^2 + \dots$$
 (63)

Using the completeness property yields

$$\sum_{\mathbf{v}_{e}} \langle \mathbf{v}' | \mu_{ge} | \mathbf{v}_{e} \rangle \langle \mathbf{v}_{e} | \mu_{eg} | \mathbf{v} \rangle = \langle \mathbf{v}' | \mu_{ge} \mu_{eg} | \mathbf{v} \rangle$$
 (64)

Noting that $|\mu_{qe}|$ is real, the operator in Equation (64) may be reexpressed as

$$|\mu_{ge}|^2 = \mu_{ge} \mu_{eg} = D_{ge}^{(0)} + D_{ge}^{(1)} \times D_{ge}^{(2)} \times D_{ge}^{(3)} \times D_{ge$$

where x is the displacement of the atoms from their equilibrium positions (i.e. $x = r - r_e$) and the $D_{ge}^{(b)}$ are all real coefficients. These coefficients are related to certain derivatives of (63) according to:

$$D_{ge}^{(0)} = |M_{ge}^{(0)}|^2$$
 (66)

$$D_{ge}^{(1)} = M_{ge}^{(0)} M_{ge}^{(1)^*} + M_{ge}^{(0)^*} M_{ge}^{(1)}$$
(67)

$$D_{ge}^{(2)} = M_{ge}^{(0)} M_{ge}^{(2)^{*}} + |M_{ge}^{(1)}|^{2} + M_{ge}^{(0)^{*}} M_{ge}^{(2)}$$
 (68)

where

$$M_{ge}^{(k)} \equiv \frac{\partial^{(k)} \mu_{ge}}{\partial r^{(k)}} \Big|_{r_e}$$
 (69)

The remaining integral in Equations (64) and (65) is of the form

$$A_{v'}^{(k)} = \langle v' | x^k | v \rangle \tag{70}$$

where $|v'\rangle$ and $|v\rangle$ are assumed to be normalized eigenfunctions of an anharmonic oscillator. Thus, Equations (59) and (60) can be evaluated according to:

$$\sum_{\mathbf{v_e}} \mu_{2e} \mu_{ev'} \mu_{v'0} = \sum_{k=0}^{2} D_{ge}^{(k)} A_{2,v'}^{(k)} \sum_{\ell=0}^{2} M_{gg}^{(\ell)} A_{v'0}^{(\ell)} R_1$$
 (71)

$$\sum_{\mathbf{v}_{e}} \mu_{2\mathbf{v}'} \mu_{\mathbf{v}'e} \mu_{e0} = \sum_{\ell=0}^{2} \eta_{gg}^{(\ell)} A_{2,\mathbf{v}'}^{(\ell)} \sum_{k=0}^{2} D_{ge}^{(k)} A_{\mathbf{v}'0}^{(k)} R_{2}$$
 (72)

Since the frequency denominators do not depend on J_e , the summations over rotational states are carried out first. Summation over J' must be performed explicitly using actual energy levels. Summation over m states can be performed by factoring the rotational part of the μ_{02} matrix element into R_1 and R_2 . This procedure yields precisely the function ϕ_R defined by Equation (23).

3.4 $\chi^{(3)}$ Calculation Results

The $\chi^{(3)}$ calculations for the three resonance enhancement schemes have been performed using the line selected CO laser frequencies corresponding to P(9), P(10), P(11), and P(12) transitions in the $[6 \rightarrow 5]$, $[5 \rightarrow 4]$, and $[4 \rightarrow 3]$ vibrational manifold. In addition, survey calculations have been carried out for each molecular species in order to determine the pump frequencies for which the nonlinear susceptibility is optimized. Nonlinear susceptibility values have been computed in CGS units; conversion to MKS units is obtained by multiplying the CGS value by a factor of 1.235 x 10^{-25} .

The following sections summarize the results of the calculations for each resonance enhancement scheme.

3.4.1 Type I Scheme

The candidate molecules studied for the type I scheme are ${\rm CO}^{18}$, NO, DC 35,37 , and DBr 79,81 . The spectroscopic constants, transition dipole moments, and linewidth data references for each molecule are listed in Table 10.

Molecule	Spectroscopic Constants	Transition Dipole Moments	Linewidth
co ¹⁸	[15]	[16]	[17]
NO	[18]	[19]	[20]
DCL 35	[21]	[22]	[23]
DBr ⁷⁹	[24]	[25]	[26]

TABLE 10. TYPE I SCHEME MOLECULAR PARAMETER REFERENCES

The spectroscopic constants for DCL 37 were calculated from the DCL 35 parameters using the isotope effect relations. 27 The same procedure was used to obtain the constants for DBr 81 and DBr 79 . The transition moments and linewidths for the isotopes were assumed to be the same.

The results of the $\chi^{(3)}$ code calculations using the line selected CO laser frequencies are listed in Tables 11 through 16. The tables indicate that χ^{THG} and χ^{SFG} values are in the range of 10^{-38} to 10^{-36} cm⁶/erg for CO¹⁸ and DCL^{35,37}, while the nonlinear susceptibilities of NO and DBr^{79,81} are on the order of 10^{-38} cm⁶/erg and 10^{-40} cm⁶/erg, respectively.

TABLE 11. TYPE I $\chi^{(3)}$ CALCULATION RESULTS

	MOLECUI	MOLECULE: [CO10]		
S in	P(9)	P(10)	P(11)	P(12)
w + w + w	1.79×10^{-37}	1.43×10^{-37}	1.22×10^{-37}	1.14×10^{-37}
q + m + en	2.40×10^{-37}	1.91×10^{-37}	1.62×10^{-37}	1.46×10^{-37}
3 + m + m	2.26 x 10 ⁻³⁸	$1.94 \times 10^{-38}(1)$	1.64×10^{-38}	1.46×10^{-38}
q _m + q _m + q _m	3.38 x 10 ⁻³⁸	1.10 × 10 ⁻³⁸	$\dot{4.41} \times 10^{-39}$	1.09×10^{-38}
e m + q m + q m	1.83×10^{-37}	1.59 × 10 ⁻³⁷	1.41×10^{-37}	1.29×10^{-37}
2 m + q m + q n	2.64 x 10 ⁻³⁸	$1.91 \times 10^{-38}(1)$	1.70 × 10 ⁻³⁸	2.34×10^{-38}
0n + 0n + 0n	2.35 x 10 ⁻³⁹	$1.05 \times 10^{-38}(1)$	4.55×10^{-39}	4.22×10^{-39}
e + ω + ω	3.12 x 10 ⁻³⁸	$3.10 \times 10^{-38}(1)$	2.64 × 10 ⁻³⁸	2.54×10^{-38}
q	2.94 x 10 ⁻³⁸	$2.15 \times 10^{-38}(1)$	1.68 × 10 ⁻³⁸	2.34×10^{-38}
m + m + m	1.19×10^{-37}	$9.56 \times 10^{-38}(1)$	8.37×10^{-38}	8.47×10^{-38}

 $[\]omega_a = [4-3]; \omega_b = [5-4]; \omega_c = [6-5]$ (1) = One-Photon Resonance; (3) = Three-Photon Resonance

TABLE 12. TYPE I $\times^{(3)}$ CALCULATION RESULTS

MOLECULE: [${\sf N0}^{16}$]

		ומרביסרבי ר ייי ד		
Sm	(6)d	P(10)	P(11)	P(12)
w + m + m	1.09 × 10 ⁻³⁹	1.18 × 10 ⁻³⁹	1.29 × 10 ⁻³⁹	1.40×10^{-39}
q + m + m	1.32 × 10 ⁻³⁹	1.45×10^{-39}	1.56×10^{-39}	1.73×10^{-39}
3 + m + m	1.69 x 10 ⁻³⁹	1.87×10^{-39}	2.08×10^{-39}	2.34×10^{-39}
q _{ω + q_m + q_m}	1.92 x 10 ⁻³⁹	2.16 × 10 ⁻³⁹	2.31×10^{-39}	2.59 × 10 ⁻³⁹
em + qm + qm	1.59 x 10 ⁻³⁹	1.77 × 10 ⁻³⁹	1.90×10^{-39}	2.12 × 10 ⁻³⁹
² ω + α + α φ	2.46 x 10 ⁻³⁹	2.77 × 10 ⁻³⁹	3.05×10^{-39}	3.48×10^{-39}
3 m + 2 m + 2 m	3.90 x 10 ⁻³⁹	4.41 × 10 ⁻³⁹	5.23 × 10 ⁻³⁹	6.17×10^{-39}
e	2.59×10^{-33}	2.90 × 10 ⁻³⁹	3.33 × 10 ⁻³⁹	3.84×10^{-39}

 $w_a = [4-3]; w_b = [5-4]; w_c = [6-5]$ (1) = One-Photon Resonance; (3) = Three-Photon Resonance

TABLE 13. TYPE I $\times^{(3)}$ CALCULATION RESULTS

MOLECULE: [$DC \mu^{35}$]

	MOLECU	MULECULE: [DC#]		
s S	P(9)	P(10)	P(11)	P(12)
υ + υ + υ ο + υ + υ	1.25 x 10 ⁻³⁸	6.17 × 10 ⁻³⁸	6.38 × 10 ⁻³⁸	1.52 x 10 ⁻³⁷
w + m + m	5.37 x 10 ⁻³⁸	7.15 × 10 ⁻³⁸	3.36×10^{-37}	6.82 x 10 ⁻³⁸
3 + m + m	5.51×10^{-37}	$1.41 \times 10^{-37}(3)$	1.46 × 10 ⁻³⁸	2.07×10^{-37}
q _m + q _m + q _m	8.21 × 10 ⁻³⁸	4.90 × 10 ⁻³⁸	2.94×10^{-39}	$1.31 \times 10^{-37}(2)$
em + qm + qm	2.19×10^{-37}	$2.31 \times 10^{-37}(3)$	6.08 × 10 ⁻⁴⁰	$1.05 \times 10^{-37}(2)$
³ π + ⁴ π + ⁴ π	7.99 × 10 ⁻³⁹	$1.69 \times 10^{-38}(2)$	4.04×10^{-39}	$2.48 \times 10^{-38}(2)$
ິກ + ິກ + ິກ	3.09 × 10 ⁻³⁹	3.54×10^{-39}	6.63 × 10 ⁻⁴⁰	1.92×10^{-39}
e	2.63 x 10 ⁻³⁸	3.63×10^{-38}	2.01 × 10 ⁻³⁹	6.22 x 10 ⁻³⁸
q _m + _m + _m	1.48 × 10 ⁻³⁸	8.25 × 10 ⁻³⁹ (2)	1.92 × 10 ⁻³⁹	$6.01 \times 10^{-39}(3)$
a^{+} a^{+} a^{+}	3.40 × 10 ⁻³⁸	$3.66 \times 10^{-38}(2)$	1.07 × 10 ⁻³⁹	5.05 × 10 ⁻³⁸

 $w_a = [4-3]; w_b = [5-4]; w_c = [6-5]$ (1) = One-Photon Resonance; (3) = Three-Photon Resonance

TABLE 14. TYPE I $x^{(3)}$ CALCULAȚION RESULTS

MOLECULE: { $0c_{\kappa}^{37}$ }

	MOLECUL	MOLECULE: DCx2'		
S	p(9)	P(10)	P(11)	P(12)
a + a + a	4.99 x 10 ⁻⁴⁰	1.31 × 10 ⁻³⁸	5.38 × 10 ⁻³⁸	4.18 × 10 ⁻³⁸
qa + a + a	1.98 × 10 ⁻³⁸	3.30×10^{-37}	7.01 × 10 ⁻³⁸	5.91 × 10 ⁻³⁸
3 + a + a	5.92 × 10 ⁻³⁹	1.17×10^{-37}	5.09 × 10 ⁻³⁸	1.38 × 10 ⁻³⁸
qm + qm + qm	2.20 × 10 ⁻³⁸	3.65 × 10 ⁻³⁸	1.90 × 10 ⁻³⁸	3.69 × 10 ⁻³⁹
en + an + an	1.47×10^{-38}	4.55×10^{-38}	3.75×10^{-38}	3.82 × 10 ⁻³⁸
om + qm + qm	1.86 × 10 ⁻³⁸	8.92×10^{-39}	9.07×10^{-39}	4.02×10^{-39}
3 + 3 + 3 m	3.57×10^{-39}	2.17×10^{-39}	5.89 x 10 ⁻⁴⁰	$1.80 \times 10^{-39}(2)$
e + 2	7.02 × 10 ⁻³⁸	1.39 x 10 ⁻³⁸	1.85 × 10 ⁻³⁸	$2.47 \times 10^{-39}(2)$
q + 2 + 2 m	6.64×10^{-39}	5.94×10^{-39}	4.46×10^{-39}	$3.25 \times 10^{-39}(2)$
$w_a + w_b + w_c$	2.64 x 10 ⁻³⁸	7.91 × 10 ⁻³⁹	1.65 × 10 ⁻³⁸	2.39 × 10 ⁻³⁹

 $\omega_a = [4-3]; \omega_b = [5-4]; \omega_c = [6-5]$ (1) = One-Photon Resonance; (3) = Three-Photon Resonance

TABLE 15. TYPE I $x^{(3)}$ CALCULATION RESULTS

MOLECULE: [DBr⁷⁹]

a S	P(9)	P(10)	P(11)	P(12)
**************************************	2.70 × 10 ⁻⁴¹	2.90×10^{-41}	3.11×10^{-41}	3.36 × 10 ⁻⁴¹
q _m + m + m	3.19 × 10 ⁻⁴ 1	3.43×10^{-41}	3.71×10^{-41}	4.03 × 10 ⁻⁴¹
3 + m + m	4.04×10^{-41}	4.39 x 10 ⁻⁴¹	4.80×10^{-41}	5.24×10^{-41}
q _m + q _m + q _m	4.39 x 10 ⁻⁴¹	4.77×10^{-41}	5.22×10^{-41}	5.74×10^{-41}
em + m + m	3.74×10^{-41}	4.06×10^{-41}	4.41×10^{-41}	4.82 x 10 ⁻⁴¹
3 m + m + q m	5.51 x 10 ⁻⁴¹	6.05×10^{-41}	6.67×10^{-41}	7.37×10^{-41}
3 + 3 + 3 a	8.57×10^{-41}	9.50 x 10 ⁻⁴¹	1.06×10^{-41}	1.18 × 10 ⁻⁴⁰
e + a + a	5.94 x 10 ⁻⁴¹	6.53 x 10 ⁻⁴¹	7.23 x 10 ⁻⁴¹	7.96 x 10 ⁻⁴¹
9m + 3m + 3m	6.89 x 10 ⁻⁴¹	7.61 × 10 ⁻⁴¹	8.47 x 10 ⁻⁴¹	9.36 x 10 ⁻⁴¹
2 + a + a c	4.72×10^{-41}	5.16×10^{-41}	5.67 × 10 ⁻⁴¹	6.23×10^{-41}
		T		

 $w_a = [4-3]; w_b = [5-4]; w_c = [6-5]$ (1) = One-Photon Resonance; (3) = Three-Photon Resonance

TABLE 16. TYPE I $\chi^{(3)}$ CALCULATION RESULTS

MOLECULE: [DBr⁸¹]

	MOLECU	MULECULE: UBr]	;	
S	P(9)	P(10)	P(11)	P(12)
w + w + w	2.68 × 10 ⁻⁴ 1	2.87 × 10 ⁻⁴¹	3.08 × 10 ⁻⁴¹	3.32 × 10 ⁻⁴¹
a + m + m	3.15 x 10 ⁻⁴¹	$3.40 \times 10^{-41}(1)$	3.67×10^{-41}	3.98 × 10 ⁻⁴¹
0 + m + m	3.40×10^{-41}	4.31 × 10 ⁻⁴¹	4.71×10^{-41}	5.12 × 10 ⁻⁴ 1
α _p + α _p + α _p	4.34 × 10 ⁻⁴ 1	$4.72 \times 10^{-41}(1)$	5.15×10^{-41}	5.66 × 10 ⁻⁴¹
e p + q p + q m	3.70×10^{-41}	$4.01 \times 10^{-41}(1)$	4.35×10^{-41}	4.76 × 10 ⁻⁴¹
o + o + o e	5.39×10^{-41}	$5.93 \times 10^{-41}(1)$	6.54×10^{-41}	7.19 x 10 ⁻⁴¹
3 + 3 + 3	8.20 × 10 ⁻⁴¹	9.18 × 10 ⁻⁴¹	1.02×10^{-40}	1.12 × 10 ⁻⁴⁰
8 + 3 + 3 8 + 3	5.75 x 10 ⁻⁴¹	6.36 × 10 ⁻⁴¹	7.01×10^{-41}	7.68 × 10 ⁻⁴¹
. q a + 3a + 3a	6.67×10^{-41}	7.41 × 10 ⁻⁴¹	8.20 × 10 ⁻⁴¹	9.03 × 10 ⁻⁴¹
om + qm + em	4.63 x 10 ⁻⁴ 1	5.07 × 10 ⁻⁴¹	5.56 × 10 ⁻⁴¹	6.08 × 10 ⁻⁴¹

 $w_a = [4-3]; w_b = [5-4]; w_c = [6-5]$ (1) = One-Photon Resonance; (3) = Three-Photon Resonance

An analysis of the molecular energy levels shows that the pump frequencies are moderately close to one, two, and three-photon resonances. However, numerous destructive interference effects cancel some of the resonance enhancement terms in the nonlinear susceptibility. Consequently, the values of χ^{THG} and χ^{SFG} fluctuate by as much as an order of magnitude within a small range of pump frequencies. This behavior is evident in the results of the calculations for each of the molecules. As an example, Figure 3 shows the calculated value of χ^{THG} for CO.

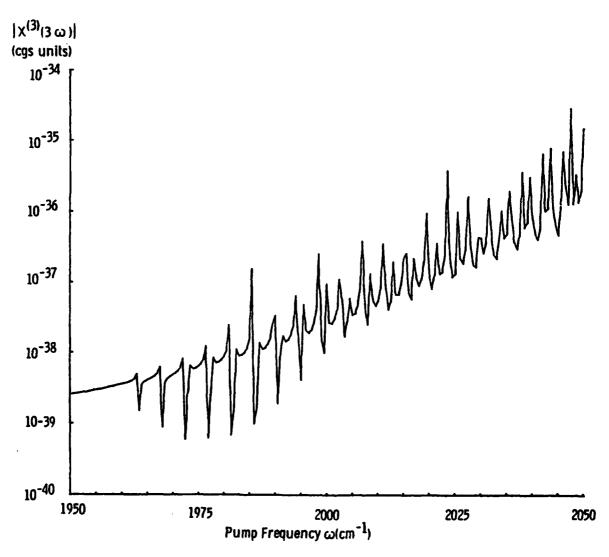


FIGURE 3. NONLINEAR SUSCEPTIBILITY OF CO¹⁸ FOR THIRD HARMONIC GENERATION

A conversion efficiency estimate based on a χ^{THG} value of 10^{-34} cm⁶/erg with N = 10^{20} cm⁻³, I = 500 MW/cm², and L = 300 cm shows that nearly 20% efficiency is feasible if phase-matching can be maintained over the interaction length during the entire pulse length. From this analysis, $\chi^{(3)}$ values on the order of 10^{-36} cm⁶/erg suggest efficiencies on the order of 2 x 10^{-5} . The small conversion efficiencies are the direct result of the small values of the nonlinear susceptibilities.

The survey calculations of χ^{THG} were carried out to find the largest two- and three-photon resonance enhancement in each of the type I scheme molecules. Using the optimum pump frequency ranges given in Table 3 as a guide, several known CO laser frequencies were chosen to closely match two- or three-photon resonances in DCL, DBr, and NO. The CO laser frequencies did not match the optimum pump frequency ranges of CO^{18} . Table 17 lists the results of the survey calculations. The χ^{THG} values in the table show significant enhancement for NO and DBr. This suggests that the choice of CO laser output frequencies to match the optimum pump frequency range and the resonances is an important factor in the overall efficiency.

TABLE 17. TYPE I THG SURVEY CALCULATION

CO Laser	Frequency	_x (3) (THG) in cm ⁶ /erg
ω(cm ⁻¹)	Transition	Molecule	X(3)
1838.49	P(24) [9-8]	NO	1.41 × 10 ⁻³⁵
1859.80	P(19) [9-8]	NO	1.28×10^{-35}
1846.87	P(16) [10-9]	NO	1.45 x 10 ⁻³⁵
2016.871	P(12) [4-3]	DCe 35	1.52 x 10 ⁻³⁷
2003.154	P(9) [5-4]	DCL 35	0.82×10^{-37}
1991.014	P(12) [5-4]	DC4 37	0.42 x 10 ⁻³⁷
1808.35	P(13) [12-11]	DBr ⁷⁹	1.1 × 10 ⁻³⁷
1809.41	P(19) [11-10]	DBr ⁷⁹	2.1 x 10 ⁻³⁷
1805.29	P(20) [11-10]	DBr ⁸¹	2.1 x 10 ⁻³⁶
1809.10	P(25) [10-9]	DBr ⁸¹	4.6×10^{-37}

3.4.2 Type II Scheme

The references used for the molecular parameters are listed in Table 18. Differential Raman cross section data for HD are not available; however, the similarity of its electronic structure to that of $\rm H_2$ implies a similar value of $\rm d\sigma/d\Omega$ for both HD and $\rm H_2$. Thus, $\rm d\sigma/d\Omega$ values for HD may be scaled from $\rm H_2$ data using the $\rm k^4$ dependence of Raman cross section.

TABLE	18.	TYPE	ΙI	SCHEME	MOLECULAR	PARAMETER	REFERENCES

Molecule	Spectroscopic Constants	$\left(\frac{d\sigma}{d\Omega}\right)_{II}$ and k	Linewidth
н ₂	[29]	[30]	[31]
HD	[29]	calculated from[30]	[32]
HF	[33]	[34]	[35]

The Raman cross sections for the 0 and S branches of $\rm H_2$ and HD were calculated from the depolarization ratio 36 and the scattering strength dependence on the rotational quantum number. 37 The ratios of the polarized S and O branch differential scattering cross sections to that of the Q branch were found to be given by the following relations:

$$\frac{(d\sigma/d\Omega)_{|||}^{S(J)}}{(d\sigma/d\Omega)_{|||}^{Q(J)}} = \frac{2(J+2)(2J-1)}{J(2J+1)} \rho_{\ell}^{Q}(J)$$
 (73)

$$\frac{(d\sigma/d\Omega)_{|J|}^{O(J)}}{(d\sigma/d\Omega)_{|J|}^{O(J)}} = \frac{2(J-1)(2J+3)}{(J+1)(2J+1)} \rho_{L}^{O}(J)$$
(74)

where $\rho_{\lambda}^{\,\,Q}(J)$ is the Q branch depolarization ratio for linearly polarized incident light.

Experimentally measured values of ρ for H_2 give cross section ratios on the order of 10^{-2} for both S and O branches. This implies that $\chi^{(3)}$ values are inherently smaller for the S and O branch resonances than those of the Q branch resonance enhancement. This property is indicated in the results of the χ^{THG} calculations given in Table 19.

TABLE 19. TYPE II THG SURVEY CALCULATION
(T = 300 K, P = 1 Atm)

CO Laser Freq	uency	x ⁽³⁾	Two-Photon Resonance Molecule
Transition	ω (cm ⁻¹)	(cm ⁶ /erg)	Branch (J)
P(19) [12-11]	1784.33	2.0 x 10 ⁻³⁸	H ₂ : 0(2)
P(23) [5-4]	1943.99	1.1 x 10 ⁻³⁷	HD: S(0)
P(11) [7-6]	1943.52	1.2 x 10 ⁻³⁷	HD: S(0)
P(10) [4-3]*	2025.07	4.0×10^{-38}	HD: S(1)
P(11) [12-11]	1815.81	1.7 x 10 ⁻³⁶	HD: Q(0)
P(18) [11-10]	1813.50	1.3 x 10 ⁻³⁶	HD: Q(1)
P(19) [11-10]	1809,09	6.6×10^{-37}	HD: Q(2)
P(20) [11-10]	1805.29	2.2×10^{-37}	HD: Q(3)
P(26) [10-9]	1804.76	1.3 x 10 ⁻³⁶	HD: Q(3)
P(14) [12-11]	1804.28	2.4×10^{-36}	HD: Q(3)
P(9) [6-5]*	1977.264	2.4 x 10 ⁻³⁹	HF: Q(3)
P(10) [6-5]*	1973.285	2.7 x 10 ⁻³⁹	HF: Q(4)
P(11) [6-5]*	1969.274	8.8 x 10 ⁻⁴⁰	HF: Q(5)

^{*} Line selected CO laser frequency

The only line selected CO laser frequency which approaches a two-photon resonance in HD is the P(10) [4-3] transition. However, since the frequency detuning is approximately 1 cm $^{-1}$ from the S branch resonance χ^{THG} is relatively small. The other lines selected pump frequencies yield smaller χ^{THG} values in HD due to off-resonance conditions. In contrast to HD and H $_2$, some of the pump frequencies are close to the Q-branch resonances in HF. However, small χ^{THG} values are calculated based on the large linewidth data. Therefore the above results suggest that Q-branch resonances in HD should be considered for optimum $\chi^{\left(3\right)}$ resonance enhancement.

3.4.3 Type III Scheme

The molecular parameter references for HCL and DF are listed in Table 20.

TABLE 20. TYPE III SCHEME MOLECULAR PARAMETER REFERENCES

Molecule	Spectroscopic Constants	Transition Dipole Moment	Linewidth
HCL	[38]	[22]	[23]
DF	[39]	[40]	[41]

The results of the χ^{THG} and χ^{SFG} calculations for the line selected CO laser frequencies are summarized in Tables 21 and 22 for HCL and DF, respectively. The values listed in Tables 21 and 22 are in the range of 0.8 to 1.5 x 10^{-38} cm⁶/erg for most of the pump frequency combinations. Based on the conversion efficiency estimate of Section 3.4.1, the type III susceptibilities are predicted to have relatively small efficiencies.

TABLE 21. TYPE III $x^{(3)}$ CALCULATION RESULTS

MOLECULE: [HC135]

•	MOLECUI	MULECULE: [nci]		
S	P(9)	P(10)	P(11)	P(12)
m + m + m	7.64 × 10 ⁻³⁹	7.96 × 10 ⁻³⁹	8.30 × 10 ⁻³⁹	8.65 x 10 ⁻³⁹
ma + m + mp	8.36 × 10 ⁻³⁹	8.71×10^{-39}	9.08 × 10 ⁻³⁹	9.48 × 10 ⁻³⁹
3 + 8 + 8 8 - 8 - 8	9.19 x 10 ⁻³⁹	9.59 × 10 ⁻³⁹	1.00 × 10 ⁻³⁸	1.05 × 10 ⁻³⁸
q _m + q _m + q _m	9.97 x 10 ⁻³⁹	1.04×10^{-38}	1.09 × 10 ⁻³⁸	1.14 × 10 ⁻³⁸
em + qm + qm	9.14×10^{-39}	9.53 × 10 ⁻³⁹	9.94×10^{-39}	1.04 × 10 ⁻³⁸
2 m + m + m m m c	1.10×10^{-38}	1.15×10^{-38}	1.20×10^{-38}	1.25 × 10 ⁻³⁸
3 m + 3 m + 3 m	1.33 × 10 ⁻³⁸	1.39 x 10 ⁻³⁸	1.46 × 10 ⁻³⁸	1.53 × 10 ⁻³⁸
e	1.11 × 10 ⁻³⁸	1.16 × 10 ⁻³⁸	1.21×10^{-38}	1.27 × 10 ⁻³⁸
q _m + 3 _m + 3 _m	1.21 × 10 ⁻³⁸	1.26×10^{-38}	1.32 × 10 ⁻³⁸	1.39 × 10 ⁻³⁸
m + m + m	1.00×10^{-38}	1.05 × 10 ⁻³⁸	1.10 × 10 ⁻³⁸	1.15 × 10 ⁻³⁸

TABLE 22. TYPE III $\chi^{(3)}$ CALCULATION RESULTS

MOLECULE: [DF

	MOLECULE: [ר ה ז		
Sm	P(9)	P(10)	P(11)	P(12)
m + m + m	3.64 x 10 ⁻³⁹	3.75 × 10 ⁻³⁹	3.86 × 10 ⁻³⁹	3.98 x 10 ⁻³⁹
q _m + m + e _m	3.88 x 10 ⁻³⁹	4.00×10^{-39}	4.13 x 10 ⁻³⁹	4.26 x 10 ⁻³⁹
3 + m + m	4.16 x 10 ⁻³⁹	4.30×10^{-39}	4.44×10^{-39}	4.60 × 10 ⁻³⁹
q _m + q _m + q _m	4.43 x 10 ⁻³⁹	4.58×10^{-39}	$4.7\dot{4} \times 10^{-39}$	4.91 x 10 ⁻³⁹
m + m + m	4.14 x 10 ⁻³⁹	4.28 × 10 ⁻³⁹	4.42×10^{-39}	4.57×10^{-39}
o + o + o o	4.77 × 10 ⁻³⁹	4.95×10^{-39}	5.14 × 10 ⁻³⁹	5.34 x 10 ⁻³⁹
3 + 3 + 3 m	5.61 x 10 ⁻³⁹	5.85×10^{-39}	6.11×10^{-39}	6.41×10^{-39}
e	4.82 x 10 ⁻³⁹	5.00×10^{-39}	5.19 x 10 ⁻³⁹	5.41×10^{-39}
q m + 2 m + 2 m	5.17 x 10 ⁻³⁹	5.37 × 10 ⁻³⁹	5.59×10^{-39}	5.84×10^{-39}
2 m + m + m	4.46 × 10 ⁻³⁹	4.61×10^{-39}	4.78×10^{-39}	4.95 × 10 ⁻³⁹

 ω_a = [4-3]; ω_b = [5-4]; ω_c = [6-5] (1) = One-Photon Resonance; (2) = Two-Photon Resonance

4.0 EFFICIENCY LIMITATION AND PHASE-MATCHING ANALYSIS

Efficiency limitations in THG and SFG generally arise from the breaking of phase-matching and the competing processes. Breaking of phase-matching can occur through various causes. These include population transfer due to one-and two-photon absorption and intensity dependent refractive index variation caused by quadratic Kerr effect. These time-dependent processes may ultimately limit pulse lengths. Examples of competing processes are stimulated vibrational Raman scattering of the pump fields. Another limitation is imposed by gas breakdown at very high power and energy densities. This section examines the importance of the different efficiency limiting processes. The quantitative analysis yields optimum operating parameters for efficient frequency up-conversion.

The breaking of phase-matching limits conversion efficiency because of reduced effective interaction length for nonlinear coherent processes. For a process involving an interaction length L and a wave vector mismatch Δk , the allowed phase mismatch is given by: ⁴²

$$\Delta kL \leq \pi$$
 (75)

The breaking of phase-matching refers to a condition that violates the above requirement. Since a nonlinear medium is usually chosen to satisfy the phase-matching condition initially, the breaking of phase-matching may arise from dynamic wave vector mismatches caused by refractive index variations in the medium during the conversion process. In the general case of SFG, the phase variation is expressed by:

$$\delta \left[\Delta k L \right] = \frac{1}{c} \left[\omega_{s} \delta n(\omega_{s}) - \omega_{p} \delta n(\omega_{p}) - \omega_{q} \delta n(\omega_{q}) - \omega_{r} \delta n(\omega_{r}) \right] L \tag{76}$$

where $\delta n(\omega_j)$ is the refractive index variation at ω_j . For the special case of THG, the above expression simplifies to:

$$\delta[\Delta kL] = \frac{3\omega}{c} [\delta n(3\omega) - \delta n(\omega)] L \qquad (77)$$

In the following sections various linear and nonlinear processes which are responsible for the refractive index variation and the competing effects are discussed in terms of specific efficiency limiting mechanisms.

4.1 Linear Processes

The important linear processes are single-photon absorption at the pump and the generated frequencies, population transfer effects, and thermal defocusing. Since the latter two effects are consequences of pump absorption in the medium, it is essential to choose molecular species which minimize the pump absorption. Therefore, infrared absorption bands of the candidate molecules provide crucial parameters for the assessment of linear efficiency limiting processes.

4.1.1 Absorption Coefficient and Refractive Index at Pump Frequencies

Single-photon absorption of the pump radiation arises from the fundamental transitions in the IR-active molecules. These transitions also determine the refractive indices at frequencies close to them. Both the absorption coefficient and refractive index as a function of pump frequency can be evaluated from the first-order (linear) susceptibility per molecule which is given by 7

$$\chi^{(1)}(\omega) = -\frac{1}{h} \sum_{a,b} \rho_{aa} |\mu_{ab}|^2 \left[\frac{1}{\omega_{ab} + \omega + i\Gamma_{ab}} + \frac{1}{\omega_{ab} - \omega - i\Gamma_{ab}} \right]$$
(78)

The symbols have their ususal meanings as used previously in the third-order susceptibility formula. The numerical values of $\chi^{(1)}$ were obtained from the same molecular spectroscopic constants and transition moment data as were used in the calculation of $\chi^{(3)}$ values.

To obtain the numerical values for the absorption coefficient $\alpha(\omega)$ and the refractive index $n(\omega)$, the following relations were used:

$$\alpha(\omega) = \frac{\omega \eta}{n(\omega)} \quad \text{Im} \left[N \chi^{(1)}(\omega) \right]$$
 (79)

$$n(\omega) = \left[1 + \text{Re}\left[N_{\chi}^{(1)}(\omega)\right]\right]^{\frac{1}{2}}$$
 (80)

In molecular gases, the real part of $N\chi^{(1)}$ is generally much smaller than unity. Thus, a good approximation of $n(\omega)$ is given by:

$$n(\omega) - 1 \simeq \frac{1}{2} \operatorname{Re} [N_{\chi}^{(1)}(\omega)]$$
 (81)

A computer code for $\chi^{(1)}$ has been developed, and a program listing is given in Appendix B.

The results of the $\alpha(\omega)$ and $n(\omega)-1$ calculations at STP conditions are plotted in Figures 4 through 6 for the candidate molecules DCL, DBr, and NO, respectively.

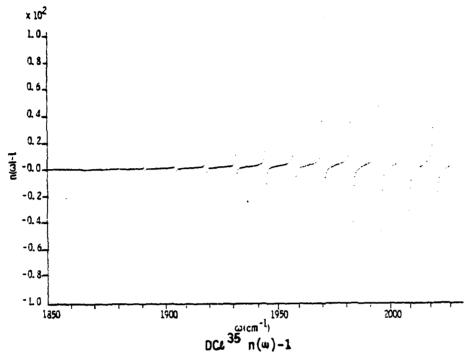


FIGURE 4(a). DCL REFRACTIVE INDEX VS FREQUENCY

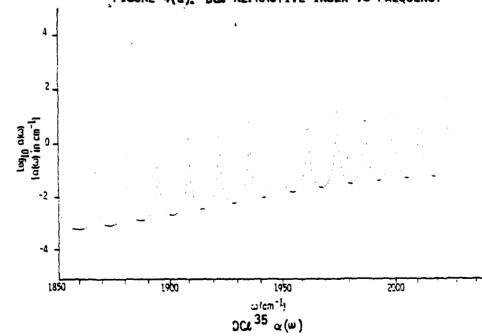


FIGURE 4(b). DC& ABSORPTION COEFFICIENT VS FREQUENCY

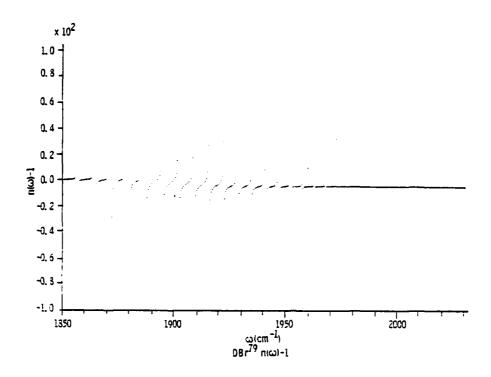


FIGURE 5(a). DBr REFRACTIVE INDEX VS FREQUENCY

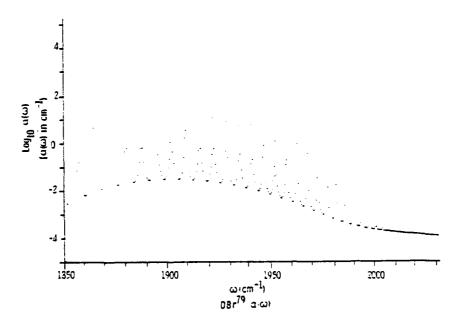


FIGURE 5(b). DBr ABSORPTION COEFFICIENT VS FREQUENCY

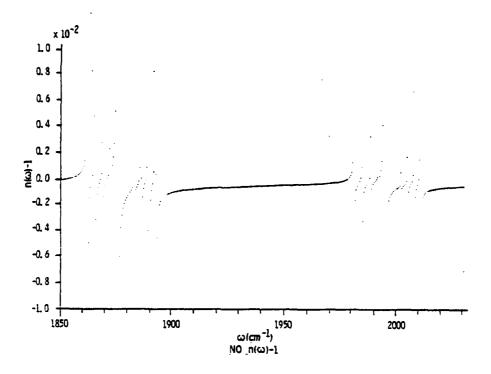


FIGURE 6(a). NO REFRACTIVE INDEX VS FREQUENCY

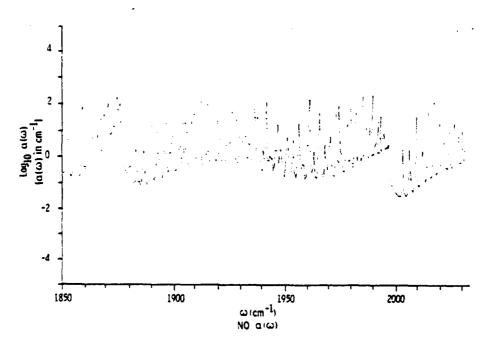


FIGURE 6(b), NO ABSORPTION COEFFICIENT VS FREQUENCY

When significant absorption is present at ω and 3ω , the electric field equations governing THG can be cast in the following form:

$$\frac{dE_3}{dz} = \beta E_1^3 - \frac{1}{2} \alpha_3 E_3 \qquad (82a)$$

$$\frac{dE_1}{dz} = \beta E_1^2 - \frac{1}{2} \alpha_1 E_1$$
 (82b)

If pump depletion and phase mismatches are considered to be negligible, the generated field amplitude, $E_3(L)$, is given by

$$E_3(L) = \beta (E_1(0))^3 \frac{2}{3\alpha_1 - \alpha_3} \left(e^{-\alpha_3 L/2} - e^{-3\alpha_1 L/2} \right)$$
 (83)

In the case of strong pump attenuation ($\alpha_1 L \gg 1$) and $\alpha_3 = 0$, the above expression states that the effective interaction length is $(3\alpha_1/2)^{-1}$ which is much less than L. However, if attenuation is small ($\alpha_1 L \ll 1$), an approximate solution for $E_3(L)$ is:

$$E_3(L) \simeq \beta (E_1(0))^3 L (1 - 3\alpha_1 L/4)$$
 (84)

Thus, small attenuation does not significantly reduce the THG efficiency if dynamic phase mismatches are negligible.

4.1.2 Absorption Coefficient and Refractive Index at the Generated Frequencies

Although the generated frequencies are far from the fundamental IR transition bands, they nearly coincide with the overtone transitions in some of the candidate molecules. The calculation of $\alpha(\omega)$ and $n(\omega)-1$ is straightforward using the $\chi^{(1)}$ computer code. Figures 7 and 8 show the results of the calculations for the first overtone bands of DF and HCL, respectively.

The second overtone bands of the type I scheme molecules are also close to the generated frequencies and are important in the resonance enhancement of $\chi^{(3)}$; however, single-photon absorption at the generated frequencies is exceedingly small (typically $\alpha < 10^{-5}$ cm⁻¹). Therefore, a model discussed in the previous section, in which $\alpha_3 = 0$ was assumed, is a realistic description of the type I scheme.

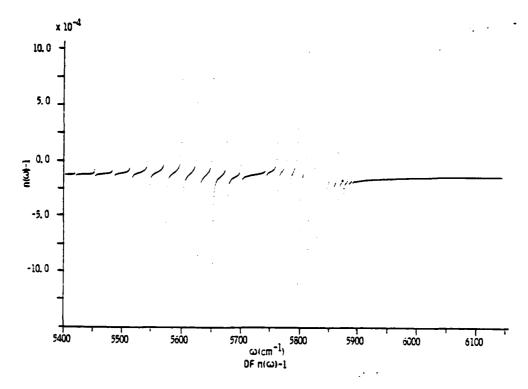


FIGURE 7(a). DF REFRACTIVE INDEX VS FREQUENCY

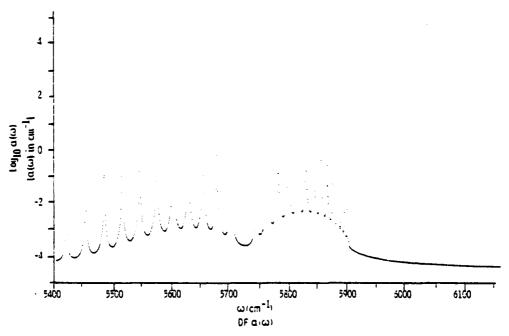


FIGURE 7(b). DF ABSORPTION COEFFICIENT VS FREQUENCY

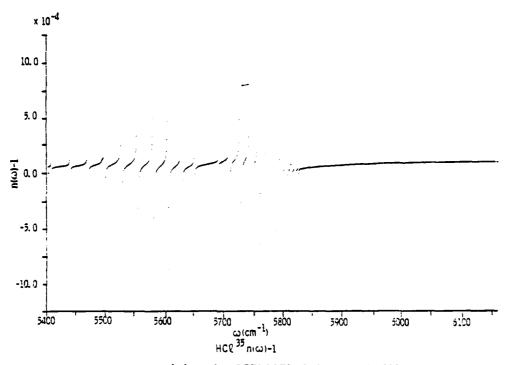


FIGURE 8(a). HC2 REFRACTIVE INDEX VS FREQUENCY

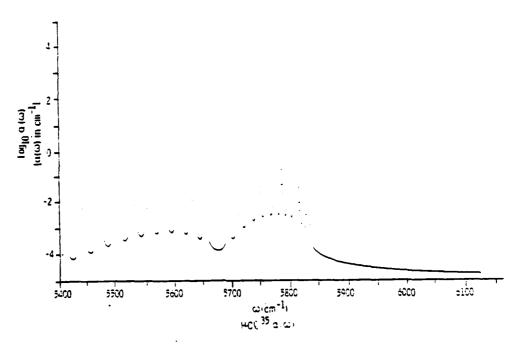


FIGURE 8(b). HC& ABSORPTION COEFFICIENT VS FREQUENCY

In contrast to the type I scheme, absorption in the type III scheme is significant only at the generated frequencies. By setting $\alpha_1 = 0$ in Equation (83), the generated field amplitude becomes

$$E_3(L) = \frac{2\beta}{\alpha_3} (E_1(0))^3 (1 - e^{-\alpha_3 L/2})$$
 (85)

In the strong attenuation limit $(\alpha_3 L \gg 1)$, the effective interaction length becomes $(\alpha_3/2)^{-1}$. On the other hand, if $\alpha_3 L \ll 1$, $E_3(L)$ is proportional to $(E_1(0))^3$ and L. From these properties, it is evident that a small attenuation of the generated field is desirable and that the attenuation only slightly reduces the conversion efficiency. These conclusions together with those of the previous section are valid only to the extent in which dynamic phase mismatches can be neglected. It will be shown in the next section, however, that the breaking of the phase-matching condition due to absorption is much more sensitive and critical than pump attenuation in the IR-active candidate molecules.

4.1.3 Population Transfer and Dynamic Phase Mismatch

Whenever ground state molecules absorb pump radiation, a certain fraction of the population is transferred to the first excited vibrational level. Since the fundamental IR transitions determine the refractive indices at the pump frequencies, population transfer perturbs the refractive indices at the pump frequencies. This immediately leads to phase variation through expressions (76) and (77).

Because population transfer is time-dependent, the resulting phase variation is a dynamic process. Although this dynamic phase mismatch can be calculated in principle, such a calculation would require an estimate of population transfer based on the radiative and kinetic properties of the gas, which are beyond the scope of this work. Therefore, a quasi-steady state model was considered for the purpose of illustrating the effects of the dynamic phase mismatch. The basic assumption of this model is that the rotational states of the first excited vibrational state are in thermal equilibrium at the gas temperature. The excited vibrational state population as a whole is considered to be time-dependent in order to allow for pulse length effects and pump intensity fluctuations.

The refractive index variation calculations using the $\chi^{(1)}$ code were accomplished by specifying a certain relative population transfer value (Δ N/N). For example, in the case of DC2 with (Δ N/N) = 10^{-3} at STP, different pump frequencies yielded wave vector mismatches from 3.2 x 10^{-4} to 6.5 x 10^{-2} cm⁻¹. These values are typical of the type I scheme molecules. For a practical device having an interaction length of 300 cm, the corresponding phase variations are 9.6 x 10^{-2} to 19.5 radians, thereby indicating that breaking of phase-matching is a serious effect for some pump frequencies and significant for many others. If (Δ N/N) = 10^{-2} is assumed, most of the pump frequencies would experience severe phase mismatches. This means that population transfer values of as little as 0.1% can lead to significant efficiency reduction and that 1% transfer levels are beyond the tolerance range. Conversely, efficient frequency conversion can be maintained only over a time interval during which population transfer can be held to less than 0.1%.

An estimate for the allowable pulse duration ΔT can be obtained from the following relation:

$$\frac{\Delta N}{N} = \frac{\alpha I \Delta T}{N h \omega} \tag{86}$$

where I is the pump intensity and α is the absorption coefficient. For most of the type I scheme molecules α/N is typically in the range of 10^{-23} cm² (off-resonance) to 10^{-19} cm² at the peaks of absorption lines. Using the lower limit, the maximum value of ΔT for I = 0.5 GW/cm² is found to be 8 x 10^{-9} second if $(\Delta N/N)$ is restricted to 10^{-3} . Therefore, at the pump intensities of interest for high conversion efficiencies, the pulse lengths are limited to the nanosecond time scale.

4.1.4 Thermal Defocusing

The population transfer may cause thermal defocusing which is a manifestation of refractive index variation across the beam for a nonuniform pump beam cross section. In the case of a gaussian beam profile with an initial beam radius, w_0 , the beam radius changes by a factor of two when the refractive index on the beam axis varies by an amount given by: 42

$$\delta n = w_0^2 / 2L^2 \tag{87}$$

where L is the interaction length. If w_0 is taken to be the waist such that $w_0^2 = \lambda b/2\pi$ (b = confocal parameter), then the condition (87) becomes:

$$\delta n = \lambda b/4\pi L^2 \tag{88}$$

For the case of confocal focusing (b = L), the numerical value of δn is 1.3×10^{-7} for L = 300 cm. From the results of the previous section, $(\Delta N/N) = 10^{-3}$ in DC2 yields δn values in the range of 2.5 x 10^{-8} to 5.2 x 10^{-6} . This clearly shows that thermal defocusing has a serious effect on the efficiency due to reduced pump intensities in the nonlinear medium. However, it is also important to note that for large beam cross sections and/or uniform intensity profiles, thermal defocusing effects can be minimized.

4.2 Nonlinear Processes

A number of third-order processes besides THG and SFG may be present at high pump intensities. These include quadratic Kerr effect, two-photon absorption, and stimulated Raman scattering. Other nonlinear processes such as three-photon absorption, gas breakdown, and pump depletion may also affect conversion efficiencies. Quantitative assessment of each of these intensity-dependent processes is discussed in the following sections.

4.2.1 Two-Photon Absorption

In the type I and II resonance enhancement schemes, small two-photon detunings are used to obtain large $\chi^{(3)}$ values. Because of such near resonances, the probability of two-photon absorption (TPA) can be very significant. As in the single-photon absorption case, two-photon absorption can reduce conversion efficiency due to pump attenuation, dynamic phase mismatch, and thermal defocusing. Thus, it is clear that a compromise between large $\chi^{(3)}$ enhancement and two-photon absorption should be considered.

For relatively small TPA, the attenuation parameter, $a^{(2)}L$, is defined by $a^{(2)}L = 1 - I_D(L)/I_D(0)$ (89)

 where

$$\chi_{\mathbf{p}}^{\mathsf{TPA}}(\omega_{\mathbf{p}}) = \mathsf{Im} \chi_{\mathbf{p}}^{(3)}(\omega_{\mathbf{p}}, -\omega_{\mathbf{p}}, \omega_{\mathbf{p}}) \tag{90b}$$

If photons of unequal frequencies cause TPA, the induced absorption at $\boldsymbol{\omega}$ is characterized by:

$$a^{(2)}L = 3 \omega_p \eta^2 \sum_{j} [NL I_j(0)][x_p^{TPA} (\omega_j)]$$
 (91a)

where

$$\chi_{p}^{TPA}(\omega_{j}) = \operatorname{Im} \chi_{p}^{(3)}(\omega_{p}, -\omega_{j}, \omega_{j}) \text{ for } j \neq p$$
 (91b)

A numerical estimate for a $^{(2)}L$ at typical operating conditions can be obtained by assuming $\omega_p=3.772\times 10^{14}~\text{rad/sec}$ (i.e., 2000 cm $^{-1}$), N = $10^{26}~\text{m}^{-3}$, L = 1 m, and I $_p(0)=5\times 10^{12}~\text{W/m}^2$. A representative value for (two-photon resonant) $_{\chi}^{TPA}$ is $10^{-34}~\text{cm}^6/\text{erg}$ which is equivalent to $1.235\times 10^{-59}~\text{MKS}$. With these parameters, a $^{(2)}L$ is equal to 0.498, or nearly half of the pump radiation is absorbed. Therefore, two-photon absorption is a significant efficiency limiting process if $_{\chi}^{TPA}$ values are on the order of $10^{-34}~\text{cm}^6/\text{erg}$. For the CO laser frequencies, calculations show that $_{\chi}^{TPA}$ values approach this magnitude only in the type II scheme.

4.2.2 Quadratic Kerr Effect

Another process intimately related to TPA is quadratic Kerr effect which causes intensity dependent refractive index variations through the real part of $\chi_p^{(3)}(\omega_p,-\omega_p,\omega_p)$. The principal effect of this process involves phase shifts along the direction of propagation, which can cause breaking of phase-matching. For a nonuniform beam intensity, the refractive index variations also lead to beam divergence (Kerr defocusing). However, since beam uniformity can be controlled to a certain extent, the Kerr phase shifts are inherently more important.

The definition of the Kerr phase shift at the pump frequency is given by

$$(\Delta kL)_{Kerr} = \frac{3}{4} \omega_p \eta^2 [NL I_p][\chi_p^{Kerr} (\omega_p)]$$
 (92a)

where

$$\chi_{p}^{\text{Kerr}}(\omega_{p}) = \text{Re } \chi_{p}^{(3)}(\omega_{p}, -\omega_{p}, \omega_{p})$$
 (92b)

In the presence of other pump frequencies, the Kerr phase shift at $\boldsymbol{\omega}_{i}$ is defined by

$$(\Delta kL)_{Kerr} = \frac{3}{2} \omega_i \eta^2 \sum_{j} [NL I_j] [\chi_i^{Kerr} (\omega_j)]$$
 (93a)

where

$$\chi_{i}^{\text{Kerr}}(\omega_{j}) = \text{Re } \chi^{(3)}(\omega_{i}, -\omega_{j}, \omega_{j}) \quad i \neq j$$
 (93b)

The above expression also describes the Kerr phase shift at the generated frequencies, ω_s , when ω_s is substituted for ω_i . In the case of SFG, all phase shifts due to various frequency combinations must be summed using (93a, b).

Since the quadratic Kerr effect vanishes (aside from small nonresonant contributions) at the exact two-photon resonance, the Kerr phase shifts can be made negligible, in principle, by an appropriate choice of pump frequencies. However, for CO frequency tripling, the two-photon detunings are generally nonzero. Thus, considerable phase shifts may be encountered. For example, if the operating conditions for the TPA calculation in the previous section are assumed and if the value of the Kerr nonlinearity at the pump frequency is assumed to be 5 x 10 $^{-35}$ cm 6 /erg (i.e., peak of x $^{\rm Kerr}$ when x $^{\rm TPA}$ = 10 $^{-34}$ cm 6 /erg on resonance), the resulting phase shift is 0.125 radian. While this shift is smaller than π , the predicted phase-matched efficiency is only 4.7% (neglecting pump attenuation) if the magnitude of x $^{\rm THG}$ were equal to x $^{\rm Kerr}$. This suggests that a large ratio of $|x|^{\rm THG}|/|x|^{\rm Kerr}|$ is desirable in order to maximize the THG efficiency without the Kerr induced phase mismatches.

In the type I resonance enhancement scheme, χ Kerr can be calculated with the $\chi^{(3)}$ code. For the line selected CO laser frequencies $|\chi_p^{\text{Kerr}}(\omega_p)|$ values are typically two orders of magnitude larger than $|\chi^{\text{THG}}|$. In contrast $|\chi_s^{\text{Kerr}}(\omega_p)|$ values are an order of magnitude smaller than $|\chi^{\text{THG}}|$. These observations indicate that the Kerr induced phase mismatches at the pump frequencies are likely to limit the THG efficiencies in the type I scheme.

The role of the Kerr induced phase mismatches in the type II scheme is important due to the fact that all the third order processes are related through a common two-photon resonance enhancement. For example, if the detuning is large with respect to the linewidth, $|\chi^{\text{Kerr}}|$ is equal to $|\chi^{\text{THG}}|/3$. On the other hand, at

exact two-photon resonance ($\Delta\omega=0$), χ^{Kerr} vanishes and χ^{THG} is equal to $3\times\chi^{TPA}$. At intermediate detunings, both the Kerr phase shift and TPA pump attenuation must be considered together. Such a treatment has shown that high efficiencies are possible with phase shifts close to $\pi/2$ while holding TPA losses to about 20%. Although the $\chi^{(3)}$ calculations for the type II scheme indicate phase shifts much smaller than $\pi/2$ at the CO laser pump frequencies due to relatively large detunings, analysis shows that if a near two-photon resonance can be achieved on a Raman-active Q-branch transition, the desired phase shifts are feasible. This point will be discussed further in connection with multiline SFG in HD.

In the type III resonance enhancement scheme, quadratic Kerr effect at the pump and the generated frequencies can be expected to be small. This is one of the advantageous features of the scheme when it was considered initially. A further analysis has shown that the Kerr effect introduces a level shift⁴⁴ of the three-photon resonance according to

$$\delta \omega \sim -\frac{|\mu|^2 \eta I_p}{h^2 \Omega} \tag{94}$$

where Ω is the vibronic transition frequency and μ is the associated matrix between the vibronic state and the v=2 level of the ground electronic state. In principle, all such transitions must be included in calculating the level shift, but approximation based on a single strong transition yields an order of magnitude estimate of 10^{-2} cm⁻¹ at the typical operating conditions. Since this is a small shift relative to the transition linewidth, resonance enhancement is not affected appreciably. Also, the Kerr induced phase mismatch can be estimated using the following relations:

$$(\Delta kL)_{Kerr} = \frac{3\omega_p \Delta nL}{n}$$
 (95a)

with
$$\Delta n \sim -\frac{N|\mu_{20}|^2 \delta \omega}{h(\Delta \omega)^2}$$
 (95b)

where μ_{20} represents the first overtone transition matrix element and $\Delta\omega$ is the detuning which is assumed to be large compared to the linewidth. Substituting representative parameters of the type III molecules into the above expressions yields a phase shift of 0.03 radian if $\delta\omega = 10^{-2}$ cm⁻¹ and $\Delta\omega = 1$ cm⁻¹ (1.886 x 10^{11} rad/sec) are used. Thus, breaking of the phase-matching condition due to quadratic Kerr effect is not believed to be a serious limitation in the type III scheme.

4.2.3 Stimulated Raman Scattering

Stimulated Raman scattering (SRS) in molecular gases may involve vibrational and/or rotational Raman transitions. In the vibrational SRS process IR frequencies up-converted via THG or SFG become the "pump" radiation. In the rotational SRS process, both the pump and the up-converted radiation can act as source terms for amplifying the respective Stokes radiation. In either SRS processes, the THG and SFG efficiencies will be limited through a competition of frequency conversion processes.

A key parameter, which indicates when the SRS processes become important, is the stimulated Raman gain coefficient ${\bf g}_{\rm s}$. This parameter is defined by: 45

$$g_{s} = \frac{4 \Delta N \lambda_{s}^{2}}{\gamma_{R}} \left(\frac{I_{p}}{h\omega_{p}}\right) \left(\frac{d\sigma}{d\Omega}\right)^{p}_{\parallel}$$
(96)

where

AN = population density difference

 λ_c = Stokes radiation wavelength

 y_p = Raman transition linewidth (FWHM) in rad/sec

I_p = pump intensity

ພ_ກ = pump frequency in rad/sec

 $\left(\frac{d\sigma}{d\Omega}\right)^{p}_{\parallel}$ = differential Raman scattering cross section for the pump radiation

The empirical values of the various parameters are generally available, but the cross section data are usually measured for the Stokes raidation in the visible region, 30,34 These data can be scaled to the IR frequencies by making use of the ω_s^4 dependence of $(d\sigma/d\omega)^S$ and the relationship

$$\left(\frac{d\sigma}{d\Omega}\right)_{||}^{p} = \left(\frac{d\sigma}{d\omega}\right)_{||}^{s} \left(\frac{\omega_{p}}{\omega_{s}}\right) \tag{97}$$

Substituting the expression (97) into (96), one obtains

$$g_{s} = \frac{16 \pi^{2} \Delta N c^{2} \omega_{s}}{h \gamma_{R}} \left[\omega_{s}^{-4} \left(\frac{d\sigma}{d\Omega} \right)_{\parallel}^{s} \right] I_{p}$$
 (98)

where the quantity inside the brackets is nearly invariant at Stokes frequencies in the visible and IR regions. Thus, by evaluating the invariant quantity from visible Raman scattering data, Raman gain coefficients can be calculated for the IR region. Table 23 lists the results of the calculations based on a ΔN value of 1 amagat (2.69 x $10^{25}~\text{m}^{-3}$) for the vibrational SRS gain at an intensity of 1 GW/cm² ($10^{13}~\text{W/m}^2$). In these calculations the pump frequency is assumed to be 6000 cm²l. Since not all cross section data were available, $g_{\rm S}$ estimates for the deuterated molecules (i.e., HD, DC2, DBr, and DF) were scaled from those of the normal species by the ratio of the Stokes frequencies.

The threshold gain for Raman oscillation is usually considered to be $g_SL=30$. For practical device lengths, the g_S values in Table 23 indicate that vibrational SRS oscillation can be regarded as a small effect in all the molecules except for H_2 . The hydrogen gas is a special case in which g_S increases with higher pressures (up to 20 amagats). For example, at 8 amagats, the linewidth is the same as that at 1 amagat, g_S thereby increasing the g_S value by a factor of 8.

Another effect of vibrational SRS is Raman amplification of the pump radiation by the generated radiation. By amplifying the pump radiation the generated radiation transfers the up-converted power back into the pump radiation. This process acts as a stabilizing mechanism to establish a steady-state efficiency condition. An analysis of this THG/SRS interaction shows that a characteristic parameter is given by:⁴³

$$\kappa = \left| \frac{\chi^{\text{THG}}}{6\chi^{\text{SRS}}} \right|^2 \left[1 + \left(\frac{\Delta w}{Y_R} \right)^2 \right]$$
 (99)

When the value of κ is close to or larger than unity, the SRS process is not important; efficiency will be limited by other processes. However, if $\kappa \ll 1$, then the efficiency limit is equal to the value of κ . For the type I scheme molecules, $\chi^{(3)}$ code calculations yield χ^{SRS} values which are an order of magnitude smaller than χ^{THG} . This indicates that vibrational Raman amplification in the type I scheme is not a significant limiting process. In contrast, $\kappa = 0.25$ on resonance ($\Delta \omega = 0$) in the type II scheme, which suggests that vibrational Raman amplification is an important factor governing the maximum THG efficiency.

TABLE 23, VIBRATIONAL RAMAN GAIN COEFFICIENTS

ain	$g_{\rm S}({\rm m}^{-1})$	0.37	0.15	1.7	0.53	0.077	2.8	1.0	0.13	0.67	2.1	
IR SRS Gain	$\omega_{\rm S} ({\rm cm}^{-1})$	3855	4123	3442	3114	2038	1845	2372	3096	3909	4161	
Raman Data (λ _p = 488.0 nm) @ STP	γ_{R} (cm ⁻¹)	0.0877	0.057	0.13	0.248	0.5	0.014	0.05	0.466	0.248	0.13	
	$\omega_{R}(cm^{-1})$	2145	1877	2558	2886	3962	4155	3628.2	2904	2091	1839	
	(do/du) <mark>s</mark> (cm ²)	3.3×10^{-31}	8.9×10^{-32}	2.3×10^{-30}	1.4×10^{-30}	4.9×10^{-31}	5.3×10^{-31}	•	1	ı	ı	
	$_{\rm s}$ (cm ⁻¹)	18346.8	18614.8	17933.8	17605.8	16529.8	16336.8	ı	ı	ı	ı	
Molecule	[Transition]	[6]	[0]	[6]	[0]	[6]	[(1)]	[(1)]	[6]	[0]	[6]	
	[Tran	8	Q	HBr	3 2	生	H ₂	웊	DF	DC¢	DBr	

Rotational Raman scattering is a third-order process that does not share any of the resonance enhancement paths used in the THG and SFG processes. As such, the rotational SRS process represents a potential competing loss mechanism for the pump and the generated radiation. As in the vibrational SRS case, a key parameter in the rotational SRS is the Raman gain coefficient. Expression (98) is still a valid formula for calculating $\mathbf{g}_{\mathbf{S}}$, but ΔN must be defined in terms of an actual population difference because of much smaller Raman shifts in the rotational case. A formula for ΔN as a function of the rotational quantum number of the initial state is given by

$$\Delta N_{J} = N(f_{J} - f_{J+2}) \tag{100}$$

where

N = total number density

 f_1 = fraction of molecules in the initial state

 $f_{,l+2}$ = fraction of molecules in the final state

Under equilibrium conditions at a temperature T, the population distribution can be expressed by:

$$f_{J'} = \frac{2 J' + 1}{Q} e^{-E(J')/kT}$$
 (101)

where

Q \simeq kT/hc B_o (rotational partition function)

and

$$E(J') \simeq hc B_0 J' (J'+1)$$

It is evident from the above formulas that population differences become smaller with smaller values of B_0 . For example, $J=6 \rightarrow J=8$ S(6) transition in CO at room temperature has a calculated value of $\Delta N_{J=6}/N=1.41 \times 10^{-3}$. Since the rotational Raman cross sections are roughly comparable to the vibrational Raman cross sections, 30 the g_s values for the rotational SRS are smaller than the vibrational Raman gains by the $\Delta N_i/N$ ratio. A survey of the candidate molecules shows that only H_2 has sufficiently large rotational Raman shifts to make $\Delta N_i/N$ ratios close to those of the vibrational Raman shifts.

Recent experimental demonstrations 46,47 of rotational SRS in H₂ (S₀(0)) using CO₂ laser radiation indicate that rotational Raman shifting can be a very

efficient IR frequency conversion process. Based on the information given in these experiments, the rotational Raman gain coefficient is predicted to be in the range of 11 to 20 m⁻¹ at a CO laser pump (single-line) intensity of 1 GW/cm². The predicted value of g_s implies efficient rotational Raman shifting for interaction lengths in excess of 3 m. Furthermore, the H_2 ($S_0(1)$) transition may also be important at room temperature with a g_s value comparable to that of the $S_0(0)$ transition.

Although $\rm H_2$ presents a potentially serious efficiency limitation due to rotational SRS, other type II molecules (HD and HF) appear to have a lesser problem. This is because of smaller ΔN values and larger Raman linewidths in HD and HF compared to that of $\rm H_2$, both of which reduce the $\rm g_s$ values sufficiently to prevent Raman oscillation.

4.2.4 Three-Photon Absorption

Three-photon absorption (ThPA) is a nonlinear process governed by a fifth-order susceptibility. Because ThPA is a higher-order effect its presence is negligible unless exceptionally small frequency detunings or high pump intensities are employed. Thus, the only resonance enhancement scheme amenable to ThPA is the type I scheme with near-resonant detunings at one-, two-, and three-photon resonances.

In the near-resonant case, three-photon transition probability per unit time can be written as 48

$$W(ThPA) = \frac{\pi g_L (3\omega) \eta^3 I^3}{256 h^6 n^3} \left(\frac{\mu_{32} \mu_{21} \mu_{10}}{\Delta \omega_1 \Delta \omega_2}\right)^2$$
 (102)

where $g_L(3\omega)$ is the ThPA line shape function and all other parameters have their usual meanings. This expression can be compared with two-photon transition probability per unit time as given by:⁴⁸

$$W(TPA) = \frac{\pi g_L (2w) \eta^2 I^2}{32 h^4 n^2} \left(\frac{\mu_{21} \mu_{10}}{\Delta \omega_1}\right)^2$$
 (103)

If the two-photon detuning is substantially larger than the linewidth, $g_{L}(2\omega)$ can be approximated by $\Gamma_{2}/\pi\Delta\omega_{2}^{2}$. Similarly, $g_{L}(3\omega)$ is approximately equal

to $\Gamma_3/\pi\Delta\omega_3^2$ when $\Delta\omega_3^2\gg\Gamma_3^2$. With these approximations, the ratio of the transition probabilities may be expressed as:

$$\frac{W(ThPA)}{W(TPA)} = \frac{\Gamma_3}{\Gamma_2} \left(\frac{\mu_{32}}{\Delta \omega_3}\right)^2 = \frac{\eta_1 I}{8n h^2}$$
(104)

For most type I molecules, the Γ_3/Γ_2 ratio is close to unity and $|\mu_{32}|$ is on the order of 0.1 debye. Using I = 1 GW/cm² (10^{13} W/m²) and $\Delta\omega_3$ = 1 cm² (1.886 x 10^{11} rad/sec), expression (104) yields a ratio of 0.13. Since three-photon detunings in the type I molecules are generally larger than 1 cm² for various combinations of CO laser frequencies, the above ratio indicates that ThPA effects are an order of magnitude smaller than those of TPA.

4.2.5 Gas Breakdown

Laser induced gas breakdown is a well known phenomenon with high peak power laser beams and is a major consideration in the analysis of efficiency limitations. Since beam propagation is severely affected when gas breakdown occurs, the critical intensity at which the breakdown is initiated sets the upper limit on the operating intensities for a frequency converter.

A literature survey showed that laser induced gas breakdown data are not available for the case of CO laser radiation interacting with the particular THG candidate molecular gases. Most of the experimentally observed breakdown intensities in the IR are reported for the 10 µm radiation. For example, at 3 atmospheres of H_2 the reported experimental conditions 46 imply a breakdown power density of 2.8 GW/cm² at 10 µm. The corresponding breakdown energy density would be 196 J/cm². If the quadratic frequency dependence of breakdown intensity 49 is assumed, the 10 μ m radiation data suggest a value of 11 GW/cm² for the 5 μm radiation provided all other parameters are unchanged. However, since semi-empirical models 49,50 of gas breakdown predict different behavior for short and long laser pulse lengths, estimates using scaling arguments based on 10 μm data should be regarded as a rough indication. Therefore, breakdown intensities based on the presently available information may be reasonably expected to be in the range of 1 to 10 $\,\mathrm{GW/cm}^2$. These intensity limits in turn imply minimum values of χ^{THG} for efficient conversion. At the lower limit, 10^{10} values in excess of 10^{-34} cm⁶/erg¹ are necessary, which establishes a criterion for selecting particular candidate molecules.

4.2.6 Pump Depletion

Efficiency limitation analysis so far has been presented with the assumption that pump radiation does not change appreciably in order to illustrate various limitations. In reality, frequency conversion processes do involve pump depletion by definition, but an analytical treatment becomes complex because of nonlinear coupled differential equations governing the generation and depletion processes. In general, these equations do not have closed form solutions and therefore require numerical methods for analyzing the effects of pump depletion. However, rather than computing various numerical solutions encompassing all aspects of interacting processes, a simple model including only the THG and pump depletion processes has been analyzed. This approach has an advantage of yielding an analytical solution to aid in understanding the efficiency when there is substantial pump depletion. The equations of this model, neglecting phase mismatches, can be cast in the following form:

$$\frac{dE_3}{dz} = \beta E_1^3 \tag{105}$$

$$\frac{dE_1}{dz} = -\beta E_1^2 E_3 \tag{106}$$

where $\beta = \frac{i \omega_3 \eta_N \ x^{THG}}{8 \ \eta_3}$.

Combining the Equations (105) and (106) yields the statement of energy conservation

$$E_1^2(0) - E_1^2(Z) = E_3^2(Z)$$
 (107)

Substitution of this relation into (105) and a direct integration gives the conversion efficiency ϵ :

$$\epsilon = \frac{E_3(L)}{E_1(0)}^2$$

$$= \frac{\eta_0}{1 + \eta_0}$$
(108)

where

$$\eta_0 = (\hat{p} E_1^2(0) L)^2 \propto |\chi^{THG}|^2 (NIL)^2$$

For small pump intensities, $\eta_0 \ll 1$, and the efficiency is approximately given by the value of η_0 , which is exactly the efficiency one would obtain by integrating (105) assuming no pump depletion. Hence, the efficiency figures

calculated without pump depletion are still useful in predicting the actual efficiencies provided that expression (108) is used. The relation (108) also shows that efficiencies below 10% can be calculated quite accurately without including pump depletion effects.

At very high pump intensities for which $\eta_0 > 1$, THG conversion efficiency is no longer increasing quadratically with pump intensity. Thus, pump depletion leads to an efficiency saturation behavior as described by (108). Because SFG and THG are basically related processes, similar saturation effects can be expected for SFG efficiencies.

4.3 Optimum Scheme

The discussions of various efficiency limiting processes and the calculations of key parameters in the previous sections can be summarized qualitatively as shown in Table 24. When a particular process causes a substantial decrease (e.g. more than 10%) in the actual efficiency relative to the predicted efficiency in the absence of the process, that process is considered to be signicant. If the effect leads to efficiency losses on the order of a percent for some candidate molecules of a given enhancement scheme, then the limiting process is considered moderate. Processes which are predicted to produce less than one percent changes in the conversion efficiency are regarded as small, and those with no measurable consequences are considered negligible. The table aids in illustrating the essential efficiency limiting characteristics for each of the three resonance enhancement schemes. Based on these characteristics, the following observations can be made:

In the type I resonance enhancement scheme, pump absorption leading to dynamic phase mismatches is found to be the primary efficiency limiting process. Since this scheme requires near-resonant conditions at one-, two-, and three-photon detunings, the pump absorption is always present and inherently restricts the application of the type I scheme to short pump pulses.

The type II scheme avoids dynamic phase mismatch caused by pump absorption. Other competing nonlinear processes become significant at the high pump intensities required for efficient conversion, however. Although two-photon absorption, quadratic Kerr effect, and stimulated Raman scattering ultimately

TABLE 24. EFFICIENCY LIMITATION ANALYSIS SUMMARY

SUMMARY							
PROCESS	RESONANCE ENHANCEMENT SCHEME						
PROCESS	TYPE I	TYPE II	TYPE III				
NONLINEAR EFFECTS:		. <u></u>					
● Two-Photon Absorption			,,,,,,				
 Quadratic Kerr Effect 							
Stimulated Raman Scattering (Vibrational)	1//////////////////////////////////////		<i>"\\\\\\</i>				
Stimulated Raman Scattering (Rotational)							
• Three-Photon Absorption	1////						
● Gas Breakdown							
Saturation		1////					
LINEAR EFFECTS:							
 Absorption Loss at Pump Frequency 							
 Absorption Loss at Sum Frequency 	111111						
Population Transfer-InducedPhase Mismatch			11111.				
● Thermal Defocusing			1/////				

Population Transfer-InducedPhase MismatchThermal Defocusing				
Negligible	/////. Small	Moder Moder	ate	Significan

limit the efficiency, near unity THG and SFG conversion efficiencies are predicted under optimum conditions. The parameters that govern these conditions are the two-photon resonance frequency and the values of Kerr-induced phase shifts.

The type III scheme analysis and the $\chi^{(3)}$ calculations show that relatively small conversion efficiencies can be expected. The principal efficiency limitation in this scheme is optical gas breakdown at high pump intensities. The high pump intensities are necessary to compensate for the relatively small nonlinear susceptibilities calculated for candidate molecules of this scheme.

In view of the efficiency limiting properties of the three enhancement schemes, the type II scheme provides a most promising technique for up-converting CO laser frequencies. In particular, H_2 and HD have an added advantage of extremely low dispersion in the infrared region. The refractive indices for H_2 can be calculated from a Sellmeir formula, and the calculated THG and SFG coherence length (distance at which $\Delta kL = \pi$) at 1 amagat is approximately 300 cm. This value is not very sensitive to the range of the line-selected CO laser frequencies, which permits simultaneous phase-matching for various combinations of pump frequencies. Since H_2 and HD are essentially identical in their electronic properties, dispersion properties can be expected to be similar. Thus, both H_2 and HD appear to be most suited for multiline THG or SFG.

5.0 MULTILINE THG AND SFG ANALYSIS

The CO laser output consists of several frequencies, as elucidated in Section 3.4. Thus, efficient THG and SFG processes for a number of lines are required. The phase-matching requirement for various frequency combinations is an important consideration in multifrequency THG and SFG. For example, it is desirable to phase-match all of the CO laser lines referred to in Section 3.4 for THG in a given gas mixture. The THG and SFG conversion efficiencies of the various frequency combinations may differ from one particular set to another because of the frequency dependence of the nonlinear susceptibility. Therefore, a scheme in which $\chi^{\left(3\right)}$ is near optimum and relatively insensitive to changes in the pump frequencies is needed. In the following section, calculations on candidate molecules for each of the three resonance enhancement schemes are discussed in relation to the criteria outlined above. Accordingly, an appropriate scheme for SFG is suggested.

5.1 Efficient THG and SFG Optimization

Efficient THG and SFG of the line selected CO laser frequencies requires optimization of the nonlinear susceptibility and phase-matching properties and suppression of the efficiency limiting processes. The nonlinear susceptibility calculations and the efficiency limitation analysis show that the type II resonance enhancement scheme allows efficient multiline frequency up-conversion under appropriate conditions in $\rm H_2$ or HD. These molecules have extremely small dispersion and absorption in the infrared and have relatively high peak values of $\chi^{(3)}$ on resonance. The $\chi^{(3)}$ frequency dependence also allows SFG for a number of different pump frequencies when one or more pairs of frequencies are two-photon resonant.

One important factor to consider in the type II scheme is the effect of competing nonlinear processes. In particular, stimulated rotational Raman scattering can be a dominant frequency conversion process under certain conditions. Several reports of efficient Raman shifting of CO₂ laser radiation in hydrogen indicate the significance of this competing effect.

Two important aspects of stimulated Raman scattering (SRS) should be noted. First, SRS represents a loss mechanism for the pump radiation and thereby decreases the THG and SFG efficiency. Second, frequencies shifted by SRS may

participate further in other nonlinear processes including induced two-photon absorption and sum frequency generation.

A survey calculation of the Raman-shifted multiline CO frequencies in $\rm H_2$ and HD shows that induced TPA and SFG may indeed occur. Analysis of the $\rm \chi^{SFG}$ values for these frequencies indicates that susceptibilities in the neighborhood of 10^{-34} cm $^6/\rm erg$ are possible with certain combinations of the pump and the shifted frequencies. Figure 9 shows the normalized $|\rm \chi^{SFG}|$ as a function of two-photon resonance frequency detuning for HD Q(1) transition at various gas densities. Figure 10 illustrates the corresponding curves for the normalized $|\rm \chi^{SFG}|$ as a function of gas density at certain detunings. The scale factor for the actual value of $|\rm \chi^{SFG}|$ is 3.14 x 10 $^{-34}$ cm $^6/\rm erg$. Figure 11 shows the normalized $\rm \chi^{Kerr}$ and $\rm \chi^{TPA}$ as a function of frequency detuning, which are obtained from the real and imaginary parts according to the equations in Table 9.

The actual frequency detunings $(\Delta\omega_{_{\scriptsize O}})$ obtainable for HD resonances from the certain combinations of the pump and the Raman shifted frequencies in H $_2$ (354.381 cm $^{-1}$ shift 29) are in the range of 0.2 to 1 cm $^{-1}$. For example, P(11) and P(12) of [5-4]give $\Delta\omega_{_{\scriptsize O}}=0.328$ cm $^{-1}$ for the HD Q(0) resonance, and P(9) and P(13) of [4-3] yield $\Delta\omega_{_{\scriptsize O}}=1.012$ cm $^{-1}$ for the HD Q(1) resonance. P(11) [6-5] and P(12) [4-3]also approach the Q(0) resonance with $\Delta\omega_{_{\scriptsize O}}=0.291$ cm $^{-1}$. These detunings lead to $_{\rm X}$ values of 10 $^{-34}$ cm $^6/\rm erg$. This suggests that efficient SFG may occur if phase-matching requirements can be satisfied.

5.2 <u>Two-Step Frequency Conversion</u>

The results of the multiline THG and SFG analysis suggest that an efficient multiline CO laser frequency up-converter may be possible with the use of a Raman shifting as an intermediate step. The Raman shifting in H₂ converts a part of the total pump radiation into coherent radiation near 6 μ m. The frequencies of the remaining pump radiation and the shifted frequencies add to yield the two-photon resonances in HD. This two-step process is schematically illustrated in Figure 12. The pump and the shifted frequencies are represented by $\{\omega\}$ and $\{\omega'\}$, respectively. The generated sum frequencies are of the form $\omega_S = 2\omega + \omega'$ or $2\omega' + \omega$ and are denoted by $\{\omega_S\}$.

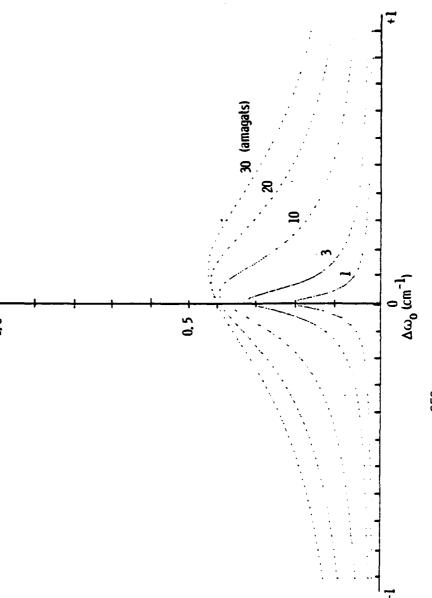
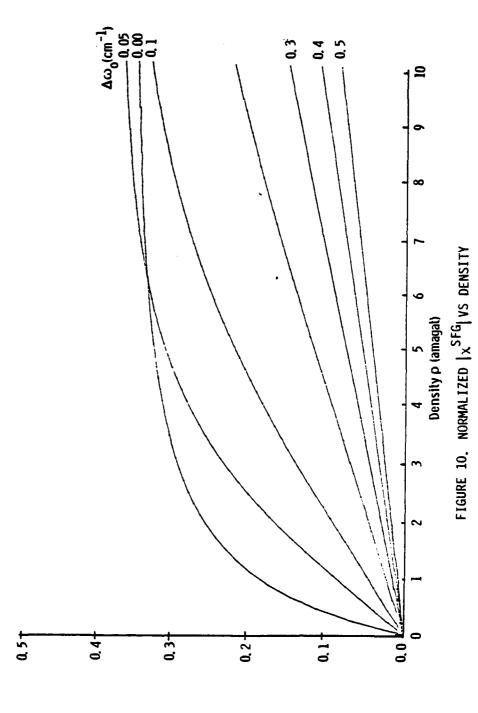


FIGURE 9. NORMALIZED | X SFG | VS HD Q(1) TWO-PHOTON RESONANCE FREQUENCY DETUNING



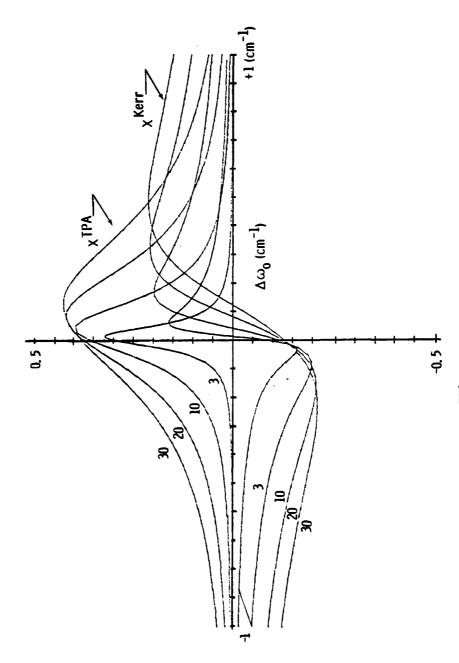


FIGURE 11. NORMALIZED $^{ ext{KERR}}_{ ext{AND}}$ AND $^{ ext{TPA}}_{ ext{VS}}$ VS HD Q(1) TWO-PHOTON RESONANCE FREQUENCY DETUNING

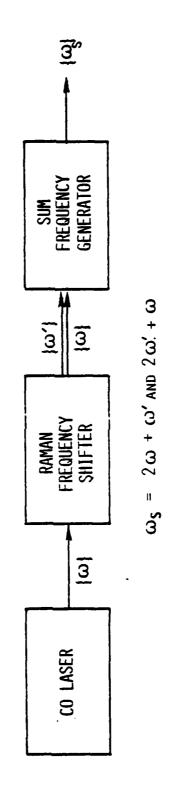


FIGURE 12. SCHEMATIC OF TWO-STEP CO LASER SUM FREQUENCY GENERATION

6.0 EXPERIMENTAL PROGRAM

The results of this study indicate that frequency up-conversion according to the type II resonance enhancement scheme in HD may be potentially efficient and warrants further investigation. Experimental data are needed to verify theoretical predictions presented in this report. Of particular interest is the frequency dependence of the conversion efficiency and of the phase-matching properties of HD. This may be used to determine the optimum parameters of the nonlinear medium for multifrequency CO laser frequency up-conversion.

6.1 Approach

The third-order susceptibility calculations and efficiency limitation analysis indicate that two-photon resonantly enhanced sum frequency generation in HD is the most promising approach to up-convert multiline CO laser frequencies. In order to verify this feasibility, an experimental investigation of SFG in HD is suggested. The investigation should consist of first setting up an experimental facility to generate tunable and fixed IR frequencies in the 5-6 μ m region and then performing parametric SFG experiments using the generated frequencies. These IR frequencies are relevant to the two-step frequency conversion process described in Section 5.2.

6.2 Experimental Facility

An IR source facility based on a Nd:YAG laser system operating at ten pulses per second would be a suitable choice because of high data acquisition rate. Figure 13 shows a block diagram of the experimental setup including a fixed and a tunable IR source. The fixed IR frequency at 6.2 μ m can be obtained by vibrational Raman frequency shifting of the Nd:YAG laser output in H₂ and HD. Figure 14 shows a schematic layout of the fixed IR source. The tunable IR frequency can be generated by difference frequency mixing ⁵² of the second harmonic of the Nd:YAG laser output and a tunable dye laser output near 0.596 μ m. Alternatively, a dye output at 0.690 μ m may be Raman shifted three times in H₂ to yield a tunable IR output. Figure 15 shows the two possible configurations of the tunable IR source. The tunable IR frequency is near 2015 cm⁻¹ (4.96 μ m) so that the sum of the tunable and the fixed IR frequencies matches the two-photon Q-branch resonances in HD. The operating conditions of the IR source facility are summarized in Table 25.

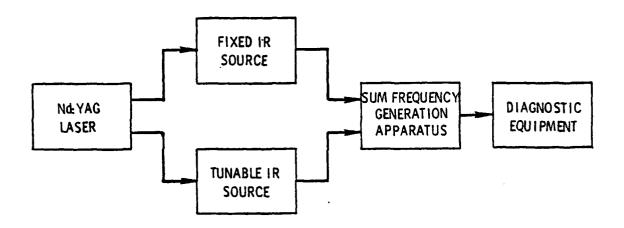


FIGURE 13 SUM FREQUENCY GENERATION EXPERIMENT BLOCK DIAGRAM

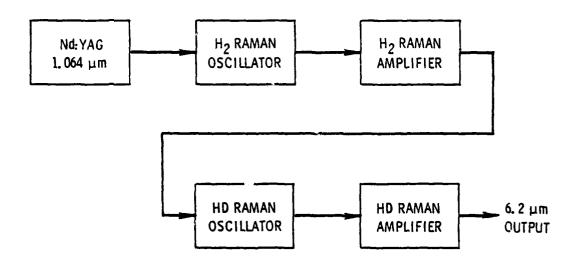


FIGURE 14. FIXED IR SOURCE BLOCK DIAGRAM

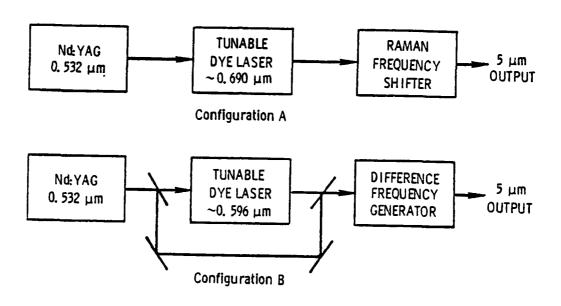


FIGURE 15. TUNABLE IR SOURCE BLOCK DIAGRAM

TABLE 25. COHERENT IR SOURCE FACILITY

FIXED IR SOURCE

Pump Laser:

Nd:YAG 1.064 μm, 10 pps, 50 MW

peak power

Frequency

Converter:

Vibrational Raman shifting in H_2 and HD (7783.4 cm⁻¹)

IR Output:

~ 5 MW peak power at 6.2 µm

TUNABLE IR SOURCE

Pump Laser:

Nd:YAG Second Harmonic 0.532 μm,

10 pps, 20 MW peak power

Frequency

Dye laser oscillator/amplifier ~ 7 MW

Tuning:

peak power output at 0.59 µm

Frequency

Difference frequency mixing of $0.532\,\mu\text{m}$

Conversion:

and 0.596 μ m in LiIO₃

IR Output:

~0.02 MW peak power at 4.96 µm

An apparatus for the SFG experiment is shown in Figure 16. It incorporates a cell consisting of a tube filled with several atmospheres of HD at 293 K, two calcium fluoride windows (to seal the ends of the tube) which transmit the pump and the generated radiation, and a gas handling system consisting of valves, gauges, and a vacuum system that controls the cell pressure.

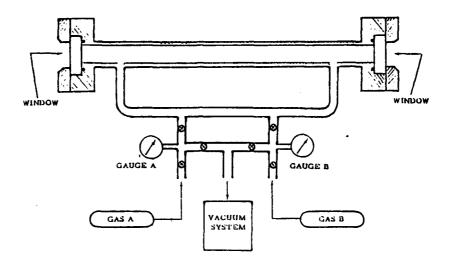


FIGURE 16. SCHEMATIC OF EXPERIMENTAL APPARATUS

6.3 Parametric Study

The parametric study should include conversion efficiency measurements as a function of two-photon resonance frequency detuning, SFG gas pressure, and pump source intensity. From these measurements the SFG nonlinear susceptibilities and the phase-matching properties of the nonlinear medium can be compared with the calculated values.

7.0 CONCLUSION

Detailed analysis and calculations on the feasibility of efficient CO laser frequency tripling have been completed. The results of this study indicate that direct frequency tripling of multiline CO laser output leads to small conversion efficiencies. These efficiencies are primarily dictated by the small nonlinear susceptibilities and the efficiency limiting processes of the molecules surveyed. However, the analysis of the three resonance enhancement schemes has yielded a potentially efficient sum frequency generation scheme in hydrogen molecules if the pump frequencies can satisfy the two-photon resonance condition.

Of the three resonance enhancement schemes investigated, the two-photon resonance (type II) scheme has been found to meet the requirements for efficient multiline frequency up-conversion of the CO laser frequencies. Various efficiency limiting processes found in the two other schemes are minimized in this scheme, and high SFG conversion efficiencies are predicted for a number of pump frequency combinations.

Unfortunately, the efficient CO laser lines do not yield frequency combinations that directly satisfy the strong resonance conditions in $\rm H_2$ or HD. However, from the analysis of stimulated rotational Raman scattering as a competing efficiency limiting process, the Raman shift in $\rm H_2$ has been found to generate frequencies which lead to HD two-photon resonances when combined with the original pump frequencies. Because Raman shifting has been demonstrated to be an efficient conversion process, this resonance coincidence provides a method of frequency up-conversion using an intermediate frequency shifting stage to optimize the sum frequency generation efficiencies. With such a two-step conversion process, output wavelengths in the 1.77 and 1.90 μm regions can be obtained.

In order to verify the feasibility of efficient sum frequency generation in HD, and experimental investigation of third-order susceptibility is recommended for future study. The measurement of SFG susceptibilities and phase-matching properties of HD should yield useful parameters for evaluating this molecular medium as a potentially efficient frequency up-converter.

8.0 REFERENCES

- 1. S. R. J. Brueck and H. Kildal, Appl. Phys. Lett. <u>33</u>, 928 (1978).
- 2. S. R. J. Brueck and H. Kildal, Opt. Lett. 2, 33 (1978).
- 3. H. Kildal, IEEE J. Quant. Electron QE-13, 109 (1977).
- M. H. Kang, V. T. Nguyen, T. Y. Chang, T. C. Damen, and E. G. Burkhardt,
 Appl. Phys. Lett. <u>33</u>, 303 (1978).
- 5. C. L. Pan, C. Y. She, W. M. Fairbank, Jr., and Ky W. Billman, IEEE J. Quant. Electron QE-13, 763 (1977).
- 6. M. J. Pellin and J. T. Yardley, Appl. Phys. Lett. 29, 304 (1976).
- 7. P. N. Butcher, <u>Nonlinear Optical Phenomena</u>, Bulletin 200, Engineering Experiment Station, Ohio State University, Columbus, Ohio (1965).
- 8. G. Herzberg, Molecular Spectra and Molecular Structure: I. Spectra of Diatomic Molecules, Second Edition, (Van Nostrand Reinhold Co., New York, 1950) p. 208.
- 9. D. B. Keck and C. D. Hause, J. Mol. Spectrosc. <u>26</u>, 163 (1968).
- 10. M. Rotenberg, N. Metropolis, R. Bivin, and J. K. Wooten, Jr., "The 3-j and 6-j Symbols," Technology Press, Massachusetts Institute of Technology, Cambridge, Mass. (1959).
- 11. C. H. Townes and A. L. Schawlow, <u>Microwave Spectroscopy</u>, (McGraw Hill Book Co. Inc., 1955), p. 74.
- 12. Placzek, <u>The Rayleigh and Raman Scattering</u>, translated from Handbuch der Radiologie, Edited by Erich Marx, Leipzig, Akademische Verlagsgesellschaft VI, 2, (1934) pp. 209-374, UCRL Trans. No. 526(L) by Ann Werbin (1959).
- 13. R. H. Pantell and H. E. Puthoff, <u>Fundamentals of Quantum Electronics</u>, (Wiley, New York, 1969), pp. 241-242.
- 14. V. E. Merchant and N. R. Isenor, IEEE J. Quant. Electron. QE-12, 603 (1976).
- 15. D. Chen, K. Rao, and R. McDowell, J. Mol. Spectry. <u>61</u>, 71 (1976)
- 16. J. P. Bouanich, J. Quant. Spectrosc. Radiat. Transfer 17, 636 (1977).
- J. Bonamy and D. Robert, J. Quant. Spectrosc. Radiat. Transfer <u>16</u>, 185 (1976).

- 18. A. Henry, M. F. LeMoal, Ph. Cardinet, and A. Valentin, J. Mol. Spectry. 70, 18 (1978).
- 19. F. P. Billingsley, J. Mol. Spectry. <u>61</u>, 53 (1976).
- 20. L. L. Abels and J. H. Shaw, J. Mol. Spectry. 20, 11 (1966).
- 21. B. Rosen, <u>Spectroscopic Data Relative to Diatomic Molecules</u>, (Pergamon, New York, 1970).
- 22. F. G. Smith, J. Quant. Spectrosc. Radiat. Transfer <u>13</u>, 717 (1973).
- 23. A. Rosenberg, A. Lightman, and A. Ben-Rouven, J. Quant. Spectosc. Radiat. Transfer 12, 219 (1972).
- 24. A. Fagt, D. van Lerberghe, G. Guelachvili, C. Amoit, P. Bernage, and P. Niay, Mol. Phys. <u>32</u>, 955 (1976).
- R. N. Stocker and A. Goldman, J. Quant. Spectosc. Radiat. Transfer <u>16</u>, 335 (1976).
- 26. H. J. Babrov, J. Chem. Phys. 40, 831 (1964).
- 27. G. Herzberg, Op. Cit., pp. 141-144.
- 28. "Molecular Lasers," Laser Handbook, Chemical Rubber Co., pp. 307-310.
- 29. B. P. Stoicheff, Can. J. Phys. <u>35</u>, 730 (1957).
- 30. W. R. Fenner, H. A. Hyatt, J. M. Kellam, S.P.S. Porto, J.O.S.A. <u>63</u>, 73 (1973).
- 31. M. A. Henesian, L. Kulevskii, R. L. Byer, and R. L. Herbst, (Abstract) Opt. Commun. 18, 225 (1976).
- 32. T. Witkowicz and A. D. May, Can. J. Phys. <u>54</u>, 575 (1976).
- 33. D. V. Webb and K. N. Rao, J. Mol. Spectry. <u>28</u>, 121 (1968).
- 34. J. M. Cherlow, H. A. Hyatt, S.P.S. Porto, J. Chem. Phys. 63, 3996 (1975).
- 35. R. E. Meredith, J. Quant. Spectosc. Radiat. Transfer 12, 485 (1972).
- 36. W. Holzer, Y. LeDuff, and K. Altmann, J. Chem. Phys. 58, 642 (1973).
- 37. K. Altmann and G. Strey, J. Mol. Spectry. 44, 571 (1972).
- 38. D. H. Rank, B. S. Rao, and T. A. Wiggins, J. Mol. Spectry. 17, 122 (1965).

- 39. Calculated from Reference 21 and isotope shift.
- 40. R. N. Sileo and T. A. Cool, J. Chem. Phys. <u>65</u>, 117 (1976).
- 41. F. G. Smith and R. E. Meredith, J. Quant. Spectrosc. Radiat. Transfer 14, 385 (1974).
- 42. R. B. Miles and S. E. Harris, IEEE J. Quant. Electron. QE-9, 470 (1973).
- 43. E. A. Stappaerts, IEEE J. Quant. Electron QE-15, 110 (1979).
- 44. E. A. Stappaerts, Phys. Rev. A <u>11</u>, 1664 (1975).
- 45. N. Bloembergen, Am. J. Phys. <u>35</u>, 989 (1967).
- 46. R. L. Byer and W. R. Trutna, Opt. Lett. <u>3</u>, 144 (1978).
- 47. P. Rabinowitz, A. Stein, R. Brickman, and A. Kaldor, Opt. Lett. 3, 147 (1978).
- 48. R. H. Pantell and H. E. Puthoff, Op. Cit., pp. 141-142.
- 49. D. C. Smith, J. Appl. Phys. 41, 4501 (1970).
- 50. C. C. Wang and L. I. Davis, Phys. Rev. Lett. <u>26</u>, 822 (1971).
- 51. M. Karplus, J. Chem. Phys. 41, 880 (1964).
- 52. D. W. Meltzer and L. S. Goldberg, Opt. Commun. <u>5</u>, 209 (1972).

APPENDIX A: x (3) CODE

Program Structure and Performance

The program consists of loops over the vibrational and rotational quantum numbers. Inside these nested loops, subroutines are called and the following steps are performed:

- (1) Calculation of rotational and vibrational terms, and partition functions
- (2) Calculation of rotational populations and all transition frequencies allowed by selection rules
- (3) Calculation of the frequency denominator which occurs in the nested sum over states
- (4) Inclusion of all permutations of the three input frequencies

Several subroutines are called in the course of the program. The structure and function of each of these is relatively simple, and, therefore, will only be described briefly. Subroutine FREQ calculates the frequency denominator and sets up the indices to be printed when a resonance is encountered. Subroutine SUMO provides the contributions to the sum over states of the total angular momentum projected along the molecular axis (OMEGA) when the molecular ground state is spatially degenerate (LAMBDA is not zero).

Matrix elements involving anharmonic oscillator eigenfunctions which are required for inclusion of an upper electronic level in the $\chi^{(3)}$ calculation are calculated in the subroutine LMENTS. The sum over state of the total angular momentum projected along the molecular axis for a spatially degenerate upper electronic level is performed in the subroutine TUMO. Finally, the frequency denominators which involve more than one electronic level are evaluated in subroutine GREQ.

The data items to be input, specified in READ statements at the beginning of the main program, consist of alphanumeric symbols, indicators, spectroscopic constants, and transition moments. The spectroscopic constants may be found in the literature. All input variables should be expressed in cgs units unless otherwise specified. In addition, the program presets all unspecified variables to zero.

In the program, the input variables have been assigned the following names:

LABEL is an alphanumeric array which stores the name of the molecule for which the calculation is performed

NV is the number of vibrational levels used in the calculation

NJ is the number of rotational levels used in the calculation

WE, WEXE,

are the familiar vibrational constants: w_e , $w_e x_e$, $w_e y_e$, $w_e z_e$, WEYE, WEZE respectively

BE, ALPHA, GAMMA, DE, BETA

are the usual rotational constants: B_e , α_e , γ_e , D_e , β_e , respectively

AE, DELTA are additional rotational constants which must be specified only if the ground electronic state is spatially degenerate

OMEGAE is the energy of an upper electronic state; this is set to zero if it is desired to only include the ground electronic state in the calculation

MGE is a real array which stores the electronic transition moments

U(5.5) is a real array which stores the dipole moments for vibrational transitions between states labeled N and M (in Debye)

FWHM is a real array which stores the linewidths for vibrational and rotational transitions

TEMP is the temperature of the system being modeled

WSIZE is the size of the interval about the input pump frequencies inside of which the program will indicate that a resonance has been approached.

IWRITE is an integer flag such that if it is set equal to one the program prints out the individual excitation path contributions or if it is set equal to two the program calculates only the contribution from the $v_a = 0$, $v_b = 3$, $v_c = 2$, $v_d = 1$ excitation

IPOINT is an integer flag such that if it is set equal to one the program calculates results for frequency tripling for pump frequencies ranging from WQ to WP with a step size of WR

WP, WQ, WR these are the pump frequencies (in cm^{-1}). The program terminates when all three are set to zero

There are also several COMMON variables used in the program. SIZE, AE, DELTA, WE, WEXE are also input variables and have been described. Some other COMMON variables are listed and described below:

NA, NB, NC, ND are the indices for the appropriate vibrational levels

RA, RB
RC, RD are the indices for the appropriate rotational levels

FABCD(20) is the frequency denominator

EAB, EAC, EAD are the imaginary half-widths

W(2,5,50) is a real array which stores the calculated energy levels

RS(2,3,50) is a real array which stores the calculated intermediate coupling coefficients ($\Lambda \neq 0$)

X(5,2,3) is a real array containing the anharmonic oscillator matrix elements (when an upper electronic state is included in the calculation)

OMEGAA,OMEGAB OMEGAC,OMEGAD are the projections of the total angular moments on the molecular axis ($\Lambda \neq 0$)

The output consists of various blocks listing the following:

- (1) All input data
- (3) Single path contributions of the susceptibility (if IWRITE = 1)
- (4) The sum frequency, the real part of $\chi^{(3)}$, the imaginary part of $\chi^{(3)}$, and the modulus of $\chi^{(3)}$

A complete calculation for one molecule, considering up to 4 vibrational levels and 30 rotational levels takes less than 26 seconds on a CDC 6600, yielding results for 10 sets of pump frequencies.

Program Listing

PROGRAM CHITHME (INPUT-DUTPUT-TAPES=INPUT-TAPES=OUTPUT-DEBUG=OUTPUT CHITME 2 THIS PURGEAM CALCULATES THIMU ORDER SUSCEPTIBILITIES FROM SPECTHO- CHITME 4 CHITME 4 CHITME 6 CHITME 7 CHITME 7 CHITME 7 CHITME 7 CHITME 10 CHITME 11 CHITME 11 CHITME 11 CHITME 11 CHITME 12 CHITME 12 CHITME 13 CHITME 14 CHITME 14 CHITME 14 CHITME 15 CHITME 16 CHITME 17 CHITME 17 CHITME 18 CHITME 19 CHITME 19 CHITME 10 CHITME 10 CHITME 11 CHITME 12 CHITME 12 CHITME 12 CHITME 13 CHITME 14 CHITME 14 CHITME 15 CHITME 16 CHITME 16 CHITME 17 CHITME 17 CHITME 17 CHITME 18 CHITME 18 CHITME 19 CHITME 19 CHITME 19 CHITME 21 CHITME 22 CHITME 22 CHITME 23 CHITME 25 CHITME 25 CHITME 25 CHITME 25 CHITME 26 CHITME 26 CHITME 27 CHITME 26 CHITME 27 CHITME 31 CHITME 31 CHITME 31 CHITME 31 CHITME 31 CHITME 31 CHITME 32 CHITME 32 CHITME 33 CHITME 33 CHITME 34 CHIT	74/14	0PT=2 UU	FTN 4.6+433R	11/22/78	11.36.27
THIS PURGRAM CALCULATES THIND ORDER SUSCEPTIBILITIES FROM SPECTMO CHITHRE 5 SUPPIC DATA PURPORTS CHITHRE 7 CHITHRE 6 CHITHRE 7 CHITHRE 7 CHITHRE 7 CHITHRE 7 CHITHRE 10 CHITHRE 11 CHITHRE 11 CHITHRE 12 CHITHRE 12 CHITHRE 13 CHITHRE 14 CHITHRE 15 CHITHRE 16 CHITHRE 16 CHITHRE 17 CHITHRE 17 CHITHRE 18 CHITHRE 18 CHITHRE 18 CHITHRE 18 CHITHRE 18 CHITHRE 19 CHITHRE 18 CHITHRE 19 CHITHRE 20 CHITHRE 20 CHITHRE 20 CHITHRE 21 CHITHRE 21 CHITHRE 22 CHITHRE 23 CHITHRE 23 CHITHRE 25 CHITHRE 25 CHITHRE 25 CHITHRE 26 CHITHRE 26 CHITHRE 26 CHITHRE 26 CHITHRE 27 CHITHRE 27 CHITHRE 27 CHITHRE 28 CHITHRE 29 CHITHRE 29 CHITHRE 29 CHITHRE 29 CHITHRE 29 CHITHRE 31 CHITHRE 32 CHITHRE 32 CHITHRE 31 CHITHRE 32 CHITHRE 33 CHITHRE 32 CHITHRE 33 CHITHRE 32 CHITHRE 32 CHITHRE 33 CHITHRE 32 CHITHRE 33 CHITHRE 32 CHITHRE 33 CHITHRE 32 CHITHRE 33 CHITHRE 34 CHITHRE 33 CHITHRE 34 CHITHRE 34 CHITHRE 35 CHITHRE 34 CHITHRE 34 CHITHRE 35 CHITHRE 34 CHITHRE 35 CHITHRE 35 CHITHRE 32 CHITHRE 34 CHITHRE 34 CHITHRE 34 CHITHRE 34 CHITHRE	PHUGRAM CHITH	IRF (INPUT•OUTPUT•T4PE5=I	NPUT .TAPE6=OUTPUT .DEBUG=OUTPU	JT CHITHRE	2
THIS PURGHAM CALCULATES THIND ORDER SUSCEPTIBILITIES FROM SPECTMO CHITHME SCUPIC DATA CHITHME CHITHM				CHITHRE	
CMITHME CMIT	•			CHITHRE	
CHITHRE CHIT	THES PROGRAM	CALCULATES THIRD ORDER	SUSCEPTIBILITIES FROM SPECTHO	- CHITHRE	5
INPUTS	SCUPIC DATA			CHITHRE	4
INDITS				CHITHRE	7
THE				34HT1HO	4
CHITHE 12				CHITHRE	4
CHITHE 12 CHITHE 13 CHITHE 14 CHITHE 14 CHITHE 15 CHITHE 16 CHITHE 16 CHITHE 17 CHITHE 18 CHITHE 18 CHITHE 18 CHITHE 18 CHITHE 18 CHITHE 19	INPUTS			CHITHRE	10
CHITHE 19					11
CHITME 14 NV+NU (215) CHITME 15 CHITME 15 CHITME 16 CHITME 17 IV = NUMBER OF VIBRATIONAL LEVELS USED IN THIS CALCULATION CHITME 17 IV = NUMBER OF VIBRATIONAL LEVELS USED IN THIS CALCULATION CHITME 19 CHITME 19 CHITME 19 CHITME 20 CHITME 21 CHITME 21 CHITME 21 CHITME 21 CHITME 21 CHITME 21 CHITME 22 CHITME 23 CHITME 25 CHITME 26 CHITME 27 CHITME 26 CHITME 26 CHITME 26 CHITME 26 CHITME 27 CHITME 26 CHITME 26 CHITME 26 CHITME 26 CHITME 27 CHITME 26 CHITME 26 CHITME 27 CHITME 26 CHITME 27 CHITME 26 CHITME 27 CHITME 27 CHITME 27 CHITME 27 CHITME 28 CHITME 30 CHITME 31 CHITME 32 CHITME 32 CHITME 33 CHITME 34 CHITME 36 CHITME 37 CHITME 40 CHITME 41 CHITME 42 CHITME 44 CHITME 45 CHITME 46 CHITME 47 CHITME 49 CHITME 55 CH					12
NV+NU	[AUFL([).I=1.	· · ·	(01AB)		13
NV = NUMBER OF VIBRATIONAL LEVELS USED IN THIS CALCULATION	•				-
THESE ARE THE VIBRATIONAL CONSTANTS (IN RECIPPOCAL CM) ALE-DELTA OMEGAE: MUL(1). I=1.3 OMEGAE: MUL(1). I=1.3 OMEGAE: ELECTUONIC ENERGY: ZEPO IF ONLY GROUND STATE IS INCLUDED OMEGAE: MUL(1). I=1.3 OMEGAE: ELECTUONIC ENERGY: ZEPO IF ONLY GROUND STATE IS INCLUDED OMEGAE: MUL(1). I=1.0 OMEGAE:					
THE ARE THE VIBRATIONAL LEVELS USED IN THIS CALCULATION WE WERKE WALTE WEZE WE WEXE WALTE WEZE THESE ARE THE VIBRATIONAL CONSTANTS (IN RECIPROCAL CM) CHITHRE 21 CHITHRE 22 CHITHRE 23 CHITHRE 23 CHITHRE 23 CHITHRE 23 CHITHRE 25 CHITHRE 26 CHITHRE 26 CHITHRE 26 CHITHRE 26 CHITHRE 27 CHITHRE 26 CHITHRE 26 CHITHRE 27 CHITHRE 26 CHITHRE 27 CHITHRE 26 CHITHRE 27 CHITHRE 27 CHITHRE 26 CHITHRE 27 CHITHRE 26 CHITHRE 27 CHITHRE 37 CHITHRE 31 CHITHRE 41 CHITHRE 41 CHITHRE 41 CHITHRE 42 CHITHRE 42 CHITHRE 42 CHITHRE 42 CHITHRE 43 CHITHRE 42 CHITHRE 43 CHITHRE 44 CHITHRE 45 CHITHRE 45 CHITHRE 46 CHITHRE 46 CHITHRE 47 CHITHRE 47 CHITHRE 47 CHITHRE 47 CHITHRE 47 CHITHRE 49 CHITHRE 40 CHITHRE	LN• 4N		(215)	_	-
NJ = WIMMER OF ROTATIONAL LEVELS USED IN THIS CALCULATION WE-WEXE-WEXE-WEXE. WE-WEXE-WEXE-WEXE. WE-WEXE-WEXE-WEXE. WE-WEXE-WEXE-WEXE. WE-WEXE-WEXE-WEXE. WE-WEXE-WEXE-WEXE. WE-WEXE-WEXE-WEXE. WE-WEXE-WEXE. WE CHITHRE 23 CHITHRE 23 CHITHRE 26 CHITHRE 26 CHITHRE 26 CHITHRE 26 CHITHRE 26 CHITHRE 27 CHITHRE 26 CHITHRE 26 CHITHRE 27 CHITHRE 26 CHITHRE 27 CHITHRE 27 CHITHRE 26 CHITHRE 27 CHITHRE 30 CHITHRE 30 CHITHRE 30 CHITHRE 30 CHITHRE 32 CHITHRE 32 CHITHRE 32 CHITHRE 32 CHITHRE 33 CHITHRE 36 CHITHRE 37 CHITHRE 36 CHITHRE 37 CHITHRE 36 CHITHRE 40 CHITHRE 50 CHITH					
CHITHRE 21 WE-WEXE-WETE-WEZE (4E15-8) CHITHRE 22 THESE ARE THE VIBRATIONAL CONSTANTS (IN RECIPERCAL CM) CHITHRE 23 GE-ALPHA-JAMMA-DE-HETA (5E15-8) CHITHRE 25 GH-ALPHA-JAMMA-DE-HETA (5E15-8) CHITHRE 26 GHITHRE 26 GHITHRE 27 THESE ARE THE NOTATIONAL CONSTANTS (IN RECIPPOCAL CM) CHITHRE 26 GHITHRE 27 THESE ARE THE NOTATIONAL CONSTANTS (IN RECIPPOCAL CM) CHITHRE 27 CHITHRE 29 CHITHRE 29 CHITHRE 30 CHITHRE 30 CHITHRE 30 CHITHRE 30 CHITHRE 30 CHITHRE 30 CHITHRE 31 AUDITIONAL HOTATIONAL CONSTANTS FOD LAMBDA NF 0 CASE CHITHRE 30 WHEN BOTH AE AND DELTA ARE SET TO ZERO. PROGRAM ASSUMES LAMBDA = 0 CHITHRE 36 CHITHRE 37 CHITHRE 40 CHITHRE 41 CHITHRE 42 CHITHRE 42 CHITHRE 42 CHITHRE 43 CHITHRE 45 CHITHRE 45 CHITHRE 45 CHITHRE 45 CHITHRE 45 CHITHRE 47 CHITHRE 57					
DE-WEXE-WEXE-WEXE WE-WEXE-WEXE-WEXE THESE ARE THE VIBRATIONAL CONSTANTS (IN RECIPROCAL CM) GE+ALPHA+DAMMA-DE-HETA THESE ARE THE NOTATIONAL CONSTANTS (IN RECIPPOCAL CM) GE+ALPHA+DAMMA-DE-HETA THESE ARE THE HOTATIONAL CONSTANTS (IN RECIPPOCAL CM) GE-DELTA GE-DELTA AUDITIONAL HOTATIONAL CONSTANTS FOO LAMBDA NF O CASE WHEN BOTH AE AND DELTA ARE SET TO ZERO. PROGRAM ASSUMES LAMBDA = 0 CHITHRE 33 CHITHRE 36 CHITHRE 37 CHITHRE 37 CHITHRE 38 CHITHRE 38 CHITHRE 39 CHITHRE 40 CHITHRE 40 CHITHRE 40 CHITHRE 40 CHITHRE 41 CHITHRE 42 CHITHRE 42 CHITHRE 42 CHITHRE 42 CHITHRE 42 CHITHRE 45 CHITHRE 46 CHITHRE 45 CHITHRE 50	M) = MIWHEK O	IF ROTATIUNAL LEVELS USE	D IN THIS CALCULATION		-
## WEXE WEXE WEXE CHITHRE 72 THESE ARE THE VIBRATIONAL CONSTANTS (IN RECIPROCAL CM) CHITHRE 73 BE ALPHA - JAMMA - DE - HETA (5E15.8) CHITHRE 75 BE ALPHA - JAMMA - DE - HETA (5E15.8) CHITHRE 75 BE - ALPHA - JAMMA - DE - HETA (5E15.8) CHITHRE 75 BE - OFFICE ARE THE HOTATIONAL CONSTANTS (IN RECIPPOCAL CM) CHITHRE 75 ADDITIONAL HOTATIONAL CONSTANTS FOR LAMBDA NF 0 CASE CHITHRE 75 AND ITIONAL HOTATIONAL CONSTANTS FOR LAMBDA NF 0 CASE CHITHRE 75 OMEGAE! MOE (1) · I = 1 · 3 (4E15.8) CHITHRE 75 OMEGAE! MOE (1) · I = 1 · 3 (4E15.8) CHITHRE 75 OMEGAE! MOE (1) · I = 1 · 3 (4E15.8) CHITHRE 75 OMEGAE! THE FLECTRONIC TRANSITION MOMENTS CHITHRE 75 OMEGAE! MOE (1) · I = 1 · 3 (4E15.8) CHITHRE 75 OMEGA! MOE (1) · I = 1 · 3 (4E15.8) CHITHRE 75 OMEGAE! MOE (1) · I =					
THESE ARE THE VIBRATIONAL CUNSTANTS (IN RECIPROCAL CM) CHITHRE 24 CHITHRE 25 GL+ALPHA+JAMMA,DE+HETA CHITHRE 26 GL+ALPHA+JAMMA,DE+HETA CHITHRE 27 THESE ARE THE HOTATIONAL CONSTANTS (IN RECIPPOCAL CM) CHITHRE 28 CHITHRE 29 CHITHRE 31 CHITHRE 31 CHITHRE 31 CHITHRE 32 CHITHRE 32 CHITHRE 32 CHITHRE 32 CHITHRE 32 CHITHRE 33 CHITHRE 33 CHITHRE 34 WHEN BOTH AL AND DELTA ARE SET TO ZERO. PROGRAM ASSUMES LAMBDA = 0 CHITHRE 36 CHITHRE 36 CHITHRE 36 CHITHRE 37 CHITHRE 38 CHITHRE 39 CHITHRE 40 CHITHRE 40 CHITHRE 40 CHITHRE 41 CHITHRE 42 CHITHRE 42 CHITHRE 42 CHITHRE 42 CHITHRE 42 CHITHRE 42 CHITHRE 45 CHITHRE 45 CHITHRE 45 CHITHRE 45 CHITHRE 45 CHITHRE 46 CHITHRE 46 CHITHRE 47 CHITHRE 47 CHITHRE 46 CHITHRE 47 CHITHRE 49 CHITHRE 50 CHITHRE					
THESE ARE THE VIBRATIONAL CONSTANTS (IN RECIPROCAL CM) CHITHRE 25 CHITHRE 25 CHITHRE 27 CHITHRE 28 CHITHRE 30 CHITHRE 30 CHITHRE 31 CHITHRE 31 CHITHRE 31 CHITHRE 31 CHITHRE 31 CHITHRE 31 CHITHRE 32 CHITHRE 32 CHITHRE 33 CHITHRE 33 CHITHRE 33 CHITHRE 36 CHITHRE 36 CHITHRE 36 CHITHRE 36 CHITHRE 37 CHITHRE 37 CHITHRE 38 CHITHRE 40 CHITHRE 50	MF + MEXE + MF & E +	WEZE	(48(5,8)		
CHITHRE 25 CHITHRE 26 CHITHRE 26 CHITHRE 27 CHITHRE 28 CHITHRE 30 CHITHRE 31 CHITHRE 31 CHITHRE 31 CHITHRE 31 CHITHRE 32 CHITHRE 33 CHITHRE 33 CHITHRE 33 CHITHRE 34 CHITHRE 36 CHITHRE 36 CHITHRE 36 CHITHRE 37 CHITHRE 40 CHITHRE 40 CHITHRE 40 CHITHRE 40 CHITHRE 42 CHITHRE 42 CHITHRE 42 CHITHRE 43 CHITHRE 45 CHITHRE 45 CHITHRE 45 CHITHRE 46 CHITHRE 46 CHITHRE 47 CHITHRE 57			. I. Daniel att.		
CHITHRE 26 CHITHRE 27 CHITHRE 29 CHITHRE 30 CHITHRE 30 CHITHRE 31 CHITHRE 32 CHITHRE 33 CHITHRE 33 CHITHRE 33 CHITHRE 33 CHITHRE 33 CHITHRE 34 CHITHRE 36 CHITHRE 36 CHITHRE 36 CHITHRE 36 CHITHRE 37 CHITHRE 38 CHITHRE 38 CHITHRE 38 CHITHRE 38 CHITHRE 38 CHITHRE 38 CHITHRE 39 CHITHRE 40 CHITHRE 50 CHIT	THESE ARE THE	VIBRATIONAL CONSTANTS	(IN RECIPROCAL CM)		-
### ### ### ### #### #### ############					
THESE ARE THE ROTATIONAL CONSTANTS (IN RECIPPOCAL CM) CHITHRE 2A CHITHRE 30 CHITHRE 30 CHITHRE 31 CHITHRE 32 CHITHRE 33 CHITHRE 33 CHITHRE 33 CHITHRE 33 CHITHRE 34 WHEN BOTH AE AND DELTA ARE SET TO ZERO. PROGRAM ASSUMES LAMBDA = 0 CHITHRE 37 CHITHRE 38 CHITHRE 37 CHITHRE 37 CHITHRE 37 CHITHRE 38 CHITHRE 40 CHITHRE 40 CHITHRE 40 CHITHRE 40 CHITHRE 40 CHITHRE 41 CHITHRE 42 CHITHRE 42 CHITHRE 43 CHITHRE 43 CHITHRE 45 CHITHRE 45 CHITHRE 45 CHITHRE 45 CHITHRE 45 CHITHRE 45 CHITHRE 46 CHITHRE 47 CHITHRE 47 CHITHRE 47 CHITHRE 47 CHITHRE 47 CHITHRE 47 CHITHRE 48 CHITHRE 48 CHITHRE 49 CHITHRE 49 CHITHRE 50			(FE) E 41		
THESE ARE THE ROTATIONAL CONSTANTS (IN RECIPPOCAL CM) CHITHRE 30 CHITHRE 31 ACCHITHRE 31 ACCHITHRE 31 ACCHITHRE 32 ACCHITHRE 32 ACCHITHRE 33 AUDITIONAL ROTATIONAL CONSTANTS FOD LAMBDA NF 0 CASE WHEN BOTH AE AND DELTA ARE SET TO ZERO. PROGRAM ASSUMES LAMBDA = 0 CMITHRE 36 CHITHRE 36 CHITHRE 37 OMEGAE: MOE(1). I=1.3 CHITHRE 38 CHITHRE 40 CHITHRE 40 CHITHRE 42 CHITHRE 42 CHITHRE 42 CHITHRE 42 CHITHRE 42 CHITHRE 43 CHITHRE 42 CHITHRE 45 CHITHRE 45 CHITHRE 45 CHITHRE 45 CHITHRE 45 CHITHRE 45 CHITHRE 46 CHITHRE 46 CHITHRE 47 CHITHRE 46 CHITHRE 47 CHITHRE 47 CHITHRE 48 CHITHRE 49 CHITHRE 50 CHITHRE 50 CHITHRE 51 CHITHRE 51 CHITHRE 52 CHITHRE 53 CHITHRE 53 CHITHRE 54 CHITHRE 54 CHITHRE 54 CHITHRE 55 CHITHRE 55	BE + AL PHA + GAMM	IA . DE . HE I A	(7612.0)		
### CHITHPE 30 CHITHPE 31 CHITHPE 32 CHITHPE 33 CHITHPE 33 CHITHPE 33 CHITHPE 33 CHITHPE 33 CHITHPE 33 CHITHPE 35 CHITHPE 35 CHITHPE 35 CHITHPE 35 CHITHPE 36 CHITHPE 36 CHITHPE 36 CHITHPE 36 CHITHPE 36 CHITHPE 36 CHITHPE 37 CHITHPE 46 CHITHPE 46 CHITHPE 47 CHITHPE 42 CHITHPE 42 CHITHPE 42 CHITHPE 42 CHITHPE 42 CHITHPE 43 CHITHPE 44 CHITHPE 45 CHITHPE 45 CHITHPE 45 CHITHPE 45 CHITHPE 46 CHITHPE 47 CHITHPE 57 CHITHPE	-utre in the		IN MECHODOCAL CM		
### ### ### ### ### ### ### ### ### ##	THESE ARE THE	SOLVITONAL CONSTRUITS (THE RECIPIONAL CAN		
AUDITIONAL HOTATIONAL CONSTANTS FOR LAMBDA NF 0 CASE WHEN BOTH AE AND DELTA ARE SET TO ZERO. PROGRAM ASSUMES LAMBDA = 0 CHITHRE 36 CHITHRE 36 CHITHRE 36 CHITHRE 38 CHITHRE 39 CHITHRE 39 CHITHRE 40 CHITHRE 40 CHITHRE 40 CHITHRE 40 CHITHRE 42 CHITHRE 42 CHITHRE 42 CHITHRE 43 CHITHRE 43 CHITHRE 45 CHITHRE 47 CHITHRE 49 CHITHRE 49 CHITHRE 50					
AUDITIONAL HOTATIONAL CONSTANTS FOR LAMBDA NF 0 CASE WHEN BOTH AE AND DELTA ARE SET TO ZERO* PROGRAM ASSUMES LAMBDA = 0 CHITHRE 36 CHITHRE 37 OMEGAE! MUE(1)* I=1*3 (4E15.8) CHITHRE 37 OMEGAE! MUE(1)* I=1*3 (4E15.8) CHITHRE 39 OMEGAE = CLECTHONIC ENERGY: ZERO IF ONLY GROUND STATE IS INCLUDED CHITHRE 40 MUE(I) = IHF FLECTRONIC TRANSITION MOMENTS CHITHRE 42 FUR FACH VIHRATIONAL LEVEL* N FUR FACH VIHRATIONAL LEVEL* N U(M***): M=1************************************	45 . DEL #4		(2515 8)		-
AUDITIONAL HOTATIONAL CONSTANTS FOD LAMBDA NF 0 CASE WHEN BOTH AE AND DELTA ARE SET TO ZERO. PROGRAM ASSUMES LAMBDA = 0 CHITHRE 36 CHITHRE 37 OMEGAET MODE(1). [=].3 (4615.8) CHITHRE 39 OMEGAE = CLECTHONIC ENERGY: ZERO IF ONLY GROUND STATE IS INCLUDED CHITHRE 39 OMEGAE = CLECTHONIC IRANSITION MOMENTS CHITHRE 40 OMEGAE = CLECTHONIC IRANSITION MOMENTS CHITHRE 41 OHITHRE 42 CHITHRE 43 OHITHRE 44 OHITHRE 45 OHITHRE 46 OHITHRE 46 OHITHRE 46 OHITHRE 46 OHITHRE 47 OHITHRE 48 OHITHRE 48 OHITHRE 48 OHITHRE 50 CHITHRE 50 CHITHRE 50 CHITHRE 51 CHITHRE 52 CHITHRE 53 CHITHRE 54 CHITHRE 54 CHITHRE 55 CHITHRE 56 CHITHRE 57	BE ALIEP IN		(721310		
WHEN BOTH AE AND DELTA ARE SET TO ZERO. PROGRAM ASSUMES LAMBDA = 0 CHITHRE 36 CHITHRE 37 CHITHRE 37 CHITHRE 37 CHITHRE 37 CHITHRE 39 CHITHRE 39 CHITHRE 39 CHITHRE 39 CHITHRE 39 CHITHRE 40 CHITHRE 50	AUDITIONAL GO	TATIONAL CONSTANTS FOR	I ANHOA NE O CASE	-	_
CHITHRE 36 CHITHRE 37 CHITHRE 37 CHITHRE 37 CHITHRE 38 CHITHRE 39 CHITHRE 39 CHITHRE 39 CHITHRE 39 CHITHRE 39 CHITHRE 40 CHITHRE 40 CHITHRE 41 CHITHRE 42 CHITHRE 42 CHITHRE 42 CHITHRE 43 CHITHRE 44 CHITHRE 45 CHITHRE 45 CHITHRE 45 CHITHRE 46 CHITHRE 46 CHITHRE 46 CHITHRE 47 CHITHRE 47 CHITHRE 48 CHITHRE 47 CHITHRE 48 CHITHRE 48 CHITHRE 48 CHITHRE 48 CHITHRE 49 CHITHRE 49 CHITHRE 49 CHITHRE 50 CHITHRE 50 CHITHRE 51 CHITHRE 51 CHITHRE 53 CHITHRE 53 CHITHRE 53 CHITHRE 53 CHITHRE 54 CHITHRE 53 CHITHRE 54 CHITHRE 54 CHITHRE 56 CHITHRE 56 CHITHRE 57 CHITHRE 56 CHITHRE 57	WHEN BOTH AL	AND DELTA ARE SET TO ZE	RO. PROGRAM ASSUMES LAMBDA =		-
OMEGAET MODE(1) = 1+3 OMEGAET MODE(1) = 1=1+3 OMEGAE = CLECTHORIC ENERGY: ZERO IF ONLY GROUND STATE IS INCLUDED CHITHRE 30 CHITHRE 40 CHITHRE 41 CHITHRE 42 CHITHRE 42 CHITHRE 43 CHITHRE 43 CHITHRE 43 CHITHRE 43 CHITHRE 43 CHITHRE 43 CHITHRE 44 CHITHRE 44 CHITHRE 44 CHITHRE 44 CHITHRE 45 CHITHRE 45 CHITHRE 46 CHITHRE 46 CHITHRE 47 CHITHRE 47 CHITHRE 47 CHITHRE 47 CHITHRE 47 CHITHRE 48 CHITHRE 48 CHITHRE 48 CHITHRE 49 CHITHRE 50 CHITHRE 50 CHITHRE 50 CHITHRE 51 CHITHRE 51 CHITHRE 52 CHITHRE 52 CHITHRE 52 CHITHRE 53 CHITHRE 53 CHITHRE 54 CHITHRE 55 CHITHRE	Wiley Stylle HE	AND DEETH AND DET TO RE			-
OMEGAET MODE(1) * [=]*3 OMEGAET MODE(1) * [=]					
CHITHRE 39 OMEGAE = ELECTRONIC ENERGY: ZERO IF ONLY GROUND STATE IS INCLUDED CHITHRE 40 MINE(I) = THE FLECTRONIC TRANSITION MOMENTS CHITHRE 42 FUN FACH VINNATIONAL LEVEL. N FUN FACH VINNATIONAL LEVEL. N GI(M.N) = JIPULE MOMENTS FOR VINNATIONAL TRANSITIONS N TO M CHITHRE 48 GI(M.N) = JIPULE MOMENTS FOR VINNATIONAL TRANSITIONS N TO M CHITHRE 49 GITHRE 49 CHITHRE 49 CHITHRE 51 FWENI(L) = L=1 * NV (SE15.8) CHITHRE 52 L=1 * MOTATIONAL CHITHRE 53 L=2 * U TO 1 VIBRATIONAL CHITHRE 54 L=3 * U TO 2 VIBRATIONAL CHITHRE 57	OMEGAET MUELL	1. !=1.3	(4E15.8)		
MINE(I) = THE FLECTRONIC TRANSITION MOMENTS CHITHRE 42 CHITHRE 42 CHITHRE 43 FUN FACH VIHRATIONAL LEVEL. N (SEIS.8) CHITHRE 46 (INTERNATIONAL LEVEL. N (SEIS.8) CHITHRE 47 CHITHRE 47 CHITHRE 47 CHITHRE 48 (INTERNATIONAL TRANSITIONS N TO M CHITHRE 48 CHITHRE 49 CHITHRE 49 CHITHRE 49 CHITHRE 50 CHITHRE 51 L=1. NU TO 1 VIENALIONAL CM) L=2. U TO 1 VIENALIONAL CM 55 CHITHRE 56 CHITHRE 57 CHITHRE 57	Wileyac V Week				19
MINE(I) = IMF FLECTRONIC TRANSITION MOMENTS CHITHRE 42 CHITHRE 42 CHITHRE 43 CHITHRE 45 II(M.N.) . MELINIV (SEIS.8) CHITHRE 45 II(M.N.) = JEPOLE MOMENTS FOR VERRATIONAL TRANSITIONS N TO M CHITHRE 47 (IN DEBYE) EWHN(L) * L=1.*V CHITHRE 51 CHITHRE 52 CHITHRE 53 CHITHRE 53 CHITHRE 53 CHITHRE 54 L=1* MOTATIONAL CH) L=2* U TO 1 VIBRATIONAL CHITHRE 55 CHITHRE 56 CHITHRE 56 CHITHRE 57	OMEGAE = ELEC	TWONIC ENERGY: ZERO IE	ONLY GROUND STATE IS INCLUDED	CHITHRE	40
CHITHRE 42 CHITHRE 43 CHITHRE 43 CHITHRE 44 CHITHRE 44 CHITHRE 45 CHITHRE 45 CHITHRE 45 CHITHRE 46 CHITHRE 47 CHITHRE 47 CHITHRE 48 CHITHRE 48 CHITHRE 48 CHITHRE 48 CHITHRE 49 CHITHRE 50 CHITHRE 51 CHITHRE 51 CHITHRE 52 CHITHRE 53 CHITHRE 53 CHITHRE 54 CHITHRE 55 CHITHRE 55 CHITHRE 56 CHITHRE 57 CHIT					41
FUR FACH VIRHATIONAL LEVEL. N (IM. P) . M = 1 - PV (IM. P) . M = 1 - PV (IM. P) . M = 1 - PV (IM. P) = J[PULF MOMENTS FOR VIRRATIONAL TRANSITIONS N TO M CHITHRE 48 (IN DEBYE) CHITHRE 49 (HITHRE 49 (HITHRE 49 (HITHRE 50 (HITHRE 51 (HITHRE 51 (HITHRE 52 (HITHRE 53 (HITHRE 53 (HITHRE 53 (HITHRE 53 (HITHRE 54 (HITHRE 55 (HITHRE 55)		E.C. T. ST. C. T. ST. T	- 1.	CHITHRE	-
CHITHRE 45				CHITHPE	
CHITHE 45	FUR FACH VIRH	PATIONAL LEVEL. N		CHITHRE	44
### CHITHE 47 ###################################	, , , , ,			CHITHRE	45
CHITHRE 47	(1 (M.);) . Male!!	IV	(5E15.81	CHITHPE	46
CHITHRE 49				CHITHHE	47
CHITHRE 49	11(M.H) = J[P(I	ILE MOMENTS FOR VINRATTO	NAL TRANSITIONS N TO M	CHITHRE	48
####(L) • L=1•4V (5E15.8) CHITHRE 51 CHITHRE 52 CHITHRE 53 CHITHRE 53 CHITHRE 53 CHITHRE 54 CHITHRE 55 CHITHRE 55 CHITHRE 55 CHITHRE 55 CHITHRE 55 CHITHRE 55 CHITHRE 56 CHITHRE 56 CHITHRE 57 CHITHRE 57 CHITHRE 57				CHITHRE	49
FWHI(L): L=1:4V (5E15:8) CHITHPE 52 CHITHPE 53 LINEUIDTHS (IN RECIPROCAL CH) CHITHRE 54 L=1: MOTATIONAL CHITHRE 55 L=2: U TO 1 VIBRATIONAL CHITHRE 56 L=3: U TO 2 VIBRATIONAL CHITHRE 57				CHITHRE	50
CHITHRE 53				• -	
LINEWIDTHS (IN RECIPROCAL CH) ===	FWHH(L) . L=1.	VV	(5815.8)		
L=1+ HUTATIONAL CHITHRE 55 L=2+ U TO 1 VIBHATIONAL CHITHRE 56 L=3+ U TO 2 VIBRATIONAL CHITHRE 57					
L=2. U TO] VIERATIONAL CHITHRE 56 L=3. U TO 2 VIERATIONAL CHITHRE 57	EINEMINTHS (1	N RECIPROCAL CHI			
L=3. U T.) 2 VIERATIONAL CHITHRE 57					

ETC. CHITHRE 58	L=3. U T				· ·
		ETC.		CHITHRE	58

```
11/22/78 11.36.27
                      0PT=2 UU
                                                           FTN 4.6+433H
                                                                                   CHITHRE
                                                                                                59
                                                                                   CHITHRE
                                                                                                60
                                                                        (2E15.8)
                                                                                   CHITHRE
       TEPP, 45122
                                                                                                61
                                                                                   CHITHRE
                                                                                                62
       TEMP = TEMPERATURE OF THE MODEL SYSTEM (NELVIN)
                                                                                   CHITHRE
                                                                                                63
       MSIZE - SIZE OF THE INTERVAL ABOUT THE INPUTTED PUMP FREQUENCIES
                                                                                   CHITHRE
                                                                                                64
                INSIDE OF WHICH THE PROGRAM WILL DETECT RESONANCES: WHEN CHITHRE IPOINT EO 1. WSIZE = WA. WHICH IS THE STEP SIZE WITH WHICH CHITHRE
                                                                                                65
                                                                                                66
                THE FREQUENCY HANGE FROM WO TO WP IS SCANNED (1/CM)
                                                                                   CHITHRE
                                                                                                67
С
                                                                                   CHITHRE
                                                                                                68
                                                                                   CHITHRE
                                                                                                69
                                                                        (215)
                                                                                   CHITHRE
                                                                                                70
       IMMITE, INVINT
                                                                                   CHITHRE
                                                                                                71
       IF INRITE EQ 1. PRINT OUT INDIVIDUAL EXCITATION PATH CONTRIBUTIONS CHITHRE
                                                                                                72
       IF IWRITE EU 2. CALCULATE ONLY THE CONTRIBUTION FROM THE
                                                                                   CHITHRE
                                                                                                73
                         VA=0. VB=3. VC=2. VD=1 PATH
                                                                                   CHITHRE
       IF IPUINT EQ 1, PROGRAM CALCULATES RESULTS FOR FREQUENCY TRIPLING
                                                                                   CHITHRE
                                                                                                75
                         FOR PUMP FREQUENCIES KANGING FROM WO TO WP WITH A
                                                                                   CHITHRE
                         STEP SIZE OF WH
                                                                                   CHITHRE
                                                                                   CHITHRE
                                                                                                78
                                                                                   CHITHRE
                                                                                                74
                                                                        (3E15.8)
                                                                                   CHITHRE
       WM + 4(1 + WH
                                                                                                80
                                                                                   CHITHRE
                                                                                                H1
       THESE AME PUMP FREQUENCIES (IN RECIPROCAL CM) ANY NUMBER OF SETS OF PUMP FREQUENCIES MAY BE INPUTTED
                                                                                   CHITHRE
                                                                                                82
                                                                                   CHITHRE
                                                                                                83
       THE PROGRAM TERMINATES WHEN THE PUMP FREQUENCIES ARE ALL ZERO
                                                                                   CHITHRE
                                                                                                84
       THESE HECUME WHAX. WHIN. AND WSIZE WHEN IPOINT EQ 1
                                                                                   CHITHRE
                                                                                                85
                                                                                   CHITHRE
                                                                                                86
                                                                                   CHITHRE
       PEAL MODCH! MODSUMY . LANGDA (5)
                                                                                                H7
       HEAL MGE (J)
                                                                                   CHITHRE
                                                                                                AH
       CUMPLEX SUMV (6.6.6) +SUMJ+SUMK+FARCD (20) +CHI3+EAB+EAC+EAD
                                                                                   CHITHRE
                                                                                                49
                                                                                   CHITHRE
                                                                                                90
       CUMPLEX F (20+2)+SUML (2)
       CUMPLEX GLO.2). TUME
                                                                                   CHITHRE
                                                                                                91
       LIMENSION A(5) . BV (5.2) . DV (5.2) . HV (5.2) . ASCRIP(5)
                                                                                   CHITHRE
                                                                                                42
       DIMENSION 4(5.5) . FAHM (5) . G(5) . B(5) . D(5) . PR(20) . LABEL (8)
                                                                                                91
                                                                                   CHITHRE
       CUMMON/CFHEQ/ NA+NB+NC+ND+RA+RB+RC+RD+W1+W2+W3+K+W(2+5+50)+
                                                                                   CHITHRE
                                                                                                94
                                                                                                95
      EFAUCD (20) + LAB+EAC+EAD+WS [ZE+AE+DELTA
                                                                                   CHITHRE
       CUM 40N/CSUMO/MA+MB+MC+MD+SA+SB+SC+SD+F(20+2)+KN+CA(5+50)+CB(5+50)+
                                                                                   CHITHRE
                                                                                                96
                                                                                   CHITHRE
                                                                                                47
       CUMMON/LHINCOM/WE. #EXE. X (5.2.3)
                                                                                   CHITHRE
                                                                                                QH
       CUMMON/CTUMO/TA.TH.TC.TD.KM.G(6.2).INDEX
                                                                                   CHITHKE
                                                                                                49
                                                                                   CHITHRE
                                                                                               100
C 3
       ՈԷԾԱԾ
                                                                                   CHITHRE
                                                                                               101
( 3
       AMMAYS
      GUTOS
                                                                                   CHETHRE
                                                                                               102
(. >
                                                                                   CHITHRE
                                                                                               103
C
Ċ
       READ IN DATA
                                                                                   CHITHRE
                                                                                               104
                                                                                   CHITHRE
                                                                                               105
       READ (5.101) (LABEL ([) . I=1.8)
                                                                                   CHITHRE
                                                                                               106
                                                                                   CHITHRE
                                                                                               107
  Int FURMATIOALUS
                                                                                   CHITHRE
                                                                                               108
      WHITE (HOLUE) LAHEL
  102 JUNNAT (INT. 1/2.5% + CALCULATION OF THE THIRD ORDER SUSCEPTIBILITY .
                                                                                   CHITHRE
                                                                                              109
                                                                                   CHITHRE
                                                                                              110
      =/+5x+841U+/)
                                                                                   CHITHRE
       Univertedictional
                                                                                              111
   ICIS) TAMMUT FAI
                                                                                   CHITHRE
                                                                                              112
                                                                                   CHITHRE
       WKITE (%+104) NV+NJ
                                                                                              113
   ING FURNATIZEDA . THIS CALCULATION USES . 15. VIBRATIONAL LEVELS AND .
                                                                                   CHITHRE
                                                                                              114
                                                                                   CHITHRE
                                                                                              115
      FID+ - RUTATIONAL LEVELS#)
```

```
74/74
CHITHPL
                      0PT=2 U0
                                                             FTN 4.6+433B
                                                                                    11/22/78 11.36.27
      PEAD ($.105) WE -WEXE - WEYE - WEZE
                                                                                       CHITHPE
                                                                                                   116
 INC FURMAT (SELS.B)
                                                                                       CHITHRE
                                                                                                   117
      WHITE (A. 100)
                                                                                       CHITHRE
                                                                                                   118
 INA FURMAT ( / . 54. * VIBRATIONAL CONSTANTS: * . 6x . * WE * . 12x . * WEXE * . 11x . * WEYE *
                                                                                       CHITHDE
                                                                                                   114
    E. 11x . . AEZE . 12x . . (IN RECIPRUCAL CM) .)
                                                                                       CHITHRE
                                                                                                   120
     WHITE (6.147) WE . WEXE . WEYE . WEZE
                                                                                       CHITHRE
                                                                                                   151
 107 FURMAT (254.5E15.8)
                                                                                       CHITHOR
                                                                                                   122
     PEAD (5.100) BE. ALPHA . GAMMA . DE. HF TA
                                                                                       CHITHRE
                                                                                                   123
      WHITE (A. LUG)
                                                                                       CHITHRE
                                                                                                   174
 ING FUNGAT (/.54.*ROTATIONAL CONSTANTS:*,7x,*BE*.12x.*ALPHA*.10x.
                                                                                                   125
                                                                                       CHITHRE
    - GANHAD + 114. *DE + 12x + BETA + 12x + (IN RECIPROCAL CM) +)
                                                                                       CHITHRE
                                                                                                   126
     WRITE (0.107) BE. ALPHA. GAMMA. DE. HETA
                                                                                       CHITHUE
                                                                                                   127
     FEAD (5.10-) AE . DELTA
                                                                                       CHITHRE
                                                                                                   128
     VHITE (A.ICL)
                                                                                       CHITHRE
                                                                                                   129
 121 FURNATIONAL CONSTANTS: 4.7X. AE*. 12X. DELTA*. 11X.
                                                                                       CHITHRE
                                                                                                   130
    E-(IN RECIPHOCAL CM)*)
                                                                                       CHITHRE
                                                                                                   131
     WHITE (6+14/) AE-DELTA
                                                                                       CHITHRE
                                                                                                   132
     PEAD (5.10-) OMEGAE. (MGE ([) . [=1.3))
IF (OMEGAE. LQ.O.) GO TO 200
                                                                                       CHITHRE
                                                                                                   133
                                                                                       CHITHRE
                                                                                                   134
     WRITE (6+125)
                                                                                       CHITHRE
                                                                                                   135
125 FURNAT (/+>A.*ELECTRUNIC STATE: +.9X. *ENERGY *.9X. *MGE(1) *.9X.
                                                                                       CHITHRE
                                                                                                   136
    E . MGE (2) . 7X. . MGE (3) .)
                                                                                       CHITHRE
                                                                                                   137
     WRITE ( .. 1 0 7) OMEGAE . (MGE ( 1 ) + I = 1 + 3 )
                                                                                       CHITHRE
                                                                                                   138
SUN CONTINUE
                                                                                       CHITHRE
                                                                                                   139
     WHITE (6.109)
                                                                                       CHITHRE
                                                                                                   140
100 FURMAT []H1+//+5x+#V[BRATIONAL TRANSITIUN MOMENTS (IN DEBYE)++/+
                                                                                       CHITHRE
                                                                                                   141
    F22X.80#.14K.41#.14X.#2#,14X.#3#.14X.#4#)
                                                                                       CHITHRE
                                                                                                   142
     DO 10 1:=1+HV
                                                                                       CHITHRE
                                                                                                   143
     READ (5.100) (U(M.N), M=1,NY)
                                                                                       CHITHRE
                                                                                                   144
     1-(4=1)14
                                                                                       CHITHRE
                                                                                                   145
     WRITE (6+110)NN+ (U(M+N)+M=1+NV)
                                                                                       CHITHRE
                                                                                                   146
110 FUNHAT (/+5A+15+5X+5E15.8)
                                                                                       CHITHRE
                                                                                                   147
 IN CUNTINUE
                                                                                       CHITHRE
                                                                                                   148
     #E40(5.102)(F#HM(L).L=1.NV)
                                                                                                   149
                                                                                       CHITHRE
     WRITE (6.111)
                                                                                       CHITHRE
                                                                                                   150
111 FURNAT (1HL.//.5X.*LINEWIDTHS:
                                             ROTATIONAL . 6x . * 0 TO 1 . 9x . * 0 TO
                                                                                       CHITHRE
                                                                                                   151
    =20,9x+00 TU 30.9x+0 TO 40.9x+0(IN RECIPROCAL CM)+)
                                                                                                   152
                                                                                       CHITHRE
     WRITE (A.112) (FWHM (L) .L=1.NV)
                                                                                       CHITHPE
                                                                                                   153
112 FURMAT (15A+4E15.A)
                                                                                       CHITHRE
                                                                                                   154
     CALCULATE INTERMEDIATE CONSTANTS FOR THE ENERGY LEVELS
                                                                                       CHITHRE
                                                                                                   155
     "IE = 2. "DE " (12. "HE " 2-ALPHA "WE) / (3. "WE " 2)
                                                                                       CHITHRE
                                                                                                   156
     DO 29 E=1+44
                                                                                                   157
                                                                                       CHITHRE
     v=L-1
                                                                                       CHITHRE
                                                                                                   158
     Y= V+0.5
                                                                                       CHITHRE
                                                                                                   159
     HIL) = df - ALPHA + Y + GAMMA + Y + # 2
                                                                                       CHITHRE
                                                                                                   140
     DIL) = OF +HC TA+Y
                                                                                       CHITHRE
                                                                                                  161
     CITTIENTOT-MEXEGYBOS-WEYERYOFS-WEZEGYOF4
                                                                                      CHITHRE
                                                                                                  162
     OS OT GO (.O.B. A.D. DELTA. FU.O.) GO TO 20
                                                                                      CHITHPE
                                                                                                  163
     A(L)=AF-DELTASY
                                                                                      CHITHRE
                                                                                                  164
     LAMPDA(L) =A(L)/B(L)
                                                                                      CHITHPE
                                                                                                  165
     ASCR[P(L)=A(L)-2.*);(L)-2.*P(L)*R(L)/A(L)
RY(L.+1)=B(L)+0(L)+R(L)*(1/LAMBDA(L)+2./LAMBDA(L)**2)
                                                                                      CHITHRE
                                                                                                  166
                                                                                      34HTIH2
                                                                                                  167
     H*([.2)=B(L)+H(L)*([L)*([L)*([VAMBDA(L)*2*/LAMBDA(L)**2)
D*([.1)=U(L)-H(L)*([VAMBDA(L)**3*4./LAMBDA(L)**4)
D*([.2)=U(L)+H(L)*([VAMBDA(L)**3*4./LAMBDA(L)**4)
                                                                                      CHITHRE
                                                                                                  144
                                                                                      CHITHDE
                                                                                                  1-9
                                                                                      CHITHRE
                                                                                                  170
     HV (L. 1) =HL-H(L) 4 (2./LAMHDA(L) 405+29./LAMBDA(L) 446)
                                                                                      CHITHPE
                                                                                                  171
     (1) #48 (L) # (2. /LAMBDA(L) #45 + 20. /LAMBDA(L) #46)
                                                                                      CHITHPE
                                                                                                  172
```

AD-A080 810

NORTHROP RESEARCH AND TECHNOLOGY CENTER PALOS VERDES --ETC F/G 20/5
INVESTIGATION OF EFFICIENT CO LASER FREQUENCY TRIPLING. (U)
SEP 79 H KOMINE, E A STAPPAERTS, A S GERVER
F29601-78-C-0068
NRTC79-13R

AFWL-TR-79-71

NL

END
NATION
AFWL
3 80

```
11/22/78 11.36.27
             14/14
                     0PT=2 UU
                                                         FIN 4.6+433H
 CHITHHE
                                                                                CHITHRE
                                                                                           173
   20 CUNTINUE
      CALCULATE <x**1> WHEN INCLUDING AN ELECTRONIC STATE
                                                                                CHITHRE
c
                                                                                           174
                                                                                CHITHRE
                                                                                           175
      IT (OMEGAL-NE.O.) CALL LMENTS
                                                                                CHITHRE
                                                                                           170
C
                                                                                CHITHRE
                                                                                           177
      NJF=NJ+2
      TTUP IS THE NUMBER OF OMEGA VALUES IN THE CALCULATION
                                                                                CHITHRE
                                                                                           178
C
      110P=2
                                                                                CHITHRE
                                                                                           179
                                                                                CHITHRE
      IF (AF .EQ. 0 .. AND .DELTA.EQ. 0.) ITOP=1
                                                                                           1 40
      110 200 J=1+NJH
                                                                                CHITHRE
                                                                                           lai
      IT (AE .EG. U. . AMI) DEL TA . EQ. O. ) GO TO 400
                                                                                CHITHRE
                                                                                           142
                                                                                CHITHHE
                                                                                           183
C
      CALCULATE THE PEDUCED MATRIA ELEMENTS FOR LAMBDA ME 0. RS([.K.J)
                                                                                CHITHRE
                                                                                           144
            I = 1 FOR OMEGAN OF 1/2
                                                                                CHITHRE
                                                                                           185
c
             . 2 FOR UNEGAN OF 3/2
                                                                                CHITHRE
                                                                                           186
            K = I FOH RX LT RY
                                                                                CHITHRE
                                                                                           187
C
                & FOH RX EU RY
                                                                                CHITHRE
                                                                                           188
C
                J FON AX GE RY
                                                                                CHITHRE
                                                                                           189
С
                                                                                           140
            J = THE INDEX FOR X-ST ROTATIONAL LEVEL
                                                                                CHITHRE
С
                                                                                CHITHHE
                                                                                           191
                                                                                CHITHRE
                                                                                           192
      P=ZaJ-1
                                                                                CHITHRE
                                                                                           193
      4=H/2.
                                                                               CHITHRE
                                                                                           194
      R>(1,1,J)=50KI(((R+1.)==2-0.5=0.5)/(R+1.))
                                                                                CHITHRE
                                                                                           145
      IF (R.EQ.0.5) 60 TO 340
      R5(2.1.J)=50Rf(((R+1.)++2-1.5+1.5)/(R+1.))
                                                                               CHITHRE
                                                                                           196
                                                                                CHITHRE
                                                                                           197
      GU TO 350
                                                                                           198
  340 P5(2.1.J)=0.
                                                                               CHITHRE
  350 H5(1.2.J)=50RT(0.5+0.5+(2.4R+1.)/(R+(R+1.)))
                                                                               CHITHRE
                                                                                           199
                                                                                CHITHRE
      P5(2,2,J)=50RT(1.5*1.5*(2.*K+1.)/(R*(R+1.)))
                                                                                           200
                                                                               CHITHRE
      R>(1.3.J)=5uRT((R*R*0.5*0.5)/R)
                                                                                           201
      IF (R.LE.1.5) GO TO 390
                                                                               CHITHRE
                                                                                           202
      R5(2.3.J)=5QRT((R*R-1.5*1.5)/R)
                                                                                CHITHRE
                                                                                           203
      60 TO 400
                                                                                CHITHRE
                                                                                           204
  340 R5(2,3,J)=U.
                                                                                CHITHRE
                                                                                           205
                                                                                CHITHRE
                                                                                           206
  400 CUNTINHE
                                                                                CHITHRE
                                                                                           207
                                                                                CHITHRE
      DU 500 N=1+NV
                                                                                           208
      IT LAE .FU. U. . AND .DELTA.EU. U.) GO TO 300
                                                                               CHITHRE
                                                                                           209
                                                                                CHITHRE
                                                                                           210
c
      CONSTRUCT THE INTERMEDIATE COUPLING COEFFICIENTS FOR LAMBDA NE O
                                                                               CHITHRE
                                                                                           211
                                                                                CHITHRE
                                                                                           212
      x=50RT (LAMBUA (N) + (LAMBUA (N) -4.) +4.+ (R+0.5) ++2)
                                                                                CHITHRE
                                                                                           213
      CA(11,J)=544f((x-2.+LAMBDA(N))/(2.*x))
                                                                                CHITHRE
                                                                                           214
      IF (J.EQ.1) GO TO 295
                                                                                CHITHRE
                                                                                           215
      CH(N+J)=54KT((x+2.-LAMBDA(N))/(2.*X))
                                                                                CHITHRE
                                                                                           216
                                                                               CHITHRE
      GU TO 300
                                                                                           217
  502 Cut 1. 1)=0.
                                                                                CHITHRE
                                                                                           218
                                                                               CHITHRE
                                                                                           219
  300 CUNTINUE
                                                                               CHITHRE
                                                                                           220
c
                                                                                CHITHRE
                                                                                           221
      00 400 I=1+170P
                                                                                CHITHPE
¢
                                                                                           222
                                                                                CHITHRE
                                                                                           223
      CALCULATE THE ENERGY LEVELS
                                                                                CHITHRE
                                                                                           224
                                                                                           225
                                                                               CHITHRE
      IF (AE. HU.U. AND DELTA . EQ. O.) GO TO 205
      *(1.01.) = G(N) - D(N) + (-1.)**[*ASCRIP(N)/2. +
                                                                               CHITHRE
                                                                                           226
     EHV (1,1) * (H+U.5) **2 - DV (N+1) * (H+U.5) **4 + HV (N+1) * (R+U.5) **6
                                                                               CHITHRE
                                                                                           227
      60 TO 500
                                                                               CHITHRE
                                                                                           228
  205 H=J-1
                                                                               CHITHRE
                                                                                           229
```

```
11/22/78 11.36.27
  CHITHRE
                                        0PT=2 U0
                                                                                                                FTN 4.6+433B
             y(I_{\bullet}(I_{\bullet})) = G(A) + y(N) + R + (R+1_{\bullet}) - n(N) + (R+(R+1_{\bullet})) + 2 +
                                                                                                                                                             CHITHOF
                                                                                                                                                                                   230
           트워틴 ( 유 + ( 유 + 1 + ) ) # # 3
                                                                                                                                                             CHITHPE
                                                                                                                                                                                   231
    Son CURITINUE
                                                                                                                                                             CHITHRE
                                                                                                                                                                                   232
                                                                                                                                                             CHITHPE
                                                                                                                                                                                   233
             PEAD (5.105) TEMP+WSTZE
                                                                                                                                                             CHITHRE
                                                                                                                                                                                   234
             WHITE (A-113) TEMP
                                                                                                                                                             CHITHRE
                                                                                                                                                                                   235
     113 FURHAT (//-SX-@TEMPERATURE FOR THIS CALCULATION IS *-E15.8-# KELV*) CHITHRE
                                                                                                                                                                                   236
             HEADIS. 103) INPLIE- IPOINT
                                                                                                                                                             CHITHRE
                                                                                                                                                                                   277
             IL OL OD TO STENE STEER THE STEER ST
                                                                                                                                                             CHITHRE
                                                                                                                                                                                   218
              IF COMEGAE . NE . O . ) GO TO 21
                                                                                                                                                             CHITHRE
                                                                                                                                                                                   239
             WHITE (6.124)
                                                                                                                                                             CHITHRE
                                                                                                                                                                                   246
     122 FURNAT (//+5x++THE RESUNANCE APPROXIMATION HAS REEN APPLIED IN THIS CHITHRE
                                                                                                                                                                                   241
           E CALCULATION* . //)
                                                                                                                                                             CHITHRE
                                                                                                                                                                                   242
             CALCULATE THE PARTITION FUNCTION
                                                                                                                                                             CHITHRE
                                                                                                                                                                                   243
      21 [F(AE.EQ.U..AND.DELTA.EQ.O.) GO TO 22
ESH[FT=ASCH[P(])+4.*BV(]+2)-16.*DV(]+2)+64.*HV(]+2)-BV(]+1)+
                                                                                                                                                             CHITHRE
                                                                                                                                                                                  244
                                                                                                                                                             CHITHRE
                                                                                                                                                                                   245
           304(1+1)-HA(1+1)
                                                                                                                                                             CHITHRE
                                                                                                                                                                                   246
           Q=2. + (1.+EXP(-ESHIFT/(6.9503E-01*TEMP)))*6.9503E-01*TEMP/8(1)*
EEXP(-15.*8(1)/(6.9503E-01*TEMP*4.))
                                                                                                                                                             CHITHRE
                                                                                                                                                                                   247
                                                                                                                                                             CHITHPE
                                                                                                                                                                                   248
                                                                                                                                                             CHITHRE
                                                                                                                                                                                   249
             60 TO 23
      22 CUNTINUE
                                                                                                                                                             CHITHRE
                                                                                                                                                                                   250
                                                                                                                                                                                   251
             Q=6.9503E-U1*TEMP/9(1)
                                                                                                                                                             CHITHRE
                                                                                                                                                             CHITHRE
      23 CUNTINHE
                                                                                                                                                                                   252
             PLAD IN PP. NO. WRI TERMINATE THE PROGRAM IF THEY ARE ALL ZERO
                                                                                                                                                             CHITHRE
                                                                                                                                                                                   253
                                                                                                                                                                                   254
                                                                                                                                                             CHITHRE
      25 PEAN (5.105) WP. WQ. WR
             IF (WP.EG.U.AND.WG.EU.O.AND.WR.EG.O) GO TO 1000 /
                                                                                                                                                                                  255
                                                                                                                                                             CHITHRE
                                                                                                                                                                                  256
             NUM=0
                                                                                                                                                             CHITHRE
                                                                                                                                                                                  257
                                                                                                                                                             CHITHRE
             IF (IPOINT . NE . 1) GO TO 55
                                                                                                                                                                                  258
             YMAX = WP
                                                                                                                                                             CHITHRE
                                                                                                                                                                                   259
                                                                                                                                                             CHITHRE
             UW = WINW
                                                                                                                                                             CHITHRE
             WSI7E = ABS(WH)
                                                                                                                                                                                   260
             JF(WMAX.LT.WMIN) WSIZE =- WSIZE
                                                                                                                                                             CHITHRE
                                                                                                                                                                                   261
             MUM= (WHAX-MMIN) /WSIZE
                                                                                                                                                             CHITHRE
                                                                                                                                                                                  242
      SS CONTINUE
                                                                                                                                                             CHITHRE
                                                                                                                                                                                  263
             WHITE (6+140) WSTZE
                                                                                                                                                             CHITHRE
                                                                                                                                                                                  244
     120 FURMAT (//+5x+*RESUNANCES WITHIN A MANGE OF *-E15.8+* /CM CENTERED
                                                                                                                                                             CHITHRE
                                                                                                                                                                                  265
           EABOUT FACH OF THE PUMP FREQUENCIES ARE INDICATED BY THE PROGRAM*)
                                                                                                                                                             CHITHRE
                                                                                                                                                                                  244
                                                                                                                                                             CHITHRE
                                                                                                                                                                                   267
             MUM=NUM+1
             DU 2000 ITER=1.NUM
                                                                                                                                                             CHITHRE
                                                                                                                                                                                   268
             IF ([POINT.NE.1) GO TO 65
                                                                                                                                                             CHITHRE
                                                                                                                                                                                  269
                                                                                                                                                                                  270
             WHEWHIN+ (ITER-1) #WSIZE
                                                                                                                                                             CHITHRE
                                                                                                                                                             CHITHRE
                                                                                                                                                                                  271
             W()=WP
                                                                                                                                                             CHITHRE
                                                                                                                                                                                  212
             WHEND
      AS WRITE (6.114) WP. WQ. WR
                                                                                                                                                             CHITHPE
                                                                                                                                                                                  273
    114 FURNAT (////.54. THE PUMP FREQUENCIES ARE*+3(5X+E15.8))
                                                                                                                                                                                   274
                                                                                                                                                             CHITHRE
                                                                                                                                                             CHITHRE
                                                                                                                                                                                  275
C
             PERMUTE THE PUMP FREQUENCIES
                                                                                                                                                             CHITHPE
C
                                                                                                                                                                                  276
                                                                                                                                                                                  217
С
                                                                                                                                                             CHITHRE
                                                                                                                                                                                  274
             HER IS THE MUMBER OF FREQUENCY PERMUTATIONS
                                                                                                                                                             CHITHRE
             MFPsi
                                                                                                                                                                                  279
                                                                                                                                                             CHITHRE
             IF (UP .: IE . WU) NEP=NFP+1
                                                                                                                                                             CHITHRE
                                                                                                                                                                                  240
             IF TWP . NE . WIC) NEP=NEP+1
                                                                                                                                                             CHITHRE
                                                                                                                                                                                  241
             IF (WO.NE.WK) NEP=MEP+1
                                                                                                                                                             CHITHRE
                                                                                                                                                                                  242
             IN THEP.GT-3) NEPENEP+2
PM 15 THE HUMMER OF TIMES EACH PERMUTATION APPEAPS
                                                                                                                                                                                  2×3
                                                                                                                                                             CHI THPF
                                                                                                                                                                                  284
                                                                                                                                                            CHITHRE
             PHER /NEP
                                                                                                                                                            CHITHPE
                                                                                                                                                                                  245
              IF COMPLETE . NE . 11 GO TO 45
                                                                                                                                                            CHI THRE
```

```
CHITHPL
              74/14
                     11PT=2 UU
                                                            FTN 4.6.4338
                                                                                  11/22/78 11.36.27
                                                                                    CHITHRE
       WHITE (0.114)
                                                                                                2H7
  119 FURNAT ( / / - 5x - + SINGLE PATH CONTRIBUTIONS TO THE SUSCEPTIBLITY )
                                                                                    CHITHRE
                                                                                                288
      WHITE (6+11/)
                                                                                    CHITHRE
                                                                                                249
  117 FURNAT (/ - <5x, = VB - 13x - VC - 13x - VD - 13x - RECH 13 - 18x - MCH 13 - 18X
                                                                                    CHITHRE
                                                                                                240
                                                                                    CHITHRE
                                                                                                241
     = 0 AUCH[3* ./]
                                                                                                242
                                                                                    CHITHRE
C
       HEGIN THE SUM OVER VIBRATIONAL LEVELS
                                                                                    CHITHRE
                                                                                                293
c
                                                                                    CHITHRE
                                                                                                294
C
                                                                                    CHITHRE
   45 CH13=(0.+U.)
                                                                                                295
       IF (OMEGAL.NE.O.) GO TO 7
                                                                                    CHITHRE
                                                                                                296
      IF (19RTTE - NE - 2) GO TO 7
PICK OUT SINGLE PATH FOR RESONANCE APPROXIMATION
                                                                                    CHITHRE
                                                                                                247
                                                                                    CHITHRE
                                                                                                298
C
                                                                                    CHI THRE
                                                                                                299
      hidL0=4
                                                                                    CHITHRE
                                                                                                300
      Noh I =4
      NCLU=3
                                                                                    CHITHRE
                                                                                                301
      NCHT=3
                                                                                    CHITHRE
                                                                                                305
      HULD=2
                                                                                    CHITHRE
                                                                                                303
      HUH [=2
                                                                                    CHITHHE
                                                                                                304
      60 TO 6
                                                                                    CHITHRE
                                                                                                305
                                                                                    CHITHRE
                                                                                                306
С
                                                                                    CHITHRE
                                                                                                307
    7 NOLO=1
                                                                                    CHITHRE
                                                                                                308
      HIGH I = NY
      NiLLO=1
                                                                                    CHITHRE
                                                                                                309
                                                                                                310
                                                                                    CHITHRE
      HUH J = NV
      NULO=1
                                                                                    CHITHRE
                                                                                                311
                                                                                    CHITHRE
                                                                                                312
      NUHIENV
    A CUNTINUE
                                                                                    CHITHRE
                                                                                                313
                                                                                                314
315
      DO 40 MP=HAFO+WBHI
                                                                                    CHITHRE
       IF COMECAE.EQ. 0) GO TO 39
                                                                                    CHITHRE
      1F (NB.EQ.-1) 60 TO 19
1F (NB.EQ.4) 60 TO 29
                                                                                    CHITHRE
                                                                                                316
                                                                                    CHITHRE
                                                                                                317
                                                                                    CHITHRE
                                                                                                318
      60 to 39
   14 HCHT=NY+1
                                                                                    CHITHRE
                                                                                                319
                                                                                                320
      NOH (=NV+)
                                                                                    CHITHRE
                                                                                    CHITHRE
      60 TO 39
                                                                                                321
  .24 NUMI =NV
                                                                                    CHITHRE
                                                                                                322
      MUH I = MV
                                                                                    CHITHRE
                                                                                                353
   34 CONTINUE
                                                                                    CHITHRE
                                                                                                324
      DO 70 NC=NCLO+NCHI
                                                                                    CHITHRE
                                                                                                325
      INCH. DJUNEUN OR UC
                                                                                    CHITHRE
                                                                                               326
      IT (NC. FQ. (NV+1) . AND . ND . EU. (NV+1)) GO TO BO
                                                                                    CHITHRE
                                                                                               327
                                                                                    CHITHRE
                                                                                                328
      SUMV (NE+NC+ND) = (0..0.)
                                                                                    CHITHRE
                                                                                                329
C
      HEGIN THE SUM OVER FREQUENCY PERMUTATIONS
                                                                                    CHITHRE
                                                                                               330
                                                                                    CHITHRE
                                                                                               331
      DU 90 N=1+NFP
                                                                                    CHITHRE
                                                                                               332
      GU TO (1+2+3+4+5+6)+N
                                                                                    CHITHRE
                                                                                               333
    1 W1=WP
                                                                                    CHITHRE
                                                                                               334
      4C=43
                                                                                    CHITHRE
                                                                                                335
      4 J=WR
                                                                                    CHITHRE
                                                                                                336
      6U TO 30
                                                                                    CHITHRE
                                                                                               337
    2 MT=41
                                                                                    CHITHRE
                                                                                                338
                                                                                                339
       46=44
                                                                                    CHITHRE
      W t=HP
                                                                                    CHITHRE
                                                                                                340
      ลับ 10 30
                                                                                    CHITHRE
                                                                                                341
    7 111= 12
                                                                                    CHITHRE
                                                                                               342
      46247
                                                                                    CHITHHE
                                                                                               343
```

```
11/22/78 11.36.27
· CHITHRE
              74/74
                      00 =19n
                                                          FTN 4.6+4338
                                                                                  CHITHRE
       MB=MO
                                                                                             344
       GU TO JO
                                                                                  CHITHHE
                                                                                             345
     4 WI=HP
                                                                                  CHITHPE
                                                                                             346
       WC=WR
                                                                                  CHITHHE
                                                                                             347
       N7=HO
                                                                                  CHITHRE
                                                                                             348
       60 TO 30
                                                                                  CHITHRE
                                                                                              344
     S WIEVO
                                                                                  CHITHRE
                                                                                             350
                                                                                  CHITHRE
                                                                                             35]
       コピニHP
       quate w
                                                                                  CHITHRE
                                                                                             352
      GU TO 30
                                                                                  CHITHRE
                                                                                             353
     K HI=WR
                                                                                             354
                                                                                  CHITHRE
                                                                                             355
      W2=M0
                                                                                  CHITHRE
                                                                                  CHITHRE
                                                                                             356
       w3≠w0
                                                                                             357
       60 10 30
                                                                                  CHITHRE
                                                                                             35A
                                                                                  CHITHRE
    30 MA=1
                                                                                  CHITHRE
                                                                                             359
       CALCULATE IMAGINARY HALFWIDTHS
С
                                                                                  CHITHRE
                                                                                             360
       EAD= (0.+0.5) *FWHM (NB)
                                                                                  CHITHRE
                                                                                             361
       EAC=(0..0.5) *FWHM(NC)
                                                                                  CHITHRE
                                                                                             362
       FAD=(0.+0.5) *FWHM(NU)
       IF (NC.EG. (NV-1).OR.NO.EG. (NV+1)) GO TO 3000 TAKE THE PRODUCT OF THE DIPOLE MATRIX ELEMENTS
                                                                                  CHITHRE
                                                                                             363
                                                                                  CHITHRE
                                                                                             364
С
       PV=11(NA+NB) +U(NB+NC) +U(NC+ND) +11(ND+NA)
                                                                                  CHITHRE
                                                                                             365
C
       REGIN THE SUM OVER RUTATIONAL LEVELS
                                                                                  CHITHRE
                                                                                             366
       SUMJ=(0..0.)
                                                                                  CHITHRE
                                                                                             367
       IF (AE.EQ.U..AND.DELTA.EQ.O.) GO TO 1060
                                                                                  CHITHRE
                                                                                             348
       ASSIGN VALUES OF VIBRATIONAL LEVEL INDICES TO BE PASSED TO SUMO
C
                                                                                  CHITHRE
                                                                                             369
       MA=NA
                                                                                  CHITHRE
                                                                                             370
       MHENB
                                                                                  CHITHRE
                                                                                             371
       HC=1C
                                                                                  CHITHRE
                                                                                             372
      MUTNO
                                                                                  CHITHRE
                                                                                             373
       DO 1050 J=1.NJ
                                                                                  CHITHRE
                                                                                             374
       R IS THE ACTUAL ROTATIONAL QUANTUM NUMBER
                                                                                  CHITHRE
                                                                                             375
C
                                                                                  CHITHRE
                                                                                             376
       p=2+J-1
      P=#/2.
                                                                                  CHITHRE
                                                                                             377
       SAZR
                                                                                  CHITHPE
                                                                                             37R
      00 1035 K=1.14
                                                                                  CHITHHE
                                                                                             379
      PK (K) =0 .
                                                                                  CHITHRE
                                                                                             380
      F(K.1)=(0.+0.)
                                                                                  CHITHRE
                                                                                             JAI
 1075 F(K.2)=(0..0.)
                                                                                  CHITHRE
                                                                                             SAE
                                                                                  CHITHPE
                                                                                             347
С
С
С
       SUM OVER RUTATIONAL LEVELS BY PATHS
                                                                                  CHITHRE
                                                                                             344
                                                                                             395
                                                                                  CHITHRE
                                                                                  CHITHRE
                                                                                             386
       It (p-1.5) 1015-1012-1011
                                                                                             3A 7
 1011 KH=1
                                                                                  CHITHRE
      SHEP-1.
                                                                                  CHITHRE
                                                                                             388
      SC=0-2.
                                                                                  CHITHRE
                                                                                             TAU
                                                                                             390
       50=0-1.
                                                                                  CHITHRE
      PH(1)=2./(15.*(2.*R-1.))
                                                                                  CHITHPE
                                                                                             391
                                                                                             302
                                                                                  CHITHRE
      CALL SHMO
 1012 KN=>
                                                                                  CHITHPE
                                                                                             393
      54=R-1.
                                                                                  CHITHRE
                                                                                             394
       SCER
                                                                                  CHITHPE
                                                                                             305
       SUSP-1
                                                                                  CHITHRE
                                                                                             396
       FK(2)=(4.*K*R+1.)/(15.*K*(2.*R-1.)*(2.*K+1.))
                                                                                  CHITHRE
                                                                                             397
       CALL SUMO
                                                                                  CHITHRE
                                                                                             344
       KN= 1
                                                                                  CHITHPE
                                                                                             399
       SHEU+1.
                                                                                  CHITHPE
                                                                                             400
```

```
74//4
                    0PT=2 UU
                                                       FTN 4.6+433H
                                                                             11/22/78 11.36.27
CHITHPL
                                                                               CHITHRE
                                                                                          401
     CC*U
     SU#R-1.
                                                                               CHITHRE
                                                                                          402
     PK(3)=2./(15.4(2.48+1.))
                                                                               CHITHRE
                                                                                          403
                                                                               CHITHRE
     CALL SUMU
                                                                                          404
                                                                               CHITHRE
                                                                                          405
     *14=4
                                                                               CHITHRE
                                                                                          406
     50=F-1.
     SC≉R
                                                                               CHITHRE
                                                                                          407
                                                                               CHITHRE
                                                                                          408
     SD=P+1.
                                                                               CHITHRE
                                                                                          409
     hk(*)=hk(?)
                                                                               CHITHRE
                                                                                          410
     CALL SUMO
                                                                               CHITHRE
                                                                                          411
     K142/
                                                                               CHITHRE
     SHER
                                                                                          412
     SC=P
                                                                               CHITHRE
                                                                                          413
     Su=q-1.
                                                                               CHITHRE
                                                                                          414
     PR(7)=(H-1.)/(15.*R*(2.*R+1.))
                                                                               CHITHRE
                                                                                          415
                                                                               CHITHRE
                                                                                          416
     CALL SUMO
                                                                               CHITHRE
                                                                                          417
     KN=4
     SHER
                                                                               CHITHRE
                                                                                          418
     SC=H-1.
                                                                               CHITHRE
                                                                               CHITHRE
                                                                                          420
     SUZD
                                                                               CHITHRE
     PK (4) =PK (7)
                                                                                          421
                                                                               CHITHRE
                                                                                          422
     CALL SUMO
                                                                               CHITHRE
                                                                                          423
     Ki4=11
                                                                               CHITHRE
                                                                                          424
     SU=#-1.
                                                                               CHITHRE
                                                                                          425
     SC=R
     5U≖Ω
                                                                               CHITHRE
                                                                                          426
                                                                               CHITHRE
                                                                                          427
     PK(11)=PK(7)
                                                                                          428
                                                                               CHITHRE
     CALL SUMU
                                                                               CHITHRE
                                                                                          429
     K11=13
                                                                               CHITHRE
                                                                                          430
     58=W-1.
                                                                               CHITHRE
                                                                                          431
     SU=N-1.
                                                                               CHITHRE
                                                                                          432
     SU=4-1.
     PK(13)=(K+1.)/(15.0R*(2.0H-1.))
                                                                               CHITHRE
                                                                                          433
                                                                               CHITHRE
     CALL SUMO
                                                                                          434
     K#=15
                                                                               CHITHRE
                                                                                          435
     50=R
                                                                               CHITHRE
                                                                                          436
     SC=R-1.
                                                                               CHITHRE
                                                                                          437
     SU#P-1.
                                                                               CHITHRE
                                                                                          438
     PR(15)=SGR[((4+1.)+(R-1.)/(R+R+(2.+R+1.)+(2.+R-1.)))/15.
                                                                               CHITHRE
                                                                                          439
                                                                               CHITHRE
                                                                                          440
     CALL SUMU
                                                                               CHITHRE
                                                                                          441
     * ti=1 /
                                                                               CHITHRE
                                                                                          442
     Su=H-1.
     SC=R-1.
                                                                               CHITHRE
                                                                                          443
                                                                               CHITHRE
                                                                                          444
     2D±K
                                                                               CHITHRE
                                                                                          445
     PK (17) =PK (15)
                                                                               CHITHRE
                                                                                          446
     CALL SUMU
                                                                               CHITHRE
                                                                                          447
1015 KN=5
                                                                               CHITHRE
                                                                                          448
     58=R+1.
                                                                               CHITHRE
                                                                                          449
     56=17
                                                                               CHITHRE
                                                                                          450
     SU=P+1
     PH(5)=(4.***************(15.*(R*1.)*(2****1.)*(2*****3*))
                                                                               CHITHRE
                                                                                          451
                                                                               CHITHRE
                                                                                          452
     CALL SUMU
                                                                               CHITHRE
                                                                                          453
     KH=6
                                                                               CHITHRE
                                                                                          454
     SU=R+1.
                                                                                          455
                                                                               CHITHRE
     5C=H+2.
     SU=H+1.
                                                                               CHITHRE
                                                                                          456
     PK(6)=2./(15.*(2.*H+3.))
                                                                               CHITHRE
                                                                                          457
```

```
74/74
                      00 S=140
                                                         FTN 4.6+433B
 CHITHRE
                                                                              11/22/78 11.36.27
       CALL SUMO
                                                                                CHITHRE
                                                                                            45A
       KN#8
                                                                                 CHITHRE
                                                                                            459
       SHER
                                                                                 CHITHPE
                                                                                            460
       SCER
                                                                                 CHITHRE
                                                                                            461
       SU=9+1.
                                                                                 CHITHRE
                                                                                            462
       PH(A)=(R+2.)/(15.*(R+1.)*(2.*R+1.))
                                                                                CHITHHE
                                                                                            463
       CALL SHMO
                                                                                CHITHPE
                                                                                            464
       K14=10
                                                                                            445
                                                                                CHITHRE
       SUFR
                                                                                           466
                                                                                CHITHRE
       SC=0+1.
                                                                                CHITHRE
                                                                                            667
       5()=0
                                                                                CHITHPE
                                                                                           46A
       PR(10)=PR(8)
                                                                                           469
                                                                                CHITHPE
                                                                                CHITHRE
       CALL SUMU
                                                                                           470
       KN=15
                                                                                CHITHRE
                                                                                           471
       S8#R+1.
                                                                                CHITHRE
                                                                                           472
       SC#P
                                                                                           473
                                                                                CHITHRE
       SUZU
                                                                                CHITHRE
                                                                                           474
       PH(12)=PH(8)
                                                                                CHITHRE
                                                                                           475
       CALL SUMO
                                                                                CHITHRE
                                                                                           476
       KN=14
                                                                                CHITHRE
                                                                                           477
       50=1.
                                                                                CHITHRE
                                                                                           47A
       sC=H+1.
                                                                                CHITHRE
                                                                                           479
       SU=R+1.
                                                                                CHITHRE
                                                                                           440
       PH(14)=R/(15.0(R+1.)*(2.*R+3.))
                                                                                CHITHRE
                                                                                           4A [
       CALL SIJMO
                                                                                CHITHPE
                                                                                           482
       KN=16
                                                                                CHITHRE
                                                                                           483
       Sゼ≠₽
                                                                                CHITHRE
                                                                                           484
       SC=P+1.
                                                                                CHITHRE
                                                                                           445
       SU=R+1.
                                                                                CHITHRE
                                                                                           486
       PK(16)=$QKT(R*(R+2.)/((R+1.)*(R+1.)*(2.*R+1.)*(2.*R+3.)))/15.
                                                                                CHITHRE
                                                                                           487
       CALL SUMU
                                                                                CHITHRE
                                                                                           488
       KN=18
                                                                                CHITHPE
                                                                                           489
       58=2+1.
                                                                                CHITHRE
                                                                                           490
       SC=R+1.
                                                                                CHITHRE
                                                                                           491
       SUPP
                                                                                CHITHPE
                                                                                           402
       PK (18) =PK (16)
                                                                                CHITHRE
                                                                                           493
       CALL SIJMO
                                                                                CHITHRE
                                                                                           494
       Ku=19
                                                                                CHITHRE
                                                                                           495
      SHED
                                                                                CHITHRE
                                                                                           496
      SCED
                                                                                CHITHRE
                                                                                           497
       SD=B
                                                                                CHITHPE
                                                                                           40A
      PR(19)=(3.*H+D.3.*H-1.)/(15.*R*(R+1.)*(2.*R+1.))
                                                                                           499
                                                                                CHITHPE
      CALL SHMU
                                                                                CHITHRE
                                                                                           500
000
                                                                                CHITHRE
                                                                                           501
      HEGIN SUM UVED PATHS
                                                                                CHITHRE
                                                                                           502
                                                                                CHITHRE
                                                                                           503
      PH (12) =PH (8)
                                                                                CHITHRE
                                                                                           504
      DU 1040 K=1.19
                                                                                CHITHRE
                                                                                           505
      SUML (2)=(0..0.)
                                                                                CHITHRE
                                                                                           506
      SUML (1) = (0..0.)
                                                                                CHITHRE
                                                                                           507
      SUML (1) =SUML (1) +PR(K) *F(K+1)
                                                                                CHITHRE
                                                                                           50H
      IF (R.E0.0.3) GO TO 1040
                                                                                CHITHPE
                                                                                           509
      SUML (2) = SUML (2) + PR (K) *F (K+2)
                                                                                CHITHRE
                                                                                           510
 TOAR CONTINUE
                                                                                           511
512
                                                                                CHITHRE
      HK= (R+0.5) 402
                                                                                CHITHPE
      E=BV([.1)*KH-1)V([.1)*RH+*Z+HV([.1)*HV*03-HV([.1)*DV([.1)-HV([.1)
                                                                                CHITHRE
                                                                                           513
      D15=EAP(-E/(6.9503E-01*TEMP))/0
                                                                                CHITHHE
                                                                                           514
```

```
11/22/78 11.36.27
                                                       FTN 4.6+4338
            74/14
                    00 5=140
CHITHHE
                                                                              CHITHRE
                                                                                         515
      SUMJESUMU+SUML(1)*DIS
                                                                                         516
                                                                              CHITHRE
      11 (R.EQ. 0.5) 50 TO 1050
      E=BV(1,2)*HH-DV(1+2)*RR**2*HV(1.2)*RR**3*ASCR[P(1)-BV(1+1)+DV(1+1) CHITHRE
                                                                                         517
                                                                                         518
                                                                              CHITHRE
     =-HV (1+1)
                                                                                         519
      DIS=EXP(-L/(6.4503E-01*TEMP))/0
                                                                              CHITHRE
                                                                                         520
      210°(S) JMUC+UMIZ=LMUZ
                                                                                         521
1050 CUNTINUE
                                                                              CHITHRE
                                                                                         522
      Su 10 1111
                                                                              CHITHRE
                                                                                         523
 1040 CUNTINUE
                                                                              CHITHRE
                                                                                         524
      DO 20 7=1+H7
                                                                                         525
                                                                               CHITHRE
      R IS THE ACTUAL ROTATIONAL QUANTUM NUMBER
C
                                                                                         526
                                                                               CHITHRE
      ちょっして
                                                                                         527
                                                                               CHITHRE
      RAFR
                                                                                         528
                                                                               CHITHRE
      DU 35 K=1+0
                                                                               CHITHRE
                                                                                         529
      PK (K) =0.
                                                                               CHITHRE
                                                                                         530
   34 FAUCD (K) = (0..0.)
                                                                                         531
                                                                               CHITHRE
¢
                                                                               CHITHRE
                                                                                         5.32
      SUM OVER THE ROTATIONAL LEVELS BY PATHS
C
                                                                                         533
                                                                               CHITHRE
                                                                                         534
                                                                               CHITHRE
      IF (w-1.)15:12:11
                                                                                         515
                                                                               CHITHRE
   13 K=1
                                                                                         536
                                                                               CHITHRE
      PH=R-1.
                                                                               CHITHRE
                                                                                          537
      RC=R-2.
                                                                                         518
                                                                               CHITHRE
      RU=P-1.
                                                                                          539
                                                                               CHITHRE
      PH(1)=2.*H*(R-1.)/(15.*(2.*R-1.)*(2.*R+1.))
                                                                                          540
                                                                               CHITHRE
      CALL FREU
                                                                                         541
                                                                               CHITHRE
   12 K#6
                                                                                         542
                                                                               CHITHRE
      Post -1.
                                                                                         543
                                                                               CHITHRE
      としまり
                                                                                         544
                                                                               CHITHRE
      pu=p-1.
                                                                                          545
      PH(2)=R*(+.*R**2+1)/(15.*(2.*R-1.1*(2.*R+1.14*2)
                                                                               CHITHRE
                                                                                         546
                                                                               CHITHRE
      CALL FREU
                                                                                          547
                                                                               CHITHRE
      K=J
                                                                               CHITHRE
                                                                                          54A
      DH=Dal.
                                                                                          549
                                                                               CHITHRE
      BC=P
                                                                               CHI THRE
                                                                                          550
       ロシェリート
                                                                                          551
                                                                               CHITHRE
       FK(3)=2.4K4(R+1.)/(15.*(2.4R+1.)442)
                                                                                          552
                                                                               CHITHRE
      CALL FREU
                                                                               CHITHRE
                                                                                          553
      r =4
                                                                               CHITHRE
                                                                                          554
       HH=H-1.
                                                                               CHITHRE
                                                                                          555
       KÇ=K
                                                                               CHITHRE
                                                                                          556
       PU=R+1.
                                                                               CHETHRE
                                                                                          557
       PK(4)=2.4K*(R+1.1/(15.*(2.4K+1.)**2)
                                                                                          558
                                                                               CHITHRE
       CALL FREQ
                                                                               CHITHRE
                                                                                          559
    14 K=5
                                                                               CHITHRE
                                                                                          560
       HB=H+1.
                                                                               CHITHRE
                                                                                          561
       HC=h
                                                                               CHITHRE
                                                                                          562
       RD=4+1.
                                                                               CHITHRE
                                                                                          563
       PH(5)=(H+1.)+(4.+R++2+8.+R+5)/(15.+(2.+H+3.)+(2.+R+1.)++2)
                                                                               CHITHRE
                                                                                          564
       CALL FREU
                                                                               CHITHRE
                                                                                          565
       K =0
                                                                               CHITHRE
                                                                                          566
       40=H+1.
                                                                               CHITHRE
                                                                                          567
       KC=4.2.
                                                                               CHITHRE
                                                                                          568
       pu=u+1.
                                                                               CHITHRE
                                                                                          5n9
       PH(6)=2.4(H-1.)4(H-2.)/(15.4(2.4R+3.)4(2.4R+1.))
                                                                               CHITHRE
                                                                                          570
       CALL FHEU
                                                                               CHITHRE
                                                                                          571
```

```
FTN 4.6+433B
                                                                             11/22/78 11.36.27
             74/14
CHITHPL
                     0PT=2 UO
                                                                               CHITHRE
                                                                                          572
      REGIN THE SUM OVER PATHS
C
                                                                                          573
                                                                               CHITHRE
С
                                                                                          574
                                                                               CHITHRE
      SUMK=(0.,U.)
                                                                                          575
                                                                               CHITHRE
      no 40 k=1.0
                                                                               CHITHRE
                                                                                          576
   LO SUMK = SIMK +PR (K) *FAHCD (K)
                                                                                          577
                                                                               CHITHRE
      RH=R+ (R+1.)
      E=8(1) +RH-D(1) +RH++2+HE+RR++3
                                                                               CHITHRE
                                                                                          57B
                                                                                          579
      DIS=(2.*R+1.)*EXP(-E/(6.9503E-01*TEMP))/Q
                                                                               CHITHRE
                                                                               CHITHRE
                                                                                          580
   SO SUMU=SUMU+SUMK*DIS
                                                                                          5A1
                                                                               CHITHRE
      1111 O1 Un
                                                                                          582
                                                                               CHITHRE
 30nn INUFX=1
                                                                                          543
      IF (NC.EQ.NV+1) INDEX=2
                                                                               CHITHRE
                                                                                          584
      DV=J(NA+NU)/OMEGAE
                                                                               CHITHRE
                                                                               CHITHRE
                                                                                          585
      BEGIN THE SUM OVER ROTATIONAL LEVELS
                                                                               CHITHRE
                                                                                          586
      5UMJ=(0..V.)
                                                                                          5A7
                                                                               CHITHRE
      DO 5020 7=1'N'
      R IS THE ACTUAL ROTATIONAL QUANTUM NUMBER
                                                                               CHITHRE
                                                                                          SAA
C
                                                                                          549
                                                                               CHITHRE
      1-C=8
                                                                                          590
                                                                               CHITHRE
      TA=R
                                                                                          591
                                                                               CHITHRE
      nU 2035 K=1.6
                                                                               CHITHRE
                                                                                          592
      PK(K)=0.
                                                                               CHITHRE
                                                                                          593
      G(K,1)=(0.+0.)
                                                                               CHETHRE
                                                                                          594
 2035 G(K.2)=(0.+0.)
                                                                               CHITHRE
                                                                                          595
000
                                                                               CHITHRE
                                                                                          596
      SUM OVER HUTATIONAL LEVELS BY PATHS
                                                                               CHITHRE
                                                                                          597
                                                                               CHITHRE
                                                                                          59A
      [F(P.LT.1) GO TO 2015
                                                                                CHITHRE
                                                                                          500
      KM±1
                                                                               CHITHPE
                                                                                          600
      16=P+1.
                                                                               CHITHRE
                                                                                          601
      TC=P
                                                                               CHITHRE
                                                                                          602
      TU=R-1.
                                                                                          603
                                                                               CHITHRE
      PH(1)=2./(15.*(2.*R+1.))
                                                                               CHITHRE
                                                                                          604
      CALL TUMO
                                                                               CHITHRE
                                                                                          605
 2015 KM=2
                                                                               CHITHRE
                                                                                          606
      THED+1.
                                                                                CHITHRE
                                                                                          607
      TC=W
                                                                                CHITHRE
                                                                                          608
      TD=R+1.
                                                                               39HT 1HD
                                                                                          609
      PH(2)=(4.*H*R+A.*R+5.)/(15.*(R+1.)*(2.*R+1)*(2.*R+3.))
                                                                                CHITHRE
                                                                                          610
      CALL TUMO
                                                                                CHITHRE
                                                                                          611
      WMET
      THEN+1.
                                                                                CHITHPE
                                                                                          612
                                                                                CHITHRE
                                                                                          613
      TC=R+2.
                                                                               CHITHRE
                                                                                          614
      TD=P+1.
                                                                               CHITHRE
                                                                                          615
      PR(3)=2./(15.*(2.*P+3.))
                                                                                CHITHRE
                                                                                          616
      CALL TUMO
                                                                                CHITHPE
                                                                                          617
      KWE'
      TH=R+1.
                                                                                CHITHRE
                                                                                          618
                                                                                CHITHRE
                                                                                          619
      TC=0
                                                                               CHITHRE
                                                                                          620
      TUER
                                                                                          621
                                                                               CHITHRE
      pk(4)==(R+2.)/(15.*(R+1.)*(2.*R+1.))
                                                                               CHITHRE
                                                                                          622
      CALL TUMU
                                                                                CHITHPE
                                                                                          623
      # M=5
                                                                                CHITHPE
                                                                                          624
       To=Q+1.
                                                                                CHITHPE
                                                                                          625
       TC=R+1.
      TD=0.1.
pH(n)=-H/(15.*(Q.1.)*(2.*H.3.))
                                                                                34HT 1HO
                                                                                          626
                                                                                CHITHRE
                                                                                          627
                                                                                CHITHPE
                                                                                          628
      CALL THMU
```

```
CHITHKE
              74/14
                      0PT=2 UU
                                                           FTN 4.6+4338
                                                                                 11/22/78 11.36.27
                                                                                   CHITHRE
       KH=6
       TU=#+1.
                                                                                   CHITHRE
                                                                                              610
       TC=P+1.
                                                                                   CHITHRE
                                                                                              631
                                                                                   CHITHRE
       TU=k
                                                                                              632
       PH(n) =-SUHF(R*(H*2.)/(|H*1.)*(H*1.)*(2.*R*1.)*(2.*R*3.)))/15.
                                                                                   CHITHRE
                                                                                              633
                                                                                   CHITHRE
                                                                                              634
       CALL TUMU
                                                                                   CHITHRE
                                                                                              635
                                                                                   CHITHRE
       HEGIN THE SUM OVER PATHS
                                                                                              636
                                                                                   CHITHRE
                                                                                              637
                                                                                   CHITHRE
                                                                                              638
       TUME = (0.. U.)
                                                                                   CHITHRE
                                                                                              639
       DA 5040 K=1.6
                                                                                   CHITHRE
 2040 TUML=TUML+PR(K)+G(K+INDEX)
                                                                                              640
                                                                                   CHITHRE
       HK=H0 (H+1.)
                                                                                              641
       E=8(1) 0RH-U(1) 0RH-02+HE0HR0#3
                                                                                   CHITHRE
                                                                                              642
      (115=(2.*H+1.)*EXP(-E/(0.9503E-01*TFMP))/Q
                                                                                   CHITHRE
                                                                                              043
 2050 SUM.J=SUMJ+TUML DIS
                                                                                   CHITHRE
                                                                                              644
       MA=NC
                                                                                   CHITHRE
                                                                                              645
       IF (INDEX.EU.2) NX=ND
                                                                                   CHITHRE
                                                                                              646
       UU=MGE(1) *MGE(1) *X(NX+[NDEX+1) + (MGE(1) *MGE(2) +MGE(2) *MGE(1))
                                                                                   CHITHPE
                                                                                              647
      ==X (NX+[NULX+2) + (MUE(1) *MGE(3) +MGE(2) *MGE(2) *MGE(3) *MGE(1))
                                                                                   CHITHRE
                                                                                   CHITHRE
     (C. KJON] - XN) ANE
                                                                                              649
                                                                                   CHITHRE
                                                                                              650
      PV=PV=UU
 1111 CUNTINUE
                                                                                   CHITHRE
                                                                                              651
      END THE SUM OVER ROTATIONAL LEVELS SUMV(NR.NC.ND)=SUMV(NB.NC.ND)+SUMJ*PV
                                                                                   CHITHRE
                                                                                              652
C
                                                                                              653
                                                                                   CHITHRE
   90 CUNTINUE
                                                                                   CHITHRE
                                                                                              654
                                                                                   CHITHRE
                                                                                              655
С
č
      END THE SUM OVER FREQUENCY PERMUTATIONS
                                                                                   CHITHRE
                                                                                              656
c
                                                                                   CHITHRE
                                                                                              657
       SUMV (NA+NC+ND) =PM* (-2.13E-261*SUMV (NB+NC+ND)
                                                                                   CHITHRE
                                                                                              658
       IF (IWRITE NE . 1) GO TO 100
                                                                                   CHITHRE
                                                                                              649
                                                                                   CHITHRE
       NUA=NB-1
                                                                                              660
       NCA=NC-1
                                                                                   CHITHRE
                                                                                              661
      NUA=ND-1
                                                                                   CHITHRE
                                                                                              662
      MUUSUMY=CAUS (SUMY (NH+NC+ND))
                                                                                   CHITHRE
                                                                                              663
       WHITE (6+110) NRA+NCA+NDA+SUMV (NB+NC+ND)+MODSUMV
                                                                                   CHITHRE
                                                                                              664
  11A FUNNAT(22A+15+10X+15+10X+15+8X+E15.8+8X+E15.8+8X+E15-8)
                                                                                   CHITHRE
                                                                                              645
  Inn CH13=CH13+5UMV(NB+HC+ND)
                                                                                   CHITHRE
                                                                                              646
   RO CUNTINUE
                                                                                   CHITHRE
                                                                                              667
                                                                                   CHITHRE
   70 CUNTINUE
                                                                                              668
                                                                                   CHITHRE
                                                                                              669
   AN CUNTINUE
                                                                                   CHITHRE
                                                                                              670
       END THE SUM OVER VIBRATIONAL LEVELS FOR A GIVEN PERMUTATION OF THE CHITHRE
                                                                                              671
       PUMP FREQUENCIES
                                                                                   CHITHRE
                                                                                              672
                                                                                   CHITHRE
                                                                                              673
                                                                                   CHITHKE
                                                                                              674
      OUTPUT THE RESILTS
                                                                                   CHITHRE
                                                                                              675
                                                                                   CHITHRE
                                                                                              676
       #5=3P+#U+#K
                                                                                   CHITHRE
                                                                                              677
       MUDCHI=CAUS (CHI3)
                                                                                   CHITHPE
                                                                                              67A
       WHITE (6.115) WS. CHI3. MODCHI
                                                                                   CHITHRE
                                                                                              679
  115 FURMAT ( /+5X++FOR THE SUM FREQUENCY ++E15+8+/+5X+ +THIRD ORDER SUS CHITHRE
                                                                                              680
     ECEPTIBILITY HAS RE PART **E15.44. CM6/ERG **/*5%. *THIND ORDER SUS ECEPTIBILITY HAS IM PART **E15.44. CM6/ERG **/*5%. *THIND ONDER SUS
                                                                                  CHITHRE
                                                                                              641
                                                                                  CHITHRE
                                                                                              642
     ECEPTIBILITY HAS MUDULUS *+E15.A+* CM6/ERG *)
                                                                                   CHI THRE
                                                                                              643
                                                                                   CHITHRE
 SOUD CONTINUE
                                                                                              644
       55 TO UU
                                                                                   CHITHRE
                                                                                              645
```

CHITHPE 76/74 NPT=2 UD FIN 4.6+433B 11/22/78 11-36-27

1000 WRITE(6+116) CHITHRE 686
116 FURMAT(///.5x.*THAT#S ALL FOLKS*) CHITHRE 687
STUP
END CHITHRE 689

```
11/22/78 11.36.27
 FREC
             74/14
                      OPT=2 UU
                                                         FTN 4.6+433B
      SUBPOUTING FREQ
                                                                                FREG
                                                                                FREQ
                                                                                             3
c
      THIS SUBHOUTINE CALCULATES THE FREQUENCY DENOMINATOR FABCO
                                                                                FREQ
                                                                                FREO
                                                                                             5
                                                                                FREQ
       INTEGER UMLGAA.OMEGAB.UMEGAC.OMEGAD
                                                                                             6
      CUMPLEX FABCD(20) .EAB.EAC.EAD.FD1.FD2.FD3.FD4.FD5.FD6.GABCD(20)
                                                                                FREO
                                                                                FREQ
      CUMMON/CEREU/ NA.NB.NC.ND.RA.RR.RC.RD.W1.W2.W3.K.W(2.5.50).
                                                                                             8
                                                                                FREO
     EFAUCD (20) +LAB+EAC+EAD+WSIZE+AE+DELTA
                                                                                             9
                                                                                FREQ
      CUMMON/DSUMU/L.UMEGAA.UMEGAU.OMEGAC.UMEGAD.GABCD(20).SA.SB.SC.SD
                                                                                            10
                                                                                FREG
CS.
      DEBUG
                                                                                            11
                                                                                FREQ
                                                                                            12
      AKRAYS
CS
                                                                                FREQ
                                                                                            13
      GUIDS
CS
      IF (AE.EQ.U..AND.DELTA.EQ.O.) GO TO 5
                                                                                FREQ
                                                                                            14
                                                                                FREQ
                                                                                            15
c
                                                                                FREQ
      CALCULATE ENERGY LEVEL DIFFERENCES
                                                                                            16
                                                                                FREQ
                                                                                            17
С
                                                                                FREQ
                                                                                            18
       JA=5A+0.5
                                                                                FREQ
                                                                                            19
      J8=28+0.5
                                                                                FREQ
       JC=5C+0.5
                                                                                            20
                                                                                FREQ
                                                                                            21
      JU=50+0+5
                                                                                FREO
      WADER (OMEGAA.NA.JA) -W (OMEGAB.NB.JB)
                                                                                            22
                                                                                FREG
      WAC=W (OMEGAA+NA+JA) -W (OMEGAC+NC+JC)
                                                                                            23
                                                                                FREG
                                                                                            24
25
      WAD=W (I)MEJAA.NA, JA) -W (UMEGAD.ND.JD)
                                                                                FREO
      GU TO 7
                                                                                FREQ
    S JA=RA+1.
                                                                                            26
                                                                                FREQ
      Jd=68+1•
                                                                                            27
                                                                                FREO
      JC=AC+1.
                                                                                            28
       JD=ED+1+
                                                                                FREG
                                                                                            29
      (BL. 884.1) W- (AL. AM.1) H= UAN
                                                                                FREG
                                                                                            30
      WAC=W(1.NA.JA)-W(1.NC.JC)
                                                                                FREQ
                                                                                            31
                                                                                FREQ
      (GL . GN . I) W= (AL . AN . I) W= CAW
                                                                                            32
    7 CUNTINUE
                                                                                FREQ
                                                                                            33
                                                                                FREQ
                                                                                            34
č
      SET UP INDICES TO BE PRINTED WHEN A RESONANCE IS ENCOUNTERED
                                                                                FREG
                                                                                            35
                                                                                FREO
                                                                                            36
                                                                                FREQ
                                                                                            37
      MAX=NA-1
                                                                                FREO
                                                                                            38
      NUX=NH-1
                                                                                FREO
                                                                                            39
      NCX =NC-1
                                                                                FREQ
                                                                                            40
      NUX=ND-1
      IF (AE.EQ.U..AND.DELTA.EU.O.) GO TO 10
                                                                                FREU
                                                                                            41
                                                                                FREQ
                                                                                            42
      [A=2.#5A
                                                                                FREO
      In=2.458
                                                                                            43
                                                                                FREQ
                                                                                            44
      1C=2.#5C
                                                                                            45
                                                                                FREG
      10=2. 450
                                                                                FREO
                                                                                            46
47
      KA=2+OHEGAA-1
                                                                                FREQ
      KU=2+ONEGAU-1
                                                                                FREO
      KC=200MEGAC-1
                                                                                            48
                                                                                FREQ
      KU=2"OME GAU-1
                                                                                            49
                                                                                FREQ
      GU TO 17
                                                                                            50
                                                                                FREG
   IN CUNTINUE
                                                                                            51
      AVEAL
                                                                                FREQ
                                                                                            52
                                                                                FREQ
      ไห≈นย
                                                                                            53
                                                                                FREQ
      IC=HC
                                                                                            54
                                                                                FREQ
                                                                                            55
      IN=ND
                                                                                FREU
                                                                                            56
   17 CUNTINUE
                                                                                FREG
                                                                                            57
C
                                                                                FREQ
                                                                                            58
```

FUR=1000.

FRFO	74/74	00 Z=140	FTN 4.6+433R	1/22/78	11.36.27
	ent -uance de la	1 . M3AM3		FREQ	59
	FUI=WAR+EAD+W			FREQ	60
	FD2=WAD-EAU-W			FREQ	61
)1)).LE.WS[ZE3)	FIREREAL (FOL)	FREU	62
	[(FOR NE - 100			FREO	43
1.1)2)) .LE.WS[ZE3)	FOR=RFAL (FUZ)	FREQ	64
•	IF IFDR . NE . LOOK		· · · · · · · · · · · · · · · · · · ·	FRED	45
1	FUJ=WAC+EAL+W			FREQ	66
-	FD4=WAC-EAC-W			FREQ	67
	WSIZEZ-WSIZE*			FREQ	68
	IF LAHS (REAL (FE)3)).LE.WS[ZE2)	FOR=REAL (FU3)	FREQ	69
	IF (FOR NE - LOOK			FREQ	70
12)411.LE.WSIZE2)	FOR=REAL (FD4)	FREQ	71
	IF (FOR.NE.1000			FREQ	72
2	FUS=WAD+EAU+W			FREQ	73
	FU6=WAB-EAU-W	·		FREQ FREQ	74
	WSIZEI=WSIZE®		500-0544 (505)	FREG	75 76
	IF (FDR_NE.100)	15)).LE.WSIZE1)	FI)K=KEAC (FUD)	FREQ	77
		06)).LE.WS[ZE])	EDB=REAL (ED6)	FREO	78
1.3	IF (FOR NE-100)		7 ()K=KP 4C 17 00 /	FREG	79
3		ND DELTA EQ.O.)	60 10 23	FREO	AO
•			D5)+(1/FD2+1/FD5)/(FD4+FD6)	FREQ	Al
	GU TO 33		•••	FREQ	82
23		01+1/FD6)/(FD3*F	D5)+(1/FD2+1/FD5)/(FD4#FD6)	FREQ	83
	CUNTINUE			FREQ	84
	RETURN			FREQ	85
C C				FREG	A6
С	WRITE STATEMEN	NTS USED WHEN A	RESONANCE IS ENCOUNTERED FOLLOW	FREG	A 7
C				FREQ	A. 8
410		NO DELTA EQ. 0.)		FREG	PA
			TA-18-1C-1D-KA-KB-KC-KD-FDR	FREQ FREQ	90
			SOMANCE: VA= +.I5.5X.+ VB= +.I5.5X.+		92 91
)x.+ JA= *.[3++/2+.5X++ JB= *.[3++/2*+ !.[3++/2+,/.29X++ KA= *.[3++/2+.5X+	FRED	93
			3.*/24.2X.* KD= *.13.*/2*.2X.* DW= *.	FREQ	94
	£15.8)	(-) JA 1 10 11-	14-15-42WA- WAT - 4124 15 4 WA DM-	FREQ	95
	FUR=1000.			FREQ	96
	60 10 11			FREQ	97
420		UD.DELTA.EQ.O.)	GO TO 42	FREQ	98
		•	IA. IB. IC. IU.KA.KB.KC.KD.FDR	FREQ	99
	FUR=1000.			FREQ	100
	GU TO 1			FREU	101
510		VI).DELTA.EQ.O.)		FREO	105
			IA-IB-IC-ID-KA-KB-KC-KD-FDR	FREG	103
			ONANCE: VA= 4.15.5x. + VR= 4.15.5x.	FREO	104
1	* VC= * 15 + 5X	.* VD= *+15+/+21	/x.+ Ja= *.13,*/2*.5x,* JR= *.13,*/2*,	ENEU ENEU	105
			7-13-4/24-/-27X-0 KA= 4-13-4/24-5X-	FREU FREU	106 107
	E12'H)	KA+24+, VC= -41-	3.4/2*.5X.* KD= 4.13.*/2*.5X.* DW= *,	FREQ	108
,	FUH=1000.			FREQ	109
	60 tu 15			FREQ	110
520		ID.DELTA.EQ.O.)	GN TO 52	FREO	iii
· · · ·			TA-IB-IC+ID+KA-KB-KC-KD+FDR	FREG	112
	FUH=1000.			FREO	113
	50 TO >			FREG	114
610	TELAE . FO. U A	IN.DELTA.EQ.O.)	GO TO 61	FREO	115

74/14

SUA	on 74774 n	P1=2 UU	FTN 4.6+4338	11/22/78	11.36.27
	SUMPOUTING SUM	0		SUMO	2
С	, - -			SUNO	3
č	THIS SHUMUUTINE	CALCULATES THE COL	TRIBUTIONS TO THE UMEGA SUM	SUNO	4
Ċ	OVER PATHS			SUMO	5
č				SUMO	6
_	CUMPLEX FAUCDIZ	0) •F(20•2)		SUMO	7
			2(4) •PHI3(4) •PHI(20)	SUNO	a
			HD.F (20.2) .K.CA(5.50) .CB(5.50)	SUMO	9
	ERR (2.3)50)			SUMO	10
	CUMMON DSUMOZE.	IA - IH - IC - IO - F ABCD (20).5A.SU.SC.SD	SUMO	11
C\$	りとないら			SUMO	12
C S	ARRAYS			SUMO	13
Ċ\$	GUTOS			SUMO	14
C				SUNO	15
С	DEFINE HUTATION	AL LEVEL INDICES TO	BE PASSED TO FREQ	SUMO	16
С				SUMO	17
	SA=HA			SUMO	18
	Su≃RB			SUMO	19
	SC=HC			SUNG	20
	2n≤r0			SUNO	21
С				SUMO	22
	2.0+A45AC			SUNO	23
	J¤≈RH+0.5			SUNO	24
	JC=HC+0.5			SUMO	25
	JU≈20+0•5			SUMO	26
С				SUNO	27
С	SURT THE REDUCE	D MATRIX ELEMENTS		SUMO	28
С				SUMO	29
	IF (RA-RB) 11-12	,13		SUMO	30
1	1 RI(1) = RR(1+1+JA			SUMO	31
	R2([]=RK(2+1+JA)		SUMO	35
	60 10 2 0			SUMO	33
1	AC+2+1)4H=(1)1H 2			SUMO	34
	H2(1)=HH(2+2+ JA)		SUMO	35
	ou to 50			SUMO	36
1	3 HT(1)=48(1+3+7V			SUMO	37
_	AC(1)=RR(2+3+JA)		SUMO	38
С		-3		SUMO SUMO	39
	n [f(RU-RC) 21.22			SUMO	40
2	H(-[-[]) HH= (5) 14 [SUMO	41
	K5 (5) =KK (5 • 1 • NB	,		SUMO	42 43
-	- パリ (10 30 - 10 10 10 10 10 10 10 10 10 10 10 10 10			SUMO	44
	HT (5) 388 (2) 78 C			SUMO	45
	P2(2)=AF(2+2+JH	,		SUMO	46
-	80.51)44=(2)13 E			SUMO	47
•	HC(5)=HR(5.3.7H			SUMO	48
c	KE (2) - KK (E) 3 (3)	•		SUMO	49
	n [F(PC-RD) 31.32	. 13		SUMO	50
	1 h;(3)=bH(1+1+7C			SUMO	ร์เ
,	H2(3)=HH(4.1.1C			SUMO	śż
	GU TO 40	,		SUMO	ร์วั
7	2 F1 (3) = KH (1+2+JC)		SUMO	54
	P2(3) =RK(2+2+JC			SUMO	55
	60 10 40	•		SUMO	56
7	7 HE (3) = PR (1+3+JC)		SUMO	57
	K2(3)=HK(2+3+JC			SUMO	58
	- · · -				

```
SUMO
              74/74
                                                                                  11/22/78 11.36.27
                       00 S=140
                                                            FTN 4.6+433B
                                                                                    SUMO
                                                                                                 50
   40 IF(PD-RA) 41.42.43
                                                                                    SUMO
                                                                                                 60
    41 pl(4)=pR(1+1+10)
                                                                                    SUMO
                                                                                                 41
       R2(4)=PH(2+1+.JD)
                                                                                    SUMO
                                                                                                 62
       GO TO 50
                                                                                    SUMO
                                                                                                 43
   47 PL(4)=UR(1+2+JD)
                                                                                    SUMO
                                                                                                 64
       R2(4) =PR(2+2+JU)
                                                                                    SUMO
                                                                                                 65
       6U TO 50
                                                                                    SUMO
                                                                                                 66
   43 P1(4)=RR(1+3+JD)
                                                                                    SUMO
                                                                                                 67
                                                                                    SUMO
       R2(1)=RR(2+3+JD)
                                                                                                 68
   SO CONTINUE
                                                                                    SUMO
                                                                                                 69
                                                                                    SUMO
                                                                                                 70
CCC
       DETERMINE THE PHI#S
                                                                                    SUMO
                                                                                                 71
                                                                                    SUMO
                                                                                                 72
       PHI1(1)=CA(NA+,JA)*CA(NB+JB)*R1(1)*CB(NA+JA)*CB(NR+JB)*P2(1)
                                                                                    SUMO
                                                                                                 73
       PHI1(2)=CA(NB.JB) *CA(NC.JC) *R1(2) *CB(NR.JB) *CB(NC.JC) *H2(2)
                                                                                    SUMO
                                                                                                 74
       PHI1 (3) =CA(NC, JC) *CA(ND, JD) *R1 (3) +CB(NC, JC) *CB(ND, JD) *R2(3)
                                                                                    SUMO
                                                                                                 75
       PHI1 (4) = CA (ND.JD) + CA (NA.JA) +R1 (4) +CB (ND+JD) +CB (NA.JA) +R2 (4)
                                                                                    SUMO
                                                                                                 76
                                                                                    SUMO
                                                                                                 77
C
       PHI2(1) = CA(NA+JA) + CA(NB+JB) + R2(1) + CB(NA+JA) + CB(NB+JB) + R1(1)
                                                                                    SUMO
                                                                                                 78
       PHIZ(2) = CA(NB.JB) + CA(NC.JC) + RZ(2) + CB(NB.JB) + CB(NC.JC) + R1(2)
                                                                                    SUMO
                                                                                                 79
       PH12(3) =CA(NC.JC) *CA(ND.JD) *R2(3) *CB(NC.JC) *CB(ND.JD) *R1(3)
                                                                                    SUMO
                                                                                                 80
       PHI2(4) = CA(ND.JD) + CA(NA.JA) + R2(4) + CB(ND.JD) + CB(NA.JA) + R1(4)
                                                                                    SUMO
                                                                                                 81
C
                                                                                    SUMO
                                                                                                 82
      PHI3(1) = CA(NA-JA) + CB(NB+JB) + R1(1) - CB(NA+JA) + CA(NB+JB) + R2(1)
                                                                                    SUMO
                                                                                                 A3
      PHI3(2) = CA(NB.JB) + CB(NC.JC) +R1(2) - CB(NB.JB) + CA(NC.JC) +R2(2)
                                                                                    SUMo
                                                                                                 84
      PHL3(3) = CA(NC.JC) +CB(ND.JD) +R1(3) +CB(NC.JC) +CA(ND.JD) +P2(3)
                                                                                    SUMO
                                                                                                 45
      PHI3(4) =CA(ND+JD) +CB(NA+JA) +R1(4) -CB(ND+JD) +CA(NA+JA) +R2(4)
                                                                                    SUMo
                                                                                                 86
CCC
                                                                                    SUMO
                                                                                                 87
      SUM OVER UMEGA BY PATHS FOR OMEGAA EQ 0.5
                                                                                    SUMO
                                                                                                 88
                                                                                    SUMO
                                                                                                 a o
       [A=]
                                                                                    SUMO
                                                                                                 90
C
                                                                                    SUMO
                                                                                                 91
      L=1
                                                                                    SUMO
                                                                                                 92
      IR≄J
                                                                                    SUMO
                                                                                                 93
       [C=1
                                                                                    SUMO
                                                                                                 94
       10=1
                                                                                    SUMO
                                                                                                 95
      PHI(1)=PHII(1)=PHII(2)=PHII(3)=PHII(4)
                                                                                    SUMO
                                                                                                 96
      CALL FREW
                                                                                    SUMO
                                                                                                 97
      l = 2
                                                                                    SUMO
                                                                                                 AP
       In=I
                                                                                    SUMO
       [C=1
                                                                                    SUMO
                                                                                               100
       10=2
                                                                                    SUMO
                                                                                               101
      PHI(2)=PHII(1)*PHII(2)*PHI3(3)*PHI3(4)
                                                                                    SUMO
                                                                                               102
      CALL FREU
                                                                                    SUMO
                                                                                               103
      £=3
                                                                                    SUMO
                                                                                               104
      16=1
                                                                                    SUMO
                                                                                               105
      1C=5
                                                                                    SUMO
                                                                                               106
      10=1
                                                                                    SUMO
                                                                                               107
      PHI(3)=PHII(1)*PHI3(2)*PHI3(3)*PHII(4)
                                                                                    SUMO
                                                                                               LOA
      CALL FREG
                                                                                    SUMO
                                                                                               109
      L =4
                                                                                    SUMO
                                                                                               110
      18=1
                                                                                    SUMO
                                                                                               111
      [C=2
                                                                                    SUMO
                                                                                               112
      10=7
                                                                                    SUMo
                                                                                               113
      PHI (4) = PHII (1) PHI (2) PHI 2 (3) EPHI 3 (4)
                                                                                    SUMO
                                                                                               114
      CALL FREQ
                                                                                    SUMO
                                                                                               115
```

SUMN	74//4 OPT=2 UU	FTN 4.6+433H	11/22/78	11.36.27
	1.=5		SUMO	116
	[h=>		SUMO	117
	ic=!		SUMO	118
	Inst		SUMO	119
	PHI(5)=PHIJ(1)+PHI3(2)+PHI1(3)+PHI1(4)		SUMO	120
	CALL FREU		SUMO	121
	F=0		SUMO	122
	19=5		SUMO	123 124
	[C=]		SUMO	125
	10=2		SUMO SUMO	125
	Pnl(h)=Phl3(1)*Phl3(2)*Phl3(3)*Phl3(4)		SUMO	127
	CALL FHEU		SUMO	128
	(2)		SUMO	129
	16=3		SUMO	130
	1C=2 1D=1		SUMO	131
	PHI (7) =PHI3(1) =PHI2(2) =PHI3(3) =PHI1(4)		SUMO	132
	CALL FREU		SUMO	133
	[=#		SUMO	134
	IB#2		SUMO	135
	IC=5		SUMO	136
	(S=0)		SUMO	137
	PHI(8)=PHIJ(1)*PHIZ(2)*PHIZ(3)*PHI3(4)		SUMO	1.38
	CALL FHEU		SUMO	139
С			SUMO	140
С	BEGIN SUM UVER PATHS		SUMO	141
C			SUMO	142
	$F(K_{\bullet}) = (0 \cdot *0 \cdot)$		SUMO	143
	00 90 F=1.9		SUMO	144
60	F(K+1) = F(K+1) + PHI(L)*FABCD(L)		SUMO	145
	If (RA.EQ.U.5) GO TO 80		SUMO	146
C			SUMU	147
C	SUM OVER UMEGA BY PATHS FOR OMEGA EQ 1.5		SUMO	148
¢			SUMO	149
_	[A=>		SUMO SUMO	150 151
С	1		SUMO	152
	[=]		SUMO	152
	10=5		SUMO	154
	In=5 Ir=5		SUMO	155
	pdl(1)=Phl2(1)+Phl2(2)+Phl2(3)+Phl2(4)		SUMO	156
	CALL FREQ		SUMO	157
	L=6		SUMO	158
	10=2		SUMO	159
	1C#2		SUMO	160
	10-1		SUMO	161
	PHI(2)=PHI2(1)*PHI2(2)*PHI3(3)*PHI3(4)		SUMO	162
	CALL FREU		SUMO	163
	(=3)		SUMU	164
	14=>		SUMO	165
	[C=]		SUMO	166
	[n=5		SUMO	167
	PIIL(3)=PH12(1)=PH13(2)=PH13(3)=PH12(4)		SUMO	168
	CALL FRED		SUMU	169
	1,24		SUMU	170
	[u=2		SUMO	171
	1C=1		SUNO	172

SUMO	74/74 UPT=2 UO	FTN 4.6+4338	11/22/78	11.36.27
	[D=1		SUMO	173
	pH1(4)=PH12(1)+PH13(2)+PH11(3)+PH13(4)		SUMO	176
	CALL FREU		SUMO	175
	L=5		SUMO	176
	16=1		SUHO	177
	1C=2		SUMO	178
	In=S		SUMO	179
	PHI (5) =PHIJ(1) +PHIJ(2) +PHIZ(3) +PHIZ(4)		SUMO	180
	CALL FREU		SUMO	181
	(=6		SUMO	182
	[4=[SUM()	183
	[C=>		SUMO	194
	10=1		SUMO	185
	pHI(6)=PHI3(1)*PHI3(2)*PHI3(3)*PHI3(4)		SUMO	186
	CALL FREG		SUMO	187
	<u>L</u> =7		SUMO	188
	[H±[SUMO	189
	[C=]		SUMO	190
	10=5		SUMO	191
	PHI(7)=PHI3(1)*PHI1(2)*PHI3(3)*PHI2(4)		SUMO	105
	CALL FREU		SUMO	193
	L=8		SUMO	194
	In=I		SUMO	195
	IC=1		SUMO	196
	10=1		SUMO	197
	PHI (8) = PHIJ (1) * PHII (2) * PHII (3) * PHI3 (4)		SUMO	198
_	CALL FREG		SUMO	199
C	of Case and the Co. Balling		SUMO	2 00
C C	BEGIN SUM UVER PATHS		SUMO	501
C	FIX 31-10 .0 .		SUMO SUMO	202
	F(K.2)=(0.+0.)			203
7^	DU 70 [=1+8		SUMO SUMO	204
	F(K.2) = F(K.2) + PHI(L)*FABCD(L)		SUMO	205
r ()	CUNTINUE RETURN		SUMO	206
	END		SUMO	207
	נייש		30110	808

```
11/22/78 11.36.27
                                                         FTN 4.6+4338
             74/14
                     OPT=2 UU
LMFNTS
                                                                                 LMENTS
      SUBPOUTING LMENTS
                                                                                 LHENTS
                                                                                               3
      CONFRONTHINCOMYME - MFXE + x (2+5+3)
                                                                                  LMENTS
      HEAL N(S)
                                                                                  LHENTS
C
      THIS SUBROUTINE CALCULATES THE EXPECTATION VALUE OF X++1 FOR
                                                                                 LHENTS
C
      ANNARMONIS OSCILLATOR EIGENFUNCTIONS: THE RESULTS ARE STORED IN
                                                                                 LMENTS
                                                                                  I MENTS
                                                                                               A
                            X(K+1+CASE+1+1)
                                                                                  LMENTS
      WHERE
                                                                                  LMENTS
                                                                                              10
                     J=0 FOH CASE 1
      < >++++++K>1
                                                                                  LMENTS
                                                                                              11
                     J=2 FOR CASE 2
C
                                                                                  LHENTS
                     x=0.1.2.3.4
c
                                                                                  LHENTS
                                                                                              13
C
                                                                                  LMENTS
c
                                                                                  LMENTS
                                                                                              15
      EPSIL=-2. "SORT (WEXE/(15. *WE))
                                                                                  LMENTS
                                                                                              16
C
                                                                                  LMENTS
                                                                                              17
      DETERMINE THE NORMALIZATION CONSTANTS
C
                                                                                  LMENTS
                                                                                              18
                                                                                              19
                                                                                  LMENTS
      DO 10 1K=1+5
                                                                                  LHENTS
                                                                                              20
      H=IK-1
                                                                                  LMENTS
                                                                                              21
   10 H(IK)=SUKF(1+EPSIL+#2.+((5.*R+7.)*(2.*R+7.)+12.*(2.*R+1.)*
                                                                                  LMENTS
                                                                                              22
     ESURT (R+ (K+1.) ) ) / 72.)
                                                                                  LMENTS
                                                                                              23
                                                                                  LHENTS
                                                                                              24
      DETERMINE THE MATRIX ELEMENTS
                                                                                  LMENTS
                                                                                              25
                                                                                  LMENTS
                                                                                              26
      x(1.1.1)=1.
                                                                                              27
                                                                                  LMENTS
      x(2,1,1)=-EPSTL*(SQRT(2.)-1.)/2./N(1)/N(2)
                                                                                  LMENTS
                                                                                              28
      x(3,1,1)=-EPSIL++2.+(21.+2.+SORT(6.))/24./N(1)/N(3)
                                                                                  LMENTS
      x(4,1,1)=-EPS[L*(SQHT(3,)-1.)/6./N(1)/N(4)
                                                                                  LHENTS
                                                                                              30
      x(5.1.1)=-EPSIL**2.*SQRT(6.)*(5.+SQRT(5.))/12./N(1)/N(5)
      x(1,2,1)=-LPSIL *+2.*(21.+2.*SQRT(6.))/24./N(1)/N(3)
                                                                                  LHENTS
                                                                                              31
                                                                                  LMENTS
                                                                                              32
      x(2,2,1)=-EPSIL*(SQRT(2,)+1.-5QRT(3,))/2./N(2)/N(3)
                                                                                  LMENTS
                                                                                              33
      x (3.2.1)=1.
                                                                                  LMENTS
                                                                                              34
      x(4,2,1)=-EPSIL*(SORT(2.)+SURT(3.)-SORT(6.))/2./N(4)/N(3)
       x(5,2.1)=-LPS1L**2.*(121.*6.*SQRT(30.1)/24./N(5)/N(3)
                                                                                              35
                                                                                  LMENTS
                                                                                  LMENTS
      x(1,1,2)==EPS[L+3./2./N(1)/N(1)
                                                                                              36
      x(2,1,2)=(1./SORT(2.)+EPSIL++2.+(7.+SQRT(2.))/12.)/N(1)/N(2)
                                                                                  LMENTS
                                                                                              37
      x(3,1,2)=-EPSIL*3.*(SQRT(2,)-1,)/4./N(1)/N(3)
x(4,1,2)=EPSIL**2.*(39,-2.*SQRT(3,1)/8./N(1)/N(4)
                                                                                  LHENTS
                                                                                              34
                                                                                  LMENTS
                                                                                              39
       x(5.1.7)==LPSIL *SQRT(6.)/17./N(1)/N(5)
                                                                                  LMENTS
                                                                                              40
                                                                                  LMENTS
                                                                                              41
       x(1,2,2) = -EPSIL*J.*(SQRT(2.)-1.)/4./N(1)/N(3)
       X(2,2+2)=(1.+EPSIL+2.+(17.+SORT(2.)+74.+209.+5QRT(2./3.)+14.+
                                                                                  LMENTS
                                                                                              42
                                                                                  LMENTS
                                                                                              43
      ESUNT(3,))/48.)/N(2)/N(3)
x(3,2,2)=-EPS(L+5.+SQRT(3.)/2./N(3)/N(3)
                                                                                  LMENTS
       x(4,2,2)=(SQRT(3,/2,)+EPSIL++2,+(27,+SQRT(2,)+19,+SQRT(3,)+304,+
                                                                                              45
                                                                                  LMENTS
      =19.05QRT(0.))/12.)/N(4)/N(3)
x(5.2.)==EPSIL*(34.06.*SQRT(6.)-23.*SQRT(3.))/N(5)/N(3)
                                                                                  LMENTS
                                                                                              46
                                                                                              47
                                                                                  LMENTS
                                                                                  LMENTS
                                                                                              48
       x(1.1.7)=(1./2. *EPS[L**2.*181./72.1/N(1)/N(1)
                                                                                              49
       x(2,1,3)=-EPSIL+(3, +SQRT(2,)+2,1/2,/N(1)/N(2)
                                                                                  I MENTS
       x(3.1.3)=(SQRT(2.)/2.+EPSIL++2.+13.+(4.+13.+SQRT(6.))/72.)
                                                                                              50
                                                                                  LMENTS
                                                                                              51
                                                                                  LMENTS
      E/N(1)/4(3)
                                                                                  LMENTS
                                                                                              52
       x(4,[,3)=-LPS;L*(8.*SURT(3.)-7.)/6./N(1)/N(4)
x(5,[,3)=-LPS;L*+2.*SURT(6.)*(103.+10.*SURT(5.))/48./N(1)/N(5)
                                                                                              53
                                                                                  LMENTS
       X(1,2,3)=(SURT(2.)/2.+EPSIL++2.-13.+(9.+3.+SORT(6.))/72.)
                                                                                  LHENTS
                                                                                              54
                                                                                  LHENTS
                                                                                              55
      E/H(1)/H(3)
                                                                                  LMENTS
                                                                                              46
       x(c,2,3)=-LPS(L*(SOHT(3.)+3.*SOHT(2.)+1.)/N(2)/N(3)
       x(J.2.3)=(5./2.-EPSIL*02.*(41.*SQNT(6.)*170.)/48.)/N(3)/N(3)
                                                                                  LMENTS
                                                                                              S7
       x(4,2,3)=-EPS(L*(2.*SQRT(3.)+9.*SQRT(2.)+2.*SQRT(6.))/2./N(4)/N(3) LMENTS
                                                                                              58
```

LMENTS	74/74	OPT=2 U0	FTN 4.6+4338	11/22/78	11.36.27
x (5.	2+3)=(5QF	RT(3.1+EPSIL++2.+(32	942.#SQRT(30.)+63.*SQRT(5.)+	LMENTS	` 59
<u> </u>	, *50KT (5.)))/24.)/N(5)/N(3)		LMENTS	60
RETU	RN			LMENTS	61
END				LMENTS	62

```
74/14
                      00 2*140
                                                          FTN 4.6+433H
                                                                                11/22/78 11.36.27
 rumo
                                                                                                3
                                                                                  TUMO
      SUBROUTING TURO
                                                                                  TUMO
      COMMER ADED (4-2) +5(6+2)
COMMER ADED (4-2) +TODEX
                                                                                   TUMU
                                                                                   ONU
      CUMMON/UTUMU/ FA+TH+TC+ID+IK+AHCD(6+2)+IINDEX
                                                                                   TUMO
                                                                                                67
C
                                                                                   TUMO
      DEFINE ROTATIONAL LEVEL INDICES TO HE PASSED TO GRED
Č
                                                                                   TUMO
                                                                                   TUMO
                                                                                                9
      TARRA
                                                                                   TUMO
                                                                                               10
      16448
                                                                                   TUNO
                                                                                               iı
       trauc
                                                                                   TUMU
                                                                                               12
       TU=PD
                                                                                   TUMO
                                                                                               13
C
                                                                                   TUMO
                                                                                               14
       Iv=K
                                                                                   TUMO
                                                                                               15
c
                                                                                               16
17
                                                                                   TUMU
       [ INDEX=INDEX
                                                                                   TUMO
C
                                                                                   TUMO
                                                                                               18
       JAPRA+1
                                                                                   TUNO
                                                                                               19
       Ju=HH+I
                                                                                   TUMO
                                                                                               20
       JL=HC+1
                                                                                   TUMO
                                                                                               21
       JU#RD+1
                                                                                   TUMO
                                                                                               22
c
                                                                                   TUMO
                                                                                               23
       IF (INDEX.LU.2) GO TU LO
                                                                                               24
25
6
27
                                                                                   TUMU
       60 10 (1+2+3+4+5+6)+K
                                                                                   TUMO
    1 6(1.1)=RA*(RA+1.)/4-
                                                                                   TUMO
       60 TO 7
                                                                                   TUMO
     2 G(C.1) =RA* (RA+1.)/4.
                                                                                               28
29
                                                                                   TUMO
       60 TO 7
                                                                                   TUMO
      G(J.1) = (KA+1.) + (RA-J.)/4.
                                                                                               30
31
                                                                                   TUMO
       40 TO 7
                                                                                   TUMO
     4 6(4.1)=0.
                                                                                   TUMO
       60 10 7
                                                                                   TUMO
                                                                                               33
     5 G(5.1)=(HA+1.)+(2.4RA+3.)/4.
                                                                                   TUMO
                                                                                               34
35
       GU TU 7
                                                                                   TUMU
     £ 6(6,11=0.
                                                                                               36
                                                                                   TUMO
     7 CUNTINUE
                                                                                               37
                                                                                   TUMO
       CALL GREW
                                                                                   TUMO
                                                                                                38
       G(K+1)=G(K+1) #AHCD(K+1)
                                                                                   TUMO
                                                                                               39
       50 to 20
                                                                                   TUMO
                                                                                               40
c
                                                                                   TUMO
                                                                                               41
    IN CUNTINUE
                                                                                   TUMO
                                                                                               42
       60 TO (11+12+13+14+15+16) +K
                                                                                   TUMO
                                                                                               43
    11 G(1.2)=(RA+3.)+(RA-1.)/4.
                                                                                   TUMO
                                                                                               44
       60 10 17
                                                                                               45
                                                                                   TUMO
    12 G(2,2) = (RA+1.) + (RA+2.)/4.
                                                                                               46
47
                                                                                   TUMO
       60 to 17
                                                                                   TUMO
    17 G(J.2)=(HA+1.)+(RA+2.)/4.
                                                                                   TUMO
                                                                                                48
       60 fo 17
                                                                                   TUMO
                                                                                                49
    14 6(4.2)=(2."HA-1.)*(RA-1.)/4.
                                                                                   TUMO
                                                                                                50
       60 TO 17
                                                                                   TUMO
                                                                                                51
    15 6(5.2)=0.
                                                                                   TUMO
                                                                                                52
       60 TU 7
                                                                                   TUMO
                                                                                                53
    16 ((0.7) zU.
                                                                                   TUMO
                                                                                                54
    17 CUNTINUE
                                                                                                55
                                                                                   TUMO
       CALL GREG
                                                                                   TUMO
       6(K.2)=0(K+2)+48CD(K+2)
                                                                                   TUMO
                                                                                                57
    20 CUNTINUE
                                                                                   TUMO
       RETURN
```

TUMO 74/74 OPT=2 UU

FTN 4.6+433R

11/22/78 11.36.27

END

TUMO

50

GRFA	74/74	OPT=2 UO	FTN 4.6+433R	11/22/78	11.36.27
	SUBPOUTINE GR	leo		GREW	8
С				GREO	3
С	THIS SUBROUT	THE CALCULATES THE	ELECTRONIC FREQUENCY DENOMINATOR	GREU	4
С				GREG	5
	CUMPLEX ABCD	4.2) .EAB.EAC.EAD		GREG	6
	CUMMON/CFREG/	NA.NB.NC.ND.HA.RR	.RC.RD.W1.W2.W3.K.W(2.5.50).	GREO	7
	=FAHCH(20) +EAE	I.EAC.EAD.WSIZE.AE.	DELTA	GREO	A
	CUMMON/DTUMO/	TA.TB.TC.TD.IK.ABC	D(6.2)+INUEX	GREO	9
С				GREO	10
Ċ	CALCIJLATE ENE	BGY LEVEL DIFFEREN	CES AND FREQUENCY DENOMINATORS	GREG	11
C				GREU	12
	JA=DA+1.			GREU	13
	Jb=98+1•			GREO	14
	JC=UC+1.			GREG	15
	JU=00+1•			GREG	16
	AL . MAG _ WE DAW	(8L+8M+1)w-(1		GREQ	17
	IF (INDEX.LU.2	1) GU TU 10	•	GREQ	18
	WAC=W(I+NA+JA)-W(1.NC+JC)		GREQ	19
	ARCU (1K+1)=1.	/(WAC+EAC+W2+W3)/(WAB+W3+EAB)	GREO	20
	GU TO 20			GREQ	21
10	WAD=#(].NA+JA)-W(1.ND+JD)		GREQ	55
	AUCD (1K+2)=1.	/(WAD+EAD+W3)/(WAR	+W3+EA8)	GREG	23
20	CUNTINUE			GREO	24
-	RETURN			GREO	25
	END			GREG	56

Sample Run

建设在电影或中心或不可能。

CALCULATION OF THE THING ORDER SUSCEPTIBILITY HOL THING URDER SUSCEPTIBILITY SCAN

LINEHIUTMS: ROTATIONAL 0 TO 1 0 TO 2 0 TO 3 000000E-00 .22500000E-00 .22500000E-00 1 TO 4 (IN RECIPROCAL CH) TEMPERATURE FOR THIS CALCULATION IS .30000000E-03 KELV THE PUMP PREGUENCIFE AME .20250680E-04 .20**250680E•0**4 .20250680E+04 FOR THE SUM FREGUENCY .60752406.04
THIRD MODE SUSCEPTIBILITY HAS HE PART .79613304E-38 CM6/ENG
THIRD THIRD SUSCEPTIBILITY HAS HOULUS .7961334E-38 CM6/ENG
THIRD THIRD SUSCEPTIBILITY HAS HOULUS .7961334E-38 CM6/ENG RESONANCES WITHIN A RANGE OF *LOGOODOGE-OD /CH CENTERED ABOUT EACH OF THE PUMP FREQUENCIES ARE INDICATED BY THE PROGRAM THE PUMP FREQUENCIES ARE .20250A80E+04 .20250680E+04 .19991410E+04 FOR THE SUM FREQUENCY .60492⁷⁷0E-04 THIRD JROEM SUSCEPTIBILITY HAS RE PART .3743042E-38 CM6/ERG THIRD ORDEM SUSCEPTIBILITY HAS IM PART .3743042E-38 CM6/ERG .371306-38 CM6/ERG PESONANCES WITHIN & RANGE OF -- 10000000E+00 /CH CENTERED ABOUT EACH OF THE PUMP FREQUENCIES ARE INDICATED BY THE PROGRAM .197328506-04 THE PUMP PHEQUENCIFS ARE ·20250686E ·04 .20250660E+04 FOR THE SUM FREQUENCY .6023461UE-04
THIRD ONDER SUSCEPTIBILITY AS HE PART .3866559E-38 CM6/ENG
THIRD ORDER SUSCEPTIBILITY AS IN PART .386859E-38 CM6/ENG
THIRD ORDER SUSCEPTIBILITY AS MODILUS .9586859E-38 CM6/ENG RESONANCES 41THIN & RANGE OF .100000000-00 /CH CENTERED ABOUT EACH OF THE PUMP FREQUENCIES ARE INDICATED BY THE PROPERTY .19991410E+04 THE PUMP FREQUENCIFS ARE -19991410E-04 .19991410E-04 FOR THE NUM PRICEDRY TOTAL TOTAL THE NUMBER OF THE NUMBER

RESONANCES WITHIN & RANGE OF ... 1000000016-00 /CM CENTERED ABOUT EACH OF THE PUMP FREDUENCIES ARE INDICATED BY THE PROGRAM

```
.194914106+04
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        .20250640E-04
 THE PURP PREQUENCIFY ARE
                                                                                                                                                                                                                                                 .19-31-101-04
 RESONANCES WITHIN A PANGE OF ... 100000001-00 /CM CENTERED ABOUT EACH OF THE PUMP FREQUENCIES ARE INDICATED BY THE PROGRAM
THE PURP PREQUENCIES ARE
                                                                                                                                                                                                                                                                                                                                                                                                   .194914101-04
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 .19/32850E+04
                                                                                                                                                                                                                                          .19441410£+04
FOR THE SUM FHEDURY .5971567.000 FOR THE SUBSTITUTE OF THE SUBSTIT
 RESURANCES OF HIMIN A MANGE OF ... LOUGGOODE ... OF CENTERED ABOUT EACH OF THE PUMP FREQUENCIES ARE INDICATED BY THE PROGRAM
 THE PUMP PHEQUENCIFE ANE
                                                                                                                                                                                                                                             .19732850E-04 .19732850E-04
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 .14732850E+04
FOR THE 3MT ANY STATEMENTS, TONGUEST MUC 3HT MOTHER STAR TILLS, TRANK CHIHAL RESPOND SEASON SEAR TILLS, TRANK CHIHAL CHIH
 MARGONAUCES ATTHE & ALONG OF . LOOGOODE-ON CH CENTERED ABOUT EACH OF THE PUMP FREQUENCIES ARE INDICATED BY THE PROGRAM
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        .20250680E+04
                                                                                                                                                                                                                                                                                                                                                                                                        .197328506.04
 THE PUMP PREQUENCIFY ARE
                                                                                                                                                                                                                                               .19732850E •04
FOR THE SUM FREQUENCY .59710-300-04
THEND JOBS STORM THILLITY HAS TE PART .11505770E-37 CNG/ERG
CHAND JOBS SASSESSES THE CONTRACT OF CONTRACT CONTR
 MESONANCES WITHIN A HANGE OF ... . 1000000E-90 /CM CENTERED ABOUT EACH OF THE PUMP FREQUENCIES ARE INDICATED BY THE PHOGRAM
 THE PURP PREQUENCIFE ARE
                                                                                                                                                                                                                                          .14732850£ .04
                                                                                                                                                                                                                                                                                                                                                                                                .19732850E .04
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 .19991-10E-04
FOR THE SHIP THE SHIP
```

AFSUNANCES ATTIMEN & ALIGH OF THE PUMP FREQUENCIES ARE INDICATED BY THE PROGRAM

THE PUMP FREQUENCIFS AME .20250680E-06 .19901410E-06 .19732850E-06

FOR THE SUM FREQUENTY .59070-00E-06 -11087707E-37 CM6/EMG
THIRD ONDEM SUSCEPTIBILITY MAS ME PART -110487707E-37 CM6/EMG
THIRD ONDEM SUSCEPTIBILITY MAS MODULUS .10487707E-37 CM6/EMG

THAT#S ALL FOLKS

APPENDIX B: x (1) CODE

Program Structure and Performance

This program is quite similar to the $X^{(3)}$ code. It is, however, much less complex. Its essential steps are:

- (1) Calculation of rotational and vibrational terms, and partition functions
- (2) Calculation of rotational populations and all transition frequencies allowed by selection rules
- (3) Calculation of the frequency denominator which occurs in the sum over states
- (4) Calculation of CHIONE accounting for population in various vibrational states
- (5) Derivation of the absorption coefficient and the refractive index minus unity from the value of CHIONE
- (6) Evaluation of the k-vector mismatches if desired

Two subroutines are called in the course of the program. Subroutine ENERGY calculates the required energy levels and partition function. Subroutine CHI calculates the real and imaginary parts of CHI for a particular lower state vibrational level.

The data is input according to READ statements at the beginning of the main program, in a format very similar to that used by the $x^{(5)}$ code. All input variables should be expressed in cgs units unless otherwise specified. Unspecified variables will be preset to zero by the program.

The input variables for this program are as follows:

LABEL is an alphanumeric array which stores the name of the molecule, for which the calculation is performed

NV is the number of vibrational levels used in the calculation

NJ is the number of rotational levels used in the calculation

NOVT is the number of overtones used in the calculation

WE, WEXE, WEYE, WEZE	are the familiar vibrational constants: w_e , $w_e x_e$, $w_e y_e$, $w_e^z e$, respectively
BE, ALPHA, GAMMA, DE, BETA	are the usual rotational constants: B_e , α_e , γ_e , D_e , β_e , respectively
U(5,5)	is a real array which contains the dipole moments for vibrational transitions between states labeled N and M (in Debye)
LINEW	is a real array which stores the linewidths for vibrational and rotational transitions
POPU	is a real array consisting of the initial distribution of population among the vibrational levels
TEMP	is the temperature of the system being modeled (in Kelvin)
WS, WP	are pump frequencies; the k-vector mismatches are calculated between the pairs of frequencies

There are three labeled COMMON blocks in the program.

VIBCOM contains the vibrational constants WE, WEXE, WEYE, WEZE

ROTCOM contains the rotational constants BE, ALPHA, GAMMA, DE

BETA, TCOM contains the temperature inputted as TEMP

(used to compute the k-vector mismatch)

The output consists of various blocks listing the following:

(1) All the input data

DN

(2) The input frequencies and the population transferred between adjacent vibrational levels

is the population transfer between adjacent vibrational levels

- (3) For each input frequency, the absorption coefficient and the refractive index minus unity
- (4) The k-vector mismatch

A complete calculation for one molecule, considering 1 vibrational level, 30 rotational levels, and 1 overtone takes less than a second on a CDC 6600, yielding results for 42 pairs of input frequencies.

Program Listing

	74/74	S=140	FTN 4.6+	433B	12/01/78	09.32.25
	PHOGRAM CHION	IE (INPUT-OUTPUT	+TAPES=[NPUT+TAPE6=QUTPUT)		CHIONE	S
C		_			CHIONE	3
č	THIS PROGRAM	CALCULATES FIR	ST ORDER SUSCEPTIBILITIES A	ND RFLATED	CHIONE	4
C	PROPERTIES FR	OM SPECTRUSCOP	IC DATA		CHIONE	5
C					CHIONE	6
Ċ					CHIONE	7
С					CHIONE	A
C	INPUTS				CHIONE	9
С					CHIONE	10
С					CHIONE	11
С	[ABEL([).[=],	A		(BA10)	CHIUNE	12
C					CHIONE	13
С					CHIONE	14
С	1 40M • CI1 • AN			(315)	CHIONE	15
С				_	CHIONE	16
С		· · · · · · · · · · · · · · · · · · ·	LEVELS USED IN THIS CALCULAT		CHIONE	17
С			EVELS USED IN THIS CALCULATE	ron	CHIONE	ĮΑ
С	MUAL = UNWREK	OF OVERTONES	USED IN THIS CALCULATION		CHIONE	19
С					CHIONE	20
С					CHIONE	21
С	ME + MEXE + MEYE +	WEZE		(4E15.8)		22
С					CHIONE	53
С	THESE ARE THE	VIBRATIONAL C	ONSTANTS (IN RECIPROCAL CM)		CHIONE	24
С					CHIONE	25
C	- - • • • • • • • • • • • • • • • • • •				CHIONE	56
C	BE+ALFHA+GAMM	A.DE.HETA		(SE15.8)		27
Ç			NGT-1176 175		CHIONE	28
C	THESE ARE THE	ROTATIONAL CO	NSTANTS (IN RECIPHOCAL CM)		CHIONE	29
Ç					CHIONE	30
C	mus manu Mina		44		CHIONE	31
C	LOW EVCH ATHE	ATIONAL LEVEL.	N+		CHIONE CHIONE	32
C		out. 2		(5E15.8)		33 34
C	()(M.N), M=1.N	UV I + Z		(2613.0)	CHIONE	35
c	(14 1)100	MOMENTE FOR	VIRRATIONAL TRANSITIONS N	*O M	CHIONE	.15 36
C C		DEBAE)	A LUMBI LOWNE IMMUSTITUMS IN	יי טו	CHIONE	37
Č	7.114	JEDILI			CHIONE	38
Č					CHIONE	19
Č	LINEW (M+N) + M	-1 -NOVT +2		(5E15.8)		40
C	Crist m (maissa la	2 1 4 MOA 1 - E		()(15.0)	CHIONE	41
Č	INCUINTES IT	N PECIPROCAL C	M) FOR ALL OVERTONE TRANSIT	TONS NEEDED		42
Č	Cantina tit	WEG! WOOME C	TON THE WIENTONE THANSEN		CHIONE	43
č					CHIONE	44
Č	PUP()(N)			(5E15.8)		45
č	,,			. ,	CHIUNE	46
č	INITIAL DISTR	THUTTON OF POP	ULATION AMONG THE VIBRATIONA	AL LEVELS	CHIONE	47
č					CHIONE	48
č					CHIONE	49
Ċ	TEMP			(1E15.8)	CHIONE	50
Ċ					CHIONE	51
С	TEMP = TEMPER	ATURE OF THE M	ODEL SYSTEM (KELVIN)		CHIONE	52
С					CHIONE	53
C				_	CHIONE	54
C	W5.WP.DN			(3E15.8)		55
С					CHIONE	56
C		· · · · · · · · · · · · · · · · · · ·	IES: DN IS THE POPULATION TO			57
С	ADJACENT VIRR	ATIONAL LEVELS	THE PRUGRAM ENDS WHEN ALL	. ARE ZERO.	CHIONE	58

```
12/01/78 09.32.25
             74/74
                                                           FTN 4.6+433B
 CHIONE
                       OPT=2
                                                                                    CHIONE
      =22X,+00+]4X,=|+,|4x+*2+,|4X+*3+,|4x+*4+)
                                                                                               116
       WRITE(6+114)(POPU(N)+N=1+NV)
                                                                                    CHIONE
                                                                                               117
  114 FURMAT (/+15x+5E15.8)
                                                                                    CHIONE
                                                                                               118
                                                                                    CHIONE
                                                                                                119
       READ (5.105) TEMP
                                                                                    CHIONE
                                                                                                120
       WHITE (A+115) TEMP
  115 FURMAT(//-5x. TEMPERATURE FOR THIS CALCULATION IS "-E15.8. KELV")
                                                                                    CHIONE
                                                                                                121
                                                                                    CHIONE
                                                                                                122
                                                                                                123
      NURMALIZE THE POPULATION DISTRIBUTION
                                                                                    CHIONE
c
                                                                                    CHIONE
                                                                                               124
      PUPTOT=0.
                                                                                    CHIONE
                                                                                                125
   00 30 N=1+NV
30 POPTOT=POPTOT+POPU(N)
                                                                                               126
127
                                                                                    CHIONE
                                                                                    CHIONE
                                                                                    CHIONE
                                                                                               128
      00 40 N=1+HV
                                                                                               129
130
   40 PUPII(N) =PUPU(N) /POPTOT
                                                                                    CHIONE
                                                                                    CHIONE
       READ IN WS.WP.ON: TERMINATE THE PROGRAM IF THEY ARE ALL ZERO
                                                                                    CHIONE
                                                                                                131
                                                                                                132
                                                                                    CHIONE
                                                                                    CHIONE
   45 READ(5.105)WS.WP.ON
                                                                                                133
                                                                                    CHIONE
       IF (WS.EQ.U..AND.WP.EQ.O..AND.DN.EQ.O.) GO TO 1000
                                                                                                134
     WRITE(A.116) #S.WP.ON
FURMAT(////.5x.*THE PUMP FREQUENCIES ARE*.2(5X.E15.8)./.5X.
EPOPULATION TRANSFERED BETWEEN ADJACENT LEVELS IS.*5X.E15.8)
                                                                                    CHIONE
                                                                                               135
                                                                                    CHIONE
                                                                                                136
                                                                                               137
                                                                                    CHIONE
                                                                                    CHIONE
                                                                                                138
Ċ
       BEGIN THE CALCULATION OF CHI AT WS AND WP: FIND ACCEF AND REMION
                                                                                    CHIONE
                                                                                                139
С
                                                                                    CHIONE
                                                                                                140
      DO 60 K=1.2
                                                                                    CHIONE
                                                                                                141
                                                                                    CHIONE
                                                                                                142
       IF (K.En.2) W=WP
                                                                                    CHIONE
                                                                                                143
                                                                                    CHIONE
       CHIRET=0.
                                                                                                144
                                                                                    CHIONE
                                                                                                145
       CHIIMT=0.
                                                                                    CHIONE
                                                                                                146
       00 50 [GROUN=1.NV
       CALL ENERGY (IGROUN.NJ.NOVT.DELTAE.0)
                                                                                                147
                                                                                    CHIONE
       CALL_CHI(IGROUN.NJ.NOVT.W.Q.U.LINEW.DELTAE.CHIRE(IGROUN.K).
                                                                                    CHIONE
                                                                                                148
                                                                                    CHIONE
                                                                                                149
      ECHI [M ([GRÜUN+K))
                                                                                                150
       CHIRET=CHIRET+POPU(IGROUN) +CHIRE(IGROUN+K)
                                                                                    CHIONE
      CHI IMT=CHI IMT + POPU (IGROUN) + CHI IM (IGROUN+K)
Z=SQRT (1+4++3.1415927+CHIRET)
                                                                                                151
                                                                                    CHIONE
                                                                                    CHIONE
                                                                                               152
                                                                                                153
      ACOFF=4. 43.1415927 W+CHIIMT/Z
                                                                                    CHIONE
                                                                                                154
                                                                                    CHIONE
      REMION=Z-1.
                                                                                               155
                                                                                    CHIONE
       WRITE (6+117) W. ACOEF . REMION
  117 FURMAT ( / .54, +FOR THE FREQUENCY + .E15.8 . / .5X . +THE ABSORPTION COEFIC CHIONE
                                                                                               156
                                                                                               157
      EIENT IS *+LIS.A-/+5X+*THE REFRACTIVE INDEX MINUS UNITY IS *+E15.8) CHIONE
                                                                                               158
                                                                                    CHIONE
   AN CUNTINUE
                                                                                               159
       IF (NV.EQ.1) GO TO 45
                                                                                    CHIONE
                                                                                    CHIONE
                                                                                               160
      REGIN THE CALCULATION OF THE K-VECTOR MISMATCH
                                                                                    CHIONE
                                                                                               161
                                                                                    CHIONE
                                                                                               145
       ITOP=NV-1
                                                                                    CHIONE
                                                                                               163
      00 70 1=1.170P
                                                                                    CHIONE
                                                                                               164
       ILOWER=1
                                                                                    CHIONE
                                                                                               165
       IUPPER=1+1
                                                                                    CHIONE
                                                                                               166
       wAVEMI=WS*DN*(CHIRE(IUPPER.1)-CHIRE(ILOWER.1)-CHIRE(IUPPER.2)+
                                                                                    CHIONE
                                                                                               147
     ECHIRE ([LOWER+2))+2.*3.1415927
                                                                                    CHIONE
                                                                                               168
                                                                                    CHIONE
                                                                                               169
       IL=ILOWER-1
       IU= [UPPEH-1
                                                                                    CHIONE
                                                                                               170
       WRITE (A+118) IL + IU+WAVEMI
                                                                                    CHIONE
                                                                                               171
  ITA FURMAT (//+5x. *THE K-VECTOR MISMATCH VARIATION DUE TO POPULATION CHIONE
```

CHTONE	74/14	0PT=2	FTN 4.6+4338	12/01/78	09.32.25
==	HANSFER HET	FFN LEVELS*,15,*	AND*.15.* IS *.E15.8)	CHIONE	173
	UNTINUE			CHIONE	174
	U TO 45			CHIONE	175
-	HITE (6.140)			CHIONE	176
1000 8	N41E(8114//_(SX. THAT#S ALL FOL	KC#)	CHIONE	177
	TOP	SAT- HIMITS ACE TOE		CHIONE	178
	ND 10b			CHIUNE	179

```
ENERGY
              74/74
                                                                                   12/01/78 09.12.25
                       OPT=2
                                                            FTN 4.6+433B
       SUBROUTINE ENERGY (IGROUN . NJ . NOVT . DEL TAE . Q)
                                                                                     ENERGY
C
                                                                                     ENERGY
                                                                                                   3
       THIS SUBROUTINE CALCULATES THE NEEDED ENERGY LEVELS AND PARTITION FUNCTION: ENERGY LEVEL DIFFERENCES ARE STORED LINEARLY IN DELTAE. THE PARTITION FUNCTION IS STORED IN Q
CCC
                                                                                     ENERGY
                                                                                     ENERGY
                                                                                     ENERGY
C $ C $
                                                                                     ENERGY
       DEBUG
                                                                                     ENERGY
       AHRAYS
                                                                                     ENERGY
       GUTOS
                                                                                     ENERGY
                                                                                                  10
       DIMENSION DELTAE (500)
                                                                                     ENERGY
                                                                                                  11
       CUMMON/VIBCOM/WE.WEXE.WEYE.WEZE
                                                                                     ENERGY
                                                                                                  12
       CUMHON/ROTCOM/BE.ALPHA.GAMMA.DE.RETA
                                                                                     ENERGY
                                                                                                  13
       CUMMON/TCUM/TEMP
                                                                                     ENERGY
       IBRANC=-1
                                                                                     ENERGY
                                                                                                  15
       ILOWER=IGHOUN-I
                                                                                     ENERGY
                                                                                                  16
       IUPPER=IGHUUN-I
                                                                                     ENERGY
                                                                                                  17
       ISTORF=0
                                                                                     ENERGY
                                                                                                  18
       HE=2.*DE*(12.*BE**2-ALPHA*WE)/(3.*WE**2)
                                                                                     ENERGY
                                                                                                  19
    A THOTEO
                                                                                     ENERGY
                                                                                                  20
       X=ILOWER+U+5
                                                                                     ENERGY
                                                                                                  21
       BERE-MEPHATX + GAMMATX**2
                                                                                     ENERGY
                                                                                                  25
       D=DE+BETA*X
                                                                                     ENERGY
                                                                                                  23
   11 Y=8*IROT*(IROT+1)-D*(IROT*(IROT+1))**2+HE*(IROT*(IROT+1))**3
                                                                                     ENEPGY
                                                                                                  24
       Z=4E+X-WEXE+X++2+WEYE+X++3+WEZE+X++4
                                                                                     ENERGY
                                                                                                  25
       INDEX=TROT+ISTORE+1
                                                                                     ENERGY
                                                                                                  26
       DELTAE (INUEX) =-Y-Z
                                                                                     ENERGY
                                                                                                  27
       I+1041=10H1
                                                                                     ENERGY
                                                                                                  28
       IF (IROT.LE.NJ) GO TO 11
                                                                                     ENERGY
                                                                                                  24
       1HOT=0
                                                                                     ENERGY
                                                                                                  30
       X=1UPPER+U-5
                                                                                     ENERGY
                                                                                                  31
       BEBE-ALPHA*X+GAMMA*X**2
                                                                                     ENERGY
                                                                                                  32
      D=DE+BETA*X
                                                                                     ENERGY
                                                                                                  33
      JROT=IROT+IBRANC
                                                                                     ENERGY
                                                                                                  34
       Y=B+JRO1+(JROT+1)-D+(JROT+(JROT+1))++2+HE+(JROT+(JROT+1))++3
                                                                                     ENERGY
                                                                                                  35
       Z=#F*X-WEXE*X**2.WEYE*X**3.WEZE*X**4
                                                                                     ENERGY
       INDEX= IRO [ + ISTORE + ]
                                                                                     ENERGY
                                                                                                  37
      DELTAE (INDEX) =DELTAE (INDEX) +Y+7
                                                                                     ENERGY
                                                                                                  38
       IKOT=IROT+1
                                                                                     ENERGY
                                                                                                  19
       IF (IROT.LE.NJ) GO TO 18
                                                                                     ENERGY
                                                                                                  40
      IKOT=0
                                                                                    ENERGY
                                                                                                  41
      JHOT= IROT + IBRANC
                                                                                    ENEPGY
                                                                                                  42
      INDEX=IROT+ISTORE+1
                                                                                    ENERGY
                                                                                                  43
       IF (JROT.LT.0) DELTAE (INDEX) =0.
                                                                                    ENERGY
                                                                                                  44
      140T=180T+1
                                                                                    ENERGY
                                                                                                  45
      IF (TROT.LE.NJ) GO TU 24
                                                                                     ENERGY
                                                                                                  46
      IF (IBRANC. EO. -1) GO TO 27
                                                                                     ENERGY
                                                                                                  47
      ITEST= | GROUN + NOVT-1
                                                                                    ENERGY
                                                                                                  48
      IF (TUPPER . LE . ITEST) GO TO 28
                                                                                     ENERGY
                                                                                                  49
      R=UF-ALPHA/2.+GAMMA/4.
                                                                                    ENERGY
                                                                                                  50
      0=6.9503E-01*TEMP/B
                                                                                    ENERGY
                                                                                                 51
      RETURN
                                                                                    ENERGY
                                                                                                  52
   27 IBHANC=1
                                                                                     ENERGY
                                                                                                 53
      1310RE=NJ+1STORE
                                                                                    ENERGY
                                                                                                 54
      GU TO A
                                                                                    ENERGY
                                                                                                 55
   PR [HHANC=-1
                                                                                    ENEHGY
                                                                                                 56
      IUPPER=IUPPER+1
                                                                                    ENERGY
                                                                                                 57
      TSTORE=NJ+ISTOPE
                                                                                    ENERGY
                                                                                                 SA
```

ENFRGY 74/74 OPT=2 FTN 4.6-4338 12/01/78 09.32.25

GU TO 8 ENERGY 59
ENERGY 60

CHI	74/74	0PT=2	FTN	4.6+4338	12/01/78	09.32.25
	SUBROUTINE CH	/ // J+U+P+W+TVON+LN+N)]	EW. DELTAE. CHIRE	•CHIIM)	CHI	2
C					CHI	3
С		ME CALCULATES THE REA		PARTS OF CHI		4
C	PAHTICULAR LO	WER STATE VIBRATIONAL	LEVEL		CHI	5
С					CHI	6
C\$	DEBING				CHI	7
C\$	AKKAYS				CHI	8
C\$	GUINS	e			CHI	9
	REAL LINEWIS.		.e K.		CHI	10
		TAE (500) +U (5+5) +LINEW	(212)		CHI CHI	11
		I/WE•WEXE•WEYE•WEZE I/BE•ALPHA•GAMMA•DE•BE	**		CHI	12
	COMMON/TOUM/T		IA		CHI	13 14
	1H01=0	EMP			CHI	15
	15108E=0				CHI	16
	12108E=0				CHI	17
	IRMANC=-1				CHI	18
	SUMA=0.				CHI	19
	SUMB=0.				CHI	żó
	SUMC=0.				CH [21
	SUMD=0.				CHI	22
	CHIRE=0.				CHI	23
	CHIIH=0.				CHI	24
6	INDEX=IROT+IS	TORE+1			CHI	žŠ
**		EX1.EQ.01 GO TO 16			CHI	26
	JHDEX=JSTURE+				CHI	27
		EX) +W) **2+0.25*LINEW(S##(M+X3UNL		CHI	28
	SUM1 = (DELTAE (CHI	29
	Z= (DELTAE (IND	EX)-#) **2+0.25*LINEW(JNDEX+N1 **2		CHI	30
	SUM2= IDELTAE!	INDEX) -W)/Z			CHI	31
	SUMG=SUM1+SUM				CHI	32
		EX)+W)**2+0.25*LINEW(JNDEX+N) **2		CHI	33
		EW(JNDEX+N)/Z			CHI	34
		EX)-#) **2+0.25*LINEW(JNDEX+N) ++2		CHI	35
		EW (JNDEX+N)/Z			CHI	36
	SUMH=SUM1+SUM	2			CHI	37
15	Z=1ROT+1	1. 7-1007			CHI	38
	IF (IBRANC.EQ.				CHI CHI	39
	SUMA=Z+SUMG+S	= : :			CHI	40
	SUMB=Z+SUMH+S				CHI	41
	Z=U (JNDEX+N)+				CHI	42 43
	SUMC=Z+SUMA+S				CHI	44
	SUMD=Z+SUMU+S				CHI	45
		NOVT) GO TO 20			CHI	46
	Z=IROT+(INUT+				CHI	47
		*HE**2-ALPHA*WE)/(3.*	4F++2)		CHI	48
		.5+GAMMA+0.25) *Z-(DE+		1E+Z++3	CHI	49
		EXP (-2/6.9503F-01/TEM			CHI	50
	CHIRE = SUMC - Z+				CHI	51
	CHIIM=SUMD+Z+				CHI	52
	IF (IROT.LE.NJ) GO TO 27			CHI	53
	CHIRE=1.357E-				CHI	54
	CHI IM=1.357E-	1*CHIIM			CHI	55
	RETURN	-			CHI	56
16	SUMG=0.				CHI	57
	SUMH=0.				CHI	58

CHT	74/74 OPT=2	FTN 4.6+4338	12/01/78	09.32.25
	60 to 15		CHI	59
10	ISTORE=ISTORE+NJ		CHI	60
, .	IBRANC=1		CHI	61
	GU TO 6		CHI	62
20			CHI	63
~11	ISTORE=ISTURE+NJ		CHI	64
	IBRANC=-1		CHI	65
	SUMA=0.		CHI	66
	SUMB=0.		CHI	67
	60 to 6		CHI	68
	IKOT=IROT+1		CHI	49
- 1	ISTORE=0		CHI	70
	JSTORE=0		CHI	71
	BRANC==1		CHI	72
	SUMA=0.		CHI	73
	SUMR=0.		CHI	74
	SUMC=0.		CHI	75
			CHI	76
	SUMD=0.		CHI	77
	GU TO 6 FND		CHI	78

Sample Run

CALCULATION OF THE FIRST ORDER SUSCEPTIBILITY AND RELATED PROPERTIES DEVIENTUM FLUORIDE

```
VIBRATIONAL TRANSITION MOMENTS (IN DEGVE)
                $0-300000E-01 -.8370000E-02
TRANSITION LINEWIDTHS I'M RECIPHOCAL CHI
                                                                               N+3
               00-30000404. 00-3000004. 00-30000054.
THE INITIAL VISRATIONAL LEVEL POPULATIONS
               .100000000001
TEMPERATURE FOR THIS CALCULATION IS .3000000E-03 KELV
THE PUMP FREQUENCIES ARE .6000000E-04 .15400000E-04
THE POPULATION TRANSFERED BETWEEN ADJACENT LEVELS IS. .100000U-04
FOR THE FREQUENCY .60000008-94
THE ABSORPTION COEFICIENT IS .58108098E-94
THE REFRACTIVE INDEX HIMUS UNITY IS -.30064801E-94
THE PUMP FREQUENCIES ARE .60000000-04 .154500000-04 THE POPULATION TRANSFERSO BETWEEN ADJACENT LEVELS IS: .10000000-04
FOR THE FREQUENCY .15450000E-04
THE ABSORPTION COEFICIENT IS .36373412E-03
THE REFRACTIVE INDUSTRIBUTE TO THE REFRACTIVE TO THE REF
.15500000£ .04
                                                                              .10000000E-04
FOR THE FREQUENCY .60000008-04
THE ABSURPTION COEFICIENT IS .58108098E-04
THE REFRACTIVE INDEX NIHUS UNITY IS -.3000001E-04
FOR THE FREQUENCY .15500000E-04
THE ABSORPTION COEFICIENT IS .36164608E-03
```

the state of the s

```
FOR THE FREQUENCY ,155:0000E-06
THE ABSORPTION COEFICIENT IS -J598326E-03
THE REFRACTIVE INDEX HIMUS UNITY IS --J5390728E-03
THE PUPPLEATION TRANSFERGO BETWEEN ADJACENT LEVELS (3. .10000000-04
FOR THE FREQUENCY
                  .60000008.04
THE ABSORPTION COEFICIENT IS .SB108098E-84
THE REFRACTIVE INDEX MINUS UNITY IS --38664881E-84
FOR THE FREQUENCY .1500000404-04
THE ABSORPTION COEFICIENT IS -35754538E-03
THE REFRACTIVE INDEX HINUS UNITY IS --35119820E-03
FOR THE FREQUENCY .60000000-04
THE ABSORPTION COEFTCIENT 15 .58108078E-04
THE REFRACTIVE NIBUR NEWLY IN 15 -.3846401E-04
FOR THE FREQUENCY ,6000000-04
THE ABSORPTION COEFICIENT 15 .3810809RE-04
THE REFRACTIVE INDEX IN SUMIT YOU SHEARCH.
FOR THE FREQUENCY .1570000000-06
THE REPROTION COEFTCIENT IS -3536464E-03
THE REFRACTION DIVING SUNIT SYNCETTS --3658212E-03
```

```
FOR THE FREQUENCY .15750000E-94
THE ABSORPTION COEFICIENT IS -3515788HE-03
THE REFRACTIVE INDEX HIBUS UNITY IS --34321444E-03
 .15860000€.04
5. .1000000€-04
FOR THE FREQUENCY .1000000E-00
THE RESOPPTION COEFICIENT IS -34403027E-03
THE REFRACTIVE INDEX HIMUS UNITY IS --34050901E-03
THE PUMP FREQUENCIES ARE .6000000E-04 .15850000E-04
THE POPULATION TRANSFERED BETWEEN ADJACENT LEVELS IS. .1000000E-04
FOR THE FREQUENCY .60000000-04
THE REPROTION COEFICIENT IS .58108098E-04
THE REFRACTIVE INJET HIMLE UNITY IS -.3000000E-04
FOR THE FREQUENCY .15850000E-04
THE ABSORPTION COEFICIENT IS .34772130E-03
THE REFRACTIVE INDEX HIWUS UNITY IS -.33000018E-03
THE PUMP FREQUENCISS ARE .60-000000.11.
THE POPULATION TRANSFERED BETWEEN ADJACENT LEVELS IS.
                                                                                                                                                                                                          .15900000E+04
                                                                                                                                                                                                                                            .1000000E-04
FOR THE FREQUENCY .60000000-04
THE ABSORPTION COEFICIENT IS -SB108090E-04
THE REFRACTIVE NYOUN EUNIT NYON TO BE SEEN THE REFRACTIVE NYOUN THE REFRACTIVE NYO
FOR THE FREQUENCY ,15900004E+06
THE AUSORPTION COEFICIENT IS -34582799E-03
THE REFRACTIVE INOFX NEWS UNITY IS --32543696E-03
THE PUMP FREQUENCIES ARE .6000000E-04 .15950000E-04
THE POPULATION TRANSFERED BETWEEN ADJACENT LEVELS IS. .10000000E-04
FOR THE FREQUENCY .60000000-04
THE ABSOMPTION COEFICIENT IS .58108098E-04
THE REFRACTIVE INDEX HINUS UNITY IS -.38664801E-04
FOR THE FREQUENCY ,15950000E-04
THE ABSOMPTION COEFICIENT IS .34395787E-03
THE REFRACTIVE INDEX MINUS UNITY IS -.3289192E-03
```

```
FOR THE FREQUENCY , 14400004046
THE ABSORPTION COEFICIENT IS -JA211000E-03
THE REFRACTIVE INDEX HINLS UNITY IS --J3036676E-03
FOR THE FREQUENCY .60000000-06
THE ABSORPTION COEFICIENT IS -88100000E-06
THE REFRACTIVE INDEX HINUS UNITY IS --3006601E-06
FOR THE PREQUENCY .104500060-46
THE ABSORPTION COEFTCIENT IS -JAC26657E-03
THE REFRACTIVE INDEX HIWUS UNLIT IS --J2786317E-03
A0-300000161. A0-3000000000. SAR 2313MBUD3RR MHUR SHT 1000 OR 15 CLBVSJ THSDALDA MBSWEGG DRGSTEMART MOLIALUPDOR SHT
                                                                                                                                                                                                                                                                                                                                                                               .10000000E-04
  FOR THE FREQUENCY .6000000E-04
THE ABSORPTION COEFICIENT IS -SBIGGOOE-04
THE REFRACTIVE INDEX HINUS UNITY IS --3000600E-06
 FOR THE FREQUENCY
FOR THE FREQUENCY .101000048-00
THE ABSORPTION COEFFCIENT IS .33848-07E-03
THE REFRACTIVE INDEX HINUS UNTITY IS -.32538085E-03
FOR THE FREQUENCY .600000000 APPROPRIES OF THE NATIONAL PROPRIES OF THE STREET OF THE SHIPLE 
 FOR THE FREQUENCY .10150000E+U4
THE ABSORPTION COEFICIENT IS -13670500E-03
THE REFRACTIVE INDEX HIGHES UNITY IS -13291951E-03
 +0+300005ci, 40+300000cc, 3Ac 7:3030000cc, in consistence of the constant moltage of the constant molt
FOR THE FREQUENCY .10000000E-04
THE ABSORPTION COEFICIENT IS .3349486E-03
THE REFRACTIVE INDEX HIMUS UNITY IS -.3647887E-03
```

```
THE PUMP FREQUENCIES AME

THE POPULATION TRANSFERED BETWEEN ADJACENT LEVELS IS, "1000000E-04

FOR THE PREQUENCY ADDROSOSE 04

FOR THE PREQUENCY ADDROSOSE 04

THE ASSONPTION COEFICIENT IS "SUICED SELECTION OF THE PREQUENCY ADDROSOSE 04

THE ASSONPTION COEFICIENT IS "33321397E-03

THE ASSONPTION COEFICIENT IS "33321397E-03

THE PUMP FREQUENCY ADDROSOSE 04

THE PUMP FREQUENCY ADDROSOSE 04

THE PUMP FREQUENCY ADDROSOSE 04

THE ASSONPTION COEFICIENT IS "SUICED NACE 04

THE ASSONPTION COEFICIENT IS "SUICED NACE 04

THE REPRACTIVE INDEX NIMES UNITY IS "3335000E-04

THE REPRACTIVE INDEX NIMES UNITY IS "33150000E-04

THE PUMP FREQUENCY ADDROSOSE 06

THE PREQUENCY ADDROSOSE 06

THE REPRACTIVE INDEX NIMUS UNITY IS "31327820E-03

THE REPRACTIVE INDEX NIMUS UNITY IS "3100000E-06

THE REQUENCY ADDROSOSE 06

THE REPRACTIVE INDEX NIMUS UNITY IS "3100000E-06

THE PROPULATION COEFICIENT IS "320000E-06

THE PROPULATION COEFICIENT IS "320000E-06

THE PREQUENCY ADDROSOSE 06

THE PROPULATION COEFICIENT IS "320000E-06

THE PREQUENCY ADDROSOSE 06

THE PREQUENCY AD
```

```
THE ABSOMPTION COEFICIENT IS .202350744-43
THE REFRACTIVE INDEX MINUS UNITY IS -.19332750E-03
.400000000004.
FOR THE FREQUENCY
THE ASSORPTION COEFICIENT IS .SGIGGGGE-64
THE REFRACTIVE INDEX HINUS UNITY IS -.38664801E-64
FOR THE FREQUENCY ,19990000-04-
THE ABSORPTION COEFICIENT IS --20100095E-03
THE REFRACTIVE INDEX HILWUS WITTY IS --19176678E-03
THE POPULATION TRANSFERED SETUCEN ADJACENT LEVELS IS. .10000000-04
FOR THE FREQUENCY .6000000E-06
THE ABSORPTION COEFICIENT IS .50100000E-06
THE REPRACTIVE INDEX HINUS UNITY IS -.300660E-06
THE PURP FREQUENCIFS ARE .40000000. .19050000E-04-THE POPULATION TRANSFERED BETWEEN ADJACENT LEVELS IS. .10000000E-04-
FOR THE FREQUENCY .6900000E-0a
THE ABSORPTION COEFICIENT IS .SE10000E-0a
THE REFRACTIVE INDEX HINUS UNITY IS -.3000001E-0a
FOR THE FREQUENCY .: 19950000E-96
THE 1933RPTION COEFICIENT 19 -20101536E-93
THE PERACTIVE INDEX HIMUS UNITY 15 -: 18000653E-93
FOR THE FREQUENCY .6000000E-06
THE ABSONPTION COEFTCIENT IS .58108098E-06
THE REFRACTIVE INDEX HIGHS UNITY IS -.1806A801E-06
FOR THE FREQUENCY .14700000E-06
THE ABSORPTION COEFFCIENT IS -26060017E-03
THE REFRACTIVE INDEX HIBUS UNITY IS --18712670E-03
THE PUMP FREQUENCIFS ARE .6000000E-04 .19750000E-04
THE POPULATION TRANSFERED DETWEEN ADJACENT LEVELS IS. .1000000E-04
FOR THE FREQUENCY .40000000-04
```

```
THE ABSOMPTION COEFICIENT IS .5818888E-04
THE REPRACTIVE INDEX NIMUS UNITY IS ... 3846468E-04
FOR THE FREQUENCY .197900000-04
THE RESORPTION COEFICIENT IS .26022382E-03
THE REFRACTIVE INDFX HINUS UNITY IS -.18559353E-03
THE PUMP PHEQUENCIES AME .6000000E-04 .19800000E-04
THE POPULATION TRANSFERGO BETWEEN ADJACENT LEVELS IS. .1000
                                                                                                       -1000000E-04
FOR THE PREQUENCY .6000000E-04
THE ABSORPTION COEFICIENT IS .58108098E-04
THE REFRACTIVE INDEX HINUS UMITY IS -.30064801E-04
FOR THE FREQUENCY .1900000E-04
THE ABSORPTION COEFICTENT IS .25905956E-03
THE REFRACTIVE INDEX HINUS UNITY IS -.1000000E-03
THE PUMP FMEQUENCIES AME .40000000E-04 .19050000E-04 THE POPULATION TRANSFERED BETWEEN ADJACENT LEVELS IS. .10000000E-04
 FOR THE FREQUENCY .19850000E+04
THE ABSORPTION COEFICIENT IS -25951645E-03
THE REFRACTIVE INDEX HINUS UNITY IS -.18254654E-03
 THE PUMP FREQUENCIES ARE .19908080-04 .19908080-04 .19908080-04 .19908080-04 .19908080-04
 FOR THE FREQUENCY .6000000E-04
THE ABSORPTION COEFICIENT IS .58108098E-04
THE REFRACTIVE INDEX HILMUS UNITY IS -.3866401E-04
 THE PUMP PHEQUENCIES ARE .60000000E-04 .19
THE POPULATION TRANSFERED BETWEEN ADJACENT LEVELS IS.
                                                                                         .19950000E+04
  FOR THE FREQUENCY .60000000-04
THE ABSONOTION COEFICIENT IS .58108098E-04
THE REFRACTIVE INDEX MINUS UNITY IS -.20040401E-04
  FOR THE FREQUENCY .19950008+06
THE ABSOMPTION COEFICIENT IS -25889503E-03
THE REFRACTIVE INOFX HINUS UNITY IS --17952437E-03
```

```
THE PUMP PHEUDENCIES ARE THE POPULATION TRANSFERED BETWEEN ADJACENT LEVELS IS. .10000000-00-
FOR THE FREQUENCY .6000000E-04
THE ABSORPTION COEFICIENT IS .5810000E-04
THE REFRACTIVE INDEX HIMUS UNITY IS ..3000001E-04
FOR THE FREQUENCY .2000000E-04
THE ABSORPTION COEFFCIENT IS -25841715E-03
THE REFRACTIVE INDEX HINUS UNITY IS --17802221E-03
FOR THE FREQUENCY .6000000E-06
THE ABSORPTION COEFTCIENT IS .58108090E-06
THE REFRACTIVE INDEX HILWIS UNITY IS -.38666001E-06
FOR THE FREQUENCY .20050000E-06
THE ABSONPTION COEFICIENT IS -25036150E-03
THE REFRACTIVE INOPERIMENS UNITY IS --1762500E-03
THE PUMP FREQUENCIES ARE .60000000-04 .21
THE POPULATION TRANSFERED SETMEEN ADJACENT LEVELS IS.
                                                                                                                                                                                                 .20100000E-04
                                                                                                                                                                                                                                    -10000000E-0+
FOR THE FREQUENCY .20100004044
THE ABSONATION COEFICIENT IS -250120398-03
THE REFRACTIVE INDEX HIMUS UNITY IS --17503497E-03
 THE PUMP FREQUENCIES ARE .6000000E-04 .20150000E-04
THE POPULATION TRANSFERED DETMEEN ADJACENT LEVELS IS. .10000000E-04
FOR THE FREQUENCY .6000000E-06
THE ABSORPTION COEFTCIENT IS -58108090E-06
THE REFRACTIVE INDEX HIBUS UNITY IS -.3000001E-06
FOR THE FREQUENCY .2019006104
THE ABSORPTION COEPICIENT 13 -25'0061078020A
THE REFRACTICE INOPERING SUNIT MORE SYSTEM.
AD-300000505. AD-3000000500. AD-30000000-04 AD-3000000500 AD-300000000-04 AD-300000000-04 AD-30000000-04 AD-30000000-04 AD-30000000-04 AD-30000000-04 AD-30000000-04 AD-3000000-04 AD-3000000-04 AD-3000000-04 AD-3000000-04 AD-3000000-04 AD-3000000-04 AD-300000-04 AD-30000-04 AD-3000-04 AD-300
FOR THE FREQUENCY .2020000E-06
THE ABSORPTION COEFICIENT IS .25773072E-03
THE REFRACTIVE INDPX HIMUS UNITY IS --17200950E-03
```

FOR THE FREQUENCY .20450000E-04 THE ABSORPTION COEFICIENT IS .257[5]05E-03 THE REFRACTIVE INDEX HILMUS UNITY IS -.16474296E-03

FOR THE FREQUENCY .698888884 AND THE RESULTED HOTTENDERS BIT FRESCHIED HOTTENDERS THE RESULT BYSTOCH STEEL BYSTOCH B

FOR THE FREQUENCY .200000E-06
THE ABSOMPTION COEFICIENT IS .25711006E-03
THE REFRACTIVE INDEX HINUS WITH SO -- 16-52913E-03

THATES ALL